

ASCENT
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Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

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Bridge Girder Design Report

Powered by Autodesk Structural Bridge Design 2016

Design: Pre-tensioned Prestressed Concrete Girder
Analysis: Line Girder - Simplified Analysis using Transverse Distribution Method

Design Code: AASHTO LRFD Bridge Design Specifications
Sixth Edition with 2013 Interim Revisions

Bridge: Bridge 2
Girder Line: 11
Girder: Girder group 1 > Right exterior

Overall Performance Ratio = 1.05

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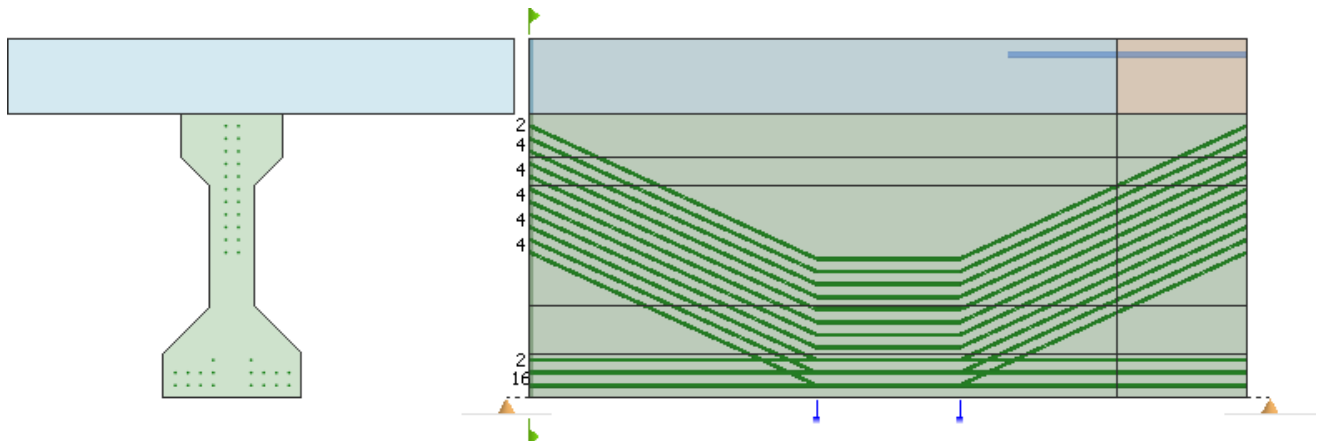
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Girder Design Summary

Descending Performance Ratios

Span	Girder	Performance	Analysis Type	Limit State	Loadcase
S1	L1	1.05	Live Load Bending	Service I/III	Max +ve
		0.96	Prestress Transfer	Service I/III	-
		0.81	Erection Stage	Service I/III	-
		0.74	Live Load Bending	Strength	Max +ve
		0.69	Construction Stage	Service I/III	-
		0.53	Live Load Bending	Strength	Max -ve
		0.52	Live Load Bending	Service I/III	Max -ve
		0.52	Shear	Strength	-



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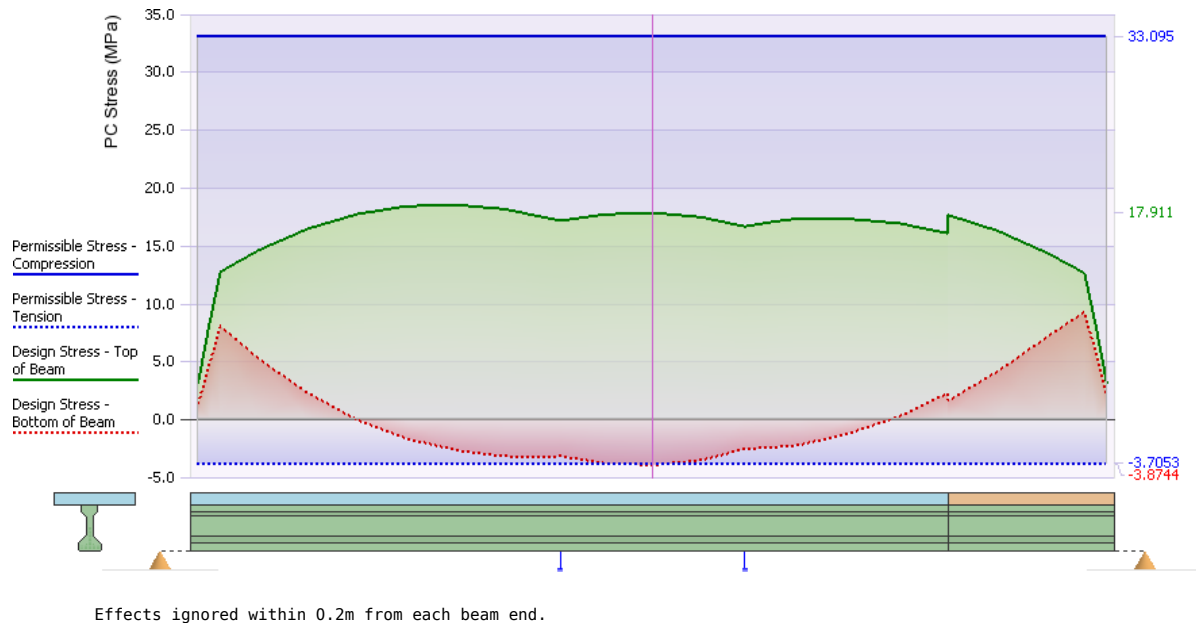
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Girder Design Calculations: Live Load Bending



Performance ratio = $-3.87 / -3.71 = 1.05$

Section details:

Ref 1 "Section 1"
at $0.5 \times \text{span} = 0.5 \times 23.1136 = 11.5568$ m from left end of beam

Design Code:

AASHTO LRFD Bridge Design Specifications
Sixth Edition with 2013 Interim Revisions

Analysis:

Live Load Bending Moments
Transient Load BM 1 : [Max +ve]
Limit State - Service I
& Service III
for Normal environment conditions [A5.9.4.2.2b]

Approximate Methods of Analysis are used - Article 4.6.2

Live Load Distribution Factor for +ve Moment = 0.94124 lanes/beam
Live Load Distribution Factor for -ve Moment = 0.94124 lanes/beam
Live Load Distribution Factor for Shear = 0.94124 lanes/beam
Live Load Distribution Factor for Fatigue = 0.78437 lanes/beam

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ACTUAL STRESSES IN PRECAST BEAM

40 tendons are fully bonded at this section
0 tendons are fully debonded at this section
0 tendons are harped at this section

INITIAL PRESTRESS

height mm	No of tendons	f_{pu} MPa	area mm ²	% of f_{pu}	initial force kN
50.8	8	1861.58	98.71	75.0	1102.542
50.8	2	1861.58	98.71	75.0	275.17634
101.6	8	1861.58	98.71	75.0	1102.542
101.6	2	1861.58	98.71	75.0	275.17634
152.4	2	1861.58	98.71	75.0	275.6355
152.4	2	1861.58	98.71	75.0	275.17634
203.2	2	1861.58	98.71	75.0	275.17634
254.0	2	1861.58	98.71	75.0	275.17634
304.8	2	1861.58	98.71	75.0	275.17634
355.6	2	1861.58	98.71	75.0	275.17634
406.4	2	1861.58	98.71	75.0	275.17634
457.2	2	1861.58	98.71	75.0	275.17634
508.0	2	1861.58	98.71	75.0	275.17634
558.8	2	1861.58	98.71	75.0	275.17634
TOTAL	40				5507.6592

Transverse Eccentricity

Tendon layout is symmetrical about the vertical centroidal axis.

INITIAL RELAXATION - Article 5.9.5.4.4b

Data has the time from stressing to transfer set to zero, indicating that initial relaxation is not required to be calculated here.

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height mm	No of tendons	f_{pj}	f_{py} MPa	relax.	After relaxation		
				loss	area mm ²	force kN	moment kN.m
50.8	8	1396.19	1675.43	0.0	98.71	1102.542	56.009134
50.8	2	1393.86	1675.43	0.0	98.71	275.17634	13.978958
101.6	8	1396.19	1675.43	0.0	98.71	1102.542	112.01827
101.6	2	1393.86	1675.43	0.0	98.71	275.17634	27.957916
152.4	2	1396.19	1675.43	0.0	98.71	275.6355	42.006851
152.4	2	1393.86	1675.43	0.0	98.71	275.17634	41.936874
203.2	2	1393.86	1675.43	0.0	98.71	275.17634	55.915832
254.0	2	1393.86	1675.43	0.0	98.71	275.17634	69.89479
304.8	2	1393.86	1675.43	0.0	98.71	275.17634	83.873748
355.6	2	1393.86	1675.43	0.0	98.71	275.17634	97.852705
406.4	2	1393.86	1675.43	0.0	98.71	275.17634	111.83166
457.2	2	1393.86	1675.43	0.0	98.71	275.17634	125.81062
508.0	2	1393.86	1675.43	0.0	98.71	275.17634	139.78958
558.8	2	1393.86	1675.43	0.0	98.71	275.17634	153.76854
TOTAL	40					5507.6592	1132.6455

Moment about the centroid of the precast beam:

$$M_r = 1132.6455 - (5507.6592 * 0.514946) \\ = -1703.501 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 5507.66 / 360.967 + (-1703.5 / 8.31E7) \\ &= 15.258068 + (-20.49937) \\ &= -5.2413 \text{ MPa} \\ \text{bottom stress} &= 5507.66 / 360.967 + (-1703.5 / -1.014E8) \\ &= 15.258068 + 16.807569 \\ &= 32.0656 \text{ MPa} \end{aligned}$$

Self weight moment:

$$\begin{aligned} \text{c.s.a.} &= 3.61E5 \text{ mm}^2 \\ \text{density} &= 23.5631 \text{ kN/m}^3 \\ \text{self weight} &= 3.61E5 * 23.5631 \\ &= 8.50551 \text{ kN/m} \\ \text{beam length} &= 23.1136 \text{ m} \\ \text{distance} &= 11.5568 \text{ m} \\ M_{sw} &= 0.5 * 8.50551 * 11.5568 * (23.1136 - 11.5568) \\ &= 567.998 \text{ kN.m} \end{aligned}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 567.998 / 8.31E7 \\ &= 6.83511 \text{ MPa} \\ \text{bottom stress} &= 567.998 / -1.014E8 \\ &= -5.6041 \text{ MPa} \end{aligned}$$

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ELASTIC SHORTENING LOSSES - Article 5.9.5.2.3a

concrete stresses at mid-span:

stress at top of precast beam = 1.59381 MPa

stress at bottom of precast beam = 26.4615 MPa

depth of precast beam = 1143.0 mm

height mm	No of tendons	conc stress MPa	E_p/E_{ci}	tendon force kN	tendon moment kN.m
50.8	10	25.35626	6.084443	152.28851	7.7362564
101.6	10	24.25103	6.084443	145.65055	14.798096
152.4	4	23.1458	6.084443	55.605035	8.4742074
203.2	2	22.04057	6.084443	26.474925	5.3797048
254.0	2	20.93534	6.084443	25.147333	6.3874226
304.8	2	19.83011	6.084443	23.819741	7.2602569
355.6	2	18.72488	6.084443	22.492148	7.9982079
406.4	2	17.61965	6.084443	21.164556	8.6012755
457.2	2	16.51442	6.084443	19.836963	9.0694597
508.0	2	15.40919	6.084443	18.509371	9.4027605
558.8	2	14.30395	6.084443	17.181779	9.6011779
TOTAL	40			528.17091	94.708826

Moment about the centroid of the precast beam:

$$M_{ed} = 94.708826 - (528.17091 \times 0.514946)$$

$$= -177.2706 \text{ kN.m}$$

$$\text{hence top stress} = 1.5938 - 528.171/360.967 - (-177.271/8.31E7)$$

$$= 1.5938 - 1.463211 - (-2.133216)$$

$$= 2.26381 \text{ MPa}$$

$$\text{bottom stress} = 26.461 - 528.171/360.967 - (-177.271/-1.014E8)$$

$$= 26.461 - 1.463211 - 1.7490381$$

$$= 23.2492 \text{ MPa}$$

After a further 2 iterations of the above process, the top and bottom stresses are as follows:

$$\text{top stress} = 2.18992 \text{ MPa}$$

$$\text{bottom stress} = 23.579 \text{ MPa}$$

REFINED ESTIMATES OF TIME-DEPENDENT LOSSES - Article 5.9.5.4

Elastic modulus of prestressing steel: $E_p = 197.0 \text{ kN/mm}^2$

Total effective tendon area: $A_{ps} = 3944.8 \text{ mm}^2$

Elastic modulus of concrete at transfer: $E_{ci} = 32.378 \text{ kN/mm}^2$

Percentage relative humidity: $H = 70.0 \%$

Humidity factor for creep: $k_{hc} = 1.56 - 0.008H = 1.0$

Humidity factor for shrinkage: $k_{hs} = 2.00 - 0.014H = 1.02$

Age at the end of curing: $t_c = 3.0 \text{ day}$

Age at transfer: $t_i = 4.0 \text{ day}$

Age at in-situ casting: $t_d = 60.0 \text{ day}$

Final age: $t_f = 120.0 \text{ day}$

Comp. strength of conc. at 1st loading: $f'_{ci} = 41.37 \text{ MPa}$

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$$\text{Factor for the effect of concrete strength: } k_f = \frac{35.0}{7 + f'_{ci}} = \frac{35.0}{7 + 41.4} = 0.7236$$

$$\begin{aligned} \text{Time factor for creep at final time: } k_{tdc, f, i} &= \frac{t_f - t_i}{61 - 0.58 * f'_{ci} + t_f - t_i} \\ &= \frac{120.0 - 4.0}{61 - 0.58 * 41.4 + 120.0 - 4.0} \\ &= 0.7581 \end{aligned}$$

$$\begin{aligned} \text{Time fac. for shrinkage at final time: } k_{tds, f, i} &= \frac{t_f - t_c}{61 - 0.58 * f'_{ci} + t_f - t_c} \\ &= \frac{120.0 - 3.0}{61 - 0.58 * 41.4 + 120.0 - 3.0} \\ &= 0.7597 \end{aligned}$$

Losses: Time of Transfer to Time of Deck Placement - Article 5.9.5.4.2

$$\begin{aligned} \text{Gross area of section: } A_g &= 3.61\text{E}5 \text{ mm}^2 \\ \text{Perimeter of section: } p &= 3503.7 \text{ mm} \\ \text{Volume to surface ratio: } V/S &= A_g/p = 103.02 \text{ mm} \\ \text{Factor for the effect of the volume: } k_s &= 1.45 - 0.0051 * (V/S) = 0.9245 \\ \text{Creep coefficient at final time: } \psi_b(t_f, t_i) &= 1.9 * k_s * k_{hc} * k_f * k_{tdc, f, i} * t_i^{-0.118} \\ &= 1.9 * 0.9245 * 1.0 * 0.7236 * 0.7581 * 4.0^{-0.118} \\ &= 0.8182 \\ \text{Inertia of the gross concrete section: } I_g &= 5.22\text{E}10 \text{ mm}^4 \\ \text{Eccentricity of prestressing force: } e_{pg} &= -306.91 \text{ mm} \end{aligned}$$

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Transformed section coefficient:

$$K_{id} = \frac{1}{1 + \frac{E_p}{E_{ci}} \cdot \frac{A_{ps}}{A_g} \left[1 + \frac{A_g \cdot e_{pg}^2}{I_g} \right] \cdot [1 + 0.7 \cdot \psi_b(t_f, t_i)]}$$

$$= \frac{1}{1 + \frac{197.0}{32.378} \cdot \frac{3944.8}{3.61E5} \left[1 + \frac{3.61E5 \cdot 306.9^2}{5.2E10} \right] \cdot (1 + 0.7 \cdot 0.8182)}$$

$$= 0.85272$$

Time factor for creep at deck placement:

$$k_{tdc,d,i} = \frac{t_d - t_i}{61 - 0.58 \cdot f'_{ci} + t_d - t_i}$$

$$= \frac{60.0 - 4.0}{61 - 0.58 \cdot 41.4 + 60.0 - 4.0}$$

$$= 0.602$$

Time factor for shrinkage at deck placement:

$$k_{tds,d,i} = \frac{t_d - t_c}{61 - 0.58 \cdot f'_{ci} + t_d - t_c}$$

$$= \frac{60.0 - 3.0}{61 - 0.58 \cdot 41.4 + 60.0 - 3.0}$$

$$= 0.606$$

Shrinkage of Girder Concrete - Article 5.9.5.4.2a

Concrete shrinkage strain of girder: $\epsilon_{bid} = k_s \cdot k_{hs} \cdot k_f \cdot k_{tds,d,i} \cdot 0.00048$

$$= 1.0 \cdot 1.02 \cdot 0.71 \cdot 0.60 \cdot 0.00048$$

$$= 2.121E-4$$

Loss of prestress = $\epsilon_{bid} \cdot E_p \cdot K_{id}$

$$= 2.12E-4 \cdot 197.0 \cdot 0.84963$$

$$= 35.495 \text{ MPa}$$

$$= \Delta f_{psR}$$

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$$\begin{aligned}\text{Total shrinkage loss of force} &= \Delta f_{pSR} \cdot A_{ps} \\ &= 35.4945 \cdot 3944.78 \\ &= 140.018 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding gain of moment} &= 140.018 \cdot 0.20803 \\ (\text{about } y = 0) &= 29.1282 \text{ kN.m}\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{sh} &= 29.1282 - (140.018 \cdot 0.51494) \\ &= -42.974 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 140.018 / 360967 + (-42.9735 / 8.31E7) \\ &= 0.3878972 + (-0.517129) \\ &= -0.129232 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 140.018 / 360967 + (-42.9735 / -1.014E8) \\ &= 0.3878972 + 0.4239978 \\ &= 0.811895 \text{ MPa}\end{aligned}$$

Creep of Girder Concrete - Article 5.9.5.4.2b

Creep coefficient at deck placement:

$$\begin{aligned}\psi_b(t_d, t_i) &= 1.9 k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, d, i} \cdot t_i^{-0.118} \\ &= 1.9 \cdot 1.0 \cdot 1.0 \cdot 0.7142 \cdot 0.6021 \cdot 4.0^{-0.118} \\ &= 0.6938\end{aligned}$$

Concrete stress at the center of gravity of prestressing tendons:

concrete stresses at transfer:

$$\begin{aligned}\text{at top of precast beam} &= 1.75172 \text{ MPa} \\ \text{at bottom of precast beam} &= 26.332 \text{ MPa} \\ \text{at center of gravity of prestress: } f_{cgp} &= 21.8583 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{Loss of prestress} &= \frac{E_p}{E_{ci}} \cdot f_{cgp} \cdot \psi_b(t_d, t_i) \cdot K_{id} \\ &= \frac{197.0}{32.3777} \cdot 21.858 \cdot 0.6938 \cdot 0.8576 \\ &= 79.1425 \text{ MPa} \\ &= \Delta f_{PCR}\end{aligned}$$

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$$\begin{aligned}\text{Total creep loss of force} &= \Delta f_{pCR} \cdot A_{ps} \\ &= 79.1425 \cdot 3944.78 \\ &= 312.2 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding loss of moment} &= 312.2 \cdot 0.20803 \\ &= 64.9475 \text{ kN.m} \\ &\quad (\text{about } y = 0)\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{Cr} &= 64.9475 - (312.2 \cdot 0.51494) \\ &= -95.819 \text{ kN.m}\end{aligned}$$

$$\begin{aligned}\text{Corresponding stresses:} \\ \text{top stress} &= 312.2 / 3.61\text{E}5 + -95.819 / 8.31002\text{E}7 \\ &= 0.86489 + -1.153 \\ &= -0.2881 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 312.2 / 3.61\text{E}5 + -95.819 / -1.0135\text{E}8 \\ &= 0.86489 + 0.94539 \\ &= 1.81029 \text{ MPa}\end{aligned}$$

Relaxation of Prestressing Strands - Article 5.9.5.4.2c

$$\begin{aligned}\text{Stress in tendons after transfer:} & f_{pt} = 1275.83 \text{ MPa} \\ \text{Yield strength of prestressing steel:} & f_{py} = 1675.43 \text{ MPa} \\ \text{Time between tensioning and deck placement:} & t = t_s - t_i = 60.0 - 4.0 = 56.0 \text{ day} \\ \text{Factor for relaxation steel type:} & K'_L = 45.0 \text{ (low relaxation)}\end{aligned}$$

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$$\begin{aligned} \text{Loss of prestress} &= \frac{f_{pt}}{K'_L} \cdot \frac{\log(24t)}{\log(24t_i)} \cdot \left[\frac{f_{pt}}{f_{py}} - 0.55 \right] \cdot \left[1 - \frac{3(\Delta f_{pSR} + \Delta f_{pCR})}{f_{pt}} \right] \cdot K_{id} \\ &= \frac{1275.8}{45.0} \cdot \frac{\log(24 \cdot 56.0)}{\log(24 \cdot 4.0)} \cdot \left[\frac{1275.8}{1675.4} - 0.55 \right] \cdot \left[1 - \frac{3 \cdot (35.495 + 79.142)}{1275.8} \right] \cdot 0.85 \\ &= 5.87309 \text{ MPa} \\ &= \Delta f_{pR1} \end{aligned}$$

$$\begin{aligned} \text{Total relaxation loss of force} &= \Delta f_{pR1} \cdot A_{ps} \\ &= 5.8731 \cdot 3944.8 \\ &= 23.168069 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Corresponding loss of moment} &= 23.168 \cdot 0.2080 \\ &= 4.8196938 \text{ kN.m} \\ &\quad (\text{about } y = 0) \end{aligned}$$

$$\begin{aligned} \text{Moment about the centroid of the composite beam:} \\ M_{rx} &= 4.81969 - (23.1681 \cdot 0.5149) \\ &= -7.1106 \text{ kN.m} \end{aligned}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 23.1681/360967 + -7.11061/8.31E7 \\ &= 0.0641833 + -0.085567 \\ &= -0.0213834 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 23.1681/360967 + -7.11061/-1.014E8 \\ &= 0.0641833 + 0.0701567 \\ &= 0.13434 \text{ MPa} \end{aligned}$$

Erection of beam Loading

Bending moment from erection loadcase at current span location:

$$M_{\text{Applied}} = 674.56207 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 674.56207/8.31E7 \\ &= 8.11746 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 674.56207/-1.014E8 \\ &= -6.6556 \text{ MPa} \end{aligned}$$

Remove the dead load applied for transfer calculations

$$M_{sw} = -568.0 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= -568.0/8.31E7 \\ &= -6.8351 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= -568.0/-1.014E8 \\ &= 5.60415 \text{ MPa} \end{aligned}$$

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Construction stage 1A Loading

$$M_{\text{Applied}} = 1017.5579 \text{ kN.m}$$

Corresponding stresses:

$$\text{top stress} = 1017.5579/8.31\text{E}7$$

$$= 12.245 \text{ MPa}$$

$$\text{bottom stress} = 1017.5579/-1.014\text{E}8$$

$$= -10.04 \text{ MPa}$$

Construction stage 1B Loading

$$M_{\text{Applied}} = 89.601562 \text{ kN.m}$$

Corresponding stresses:

$$\text{top stress} = 89.601562/8.31\text{E}7$$

$$= 1.07824 \text{ MPa}$$

$$\text{bottom stress} = 89.601562/-1.014\text{E}8$$

$$= -0.8840 \text{ MPa}$$

Losses: Time of Deck Placement to Final Time - Article 5.9.5.4.3

$$\text{Gross composite section area: } A_c = 9.72\text{E}5 \text{ mm}^2$$

$$\text{Perimeter of section: } p = 7365.6 \text{ mm}$$

$$\text{Volume to surface ratio: } V/S = A_c/p = 131.99 \text{ mm}$$

$$\text{Factor for the effect of the volume: } k_s = 1.45 - 0.0051 \cdot (V/S) = 0.7768$$

Creep coefficient at final time:

$$\begin{aligned} \psi_b(t_f, t_i) &= 1.9 \cdot k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, f, i} \cdot t_i^{-0.118} \\ &= 1.9 \cdot 0.776 \cdot 1.0 \cdot 0.723 \cdot 0.758 \cdot 4.0^{-0.118} \\ &= 0.6875 \end{aligned}$$

$$\text{Inertia of the net concrete section: } I_c = 1.94\text{E}8 \text{ mm}^4$$

$$\text{Eccentricity of prestressing force: } e_{pc} = 0.7960 \text{ mm}$$

Transformed section coefficient:

$$\begin{aligned} K_{df} &= \frac{1}{1 + \frac{E_p}{E_{ci}} \cdot \frac{A_{ps}}{A_c} \left[1 + \frac{A_c \cdot e_{pc}^2}{I_c} \right] \cdot [1 + 0.7 \cdot \psi_b(t_f, t_i)]} \\ &= \frac{1}{1 + \frac{197.0}{32.378} \cdot \frac{3944.8}{9.72\text{E}5} \left[1 + \frac{9.72\text{E}5 \cdot 796.07^2}{1.9\text{E}11} \right] \cdot (1 + 0.7 \cdot 0.6875)} \\ &= 0.86758 \end{aligned}$$

Shrinkage of Girder Concrete - Article 5.9.5.4.3a

$$\begin{aligned} \text{Concrete shrinkage strain of girder: } \epsilon_{bdf} &= k_s \cdot k_{hs} \cdot k_f \cdot k_{tds, f, i} \cdot 0.00048 \\ &= 1.0 \cdot 1.02 \cdot 0.71 \cdot 0.76 \cdot 0.00048 \\ &= 2.657\text{E}-4 \end{aligned}$$

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$$\begin{aligned}\text{Loss of prestress} &= \epsilon_{bdf} \cdot E_p \cdot K_{df} \\ &= 2.66\text{E-}4 * 1.97\text{E}8 * 0.85760 \\ &= 44.888 \text{ MPa} \\ &= \Delta f_{pSD}\end{aligned}$$

$$\begin{aligned}\text{Total shrinkage loss of force} &= \Delta f_{pSD} \cdot A_{ps} \\ &= 44.888 * 3944.78 \\ &= 177.073 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding gain of moment} &= 177.073 * 0.20803 \\ (\text{about } y = 0) &= 36.8369 \text{ kN.m}\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{sh} &= 36.8369 - (177.073 * 0.9603) \\ &= -133.21 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 177.073 / 844161 + (-133.207 / 9.901\text{E}8) \\ &= 0.2097626 + (-0.134536) \\ &= 0.0752263 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 177.073 / 844161 + (-133.207 / -1.884\text{E}8) \\ &= 0.2097626 + 0.7071458 \\ &= 0.916909 \text{ MPa}\end{aligned}$$

Creep of Girder Concrete - Article 5.9.5.4.2b

Creep coefficient at deck placement:

$$\begin{aligned}\psi_b(t_d, t_i) &= 1.9k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, d, i} \cdot t_i^{-0.118} \\ &= 1.9 * 1.0 * 1.0 * 0.7142 * 0.6021 * 4.0^{-0.118} \\ &= 0.6938\end{aligned}$$

Creep coefficient at final time:

$$\begin{aligned}\psi_b(t_f, t_d) &= 1.9k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, f, i} \cdot t_d^{-0.118} \\ &= 1.9 * 1.0 * 1.0 * 0.7142 * 0.6185 * 60.0^{-0.118} \\ &= 0.5178\end{aligned}$$

Concrete stress at the center of gravity of prestressing tendons:

concrete stresses at transfer:

$$\begin{aligned}\text{at top of precast beam} &= 1.75172 \text{ MPa} \\ \text{at bottom of precast beam} &= 26.332 \text{ MPa} \\ \text{at center of gravity of prestress: } f_{cgp} &= 21.8583 \text{ MPa}\end{aligned}$$

Change in concrete stress at centroid of prestressing strands:

concrete stress change after permanent loads:

$$\begin{aligned}\text{at top of precast beam} &= 9.85015 \text{ MPa} \\ \text{at bottom of precast beam} &= 12.1033 \text{ MPa} \\ \Delta f_{cd} &= 11.6932 \text{ MPa}\end{aligned}$$

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$$\begin{aligned}
 \text{Loss of prestress} &= \frac{E_p}{E_{ci}} * f_{cgp} * \left[\psi_b(t_f, t_i) - \psi_b(t_d, t_i) \right] * K_{df} \\
 &+ \frac{E_p}{E_c} * \Delta f_{cd} * \psi_b(t_f, t_d) * K_{df} \\
 &= \frac{197.0}{32.3777} * 21.8583 * (0.87367 - 0.69388) * 0.84963 \\
 &+ \frac{197.0}{18.6932} * 11.6932 * 0.51782 * 0.84963 \\
 &= 74.5326 \text{ MPa} \\
 &= \Delta f_{pCD}
 \end{aligned}$$

$$\begin{aligned}
 \text{Total creep loss of force} &= \Delta f_{pCD} * A_{ps} \\
 &= 74.5326 * 3944.78 \\
 &= 294.015 \text{ kN}
 \end{aligned}$$

$$\begin{aligned}
 \text{Corresponding loss of moment} &= 294.015 * 0.20803 \\
 &= 61.1644 \text{ kN.m} \\
 &\quad (\text{about } y = 0)
 \end{aligned}$$

$$\begin{aligned}
 \text{Moment about the centroid of the composite beam:} \\
 M_{cr} &= 61.1644 - (294.015 * 0.9603) \\
 &= -221.18 \text{ kN.m}
 \end{aligned}$$

Corresponding stresses:

$$\begin{aligned}
 \text{top stress} &= 294.015 / 8.442\text{E}5 + -221.18 / 9.90117\text{E}8 \\
 &= 0.34829 + -0.2233 \\
 &= 0.12490 \text{ MPa}
 \end{aligned}$$

$$\begin{aligned}
 \text{bottom stress} &= 294.015 / 8.442\text{E}5 + -221.18 / -1.8837\text{E}8 \\
 &= 0.34829 + 1.17415 \\
 &= 1.52245 \text{ MPa}
 \end{aligned}$$

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Relaxation of Prestressing Strands - Article 5.9.5.4.3c

$$\begin{aligned}\text{Loss of prestress} &= \Delta f_{pR1} \\ &= 5.87309 \text{ MPa} \\ &= \Delta f_{pR2}\end{aligned}$$

$$\begin{aligned}\text{Total relaxation loss of force} &= \Delta f_{pR2} \cdot A_{ps} \\ &= 5.8731 \cdot 3944.8 \\ &= 23.168069 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding loss of moment} &= 23.168 \cdot 0.2080 \\ &= 4.8196938 \text{ kN.m} \\ &\quad (\text{about } y = 0)\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{rx} &= 4.81969 - (23.1681 \cdot 0.9603) \\ &= -17.429 \text{ kN.m}\end{aligned}$$

$$\begin{aligned}\text{Corresponding stresses:} \\ \text{top stress} &= 23.1681/844161 + (-17.4286/9.901E8) \\ &= 0.0274451 + (-0.017603) \\ &= 0.00984252 \text{ MPa} \\ \\ \text{bottom stress} &= 23.1681/844161 + (-17.4286/-1.884E8) \\ &= 0.0274451 + 0.0925221 \\ &= 0.119967 \text{ MPa}\end{aligned}$$

Shrinkage of Deck Concrete - Article 5.9.5.4.3d

$$\begin{aligned}\text{Concrete shrinkage strain of girder:} \quad \epsilon_{ddf} &= k_s \cdot k_{hs} \cdot k_f \cdot k_{tds, f, i} \cdot 0.00048 \\ &= 1.025 \cdot 1.02 \cdot 0.71 \cdot 0.76 \cdot 0.00048 \\ &= 2.724E-4\end{aligned}$$

Creep coefficient at final time:

$$\begin{aligned}\psi_b(t_f, t_d) &= 1.9 k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, f, i} \cdot t_d^{-0.118} \\ &= 1.9 \cdot 1.0253 \cdot 1.0 \cdot 0.7142 \cdot 0.6185 \cdot 60.0^{-0.118} \\ &= 0.5309\end{aligned}$$

Change in concrete stress at centroid of prestressing strands:

$$\begin{aligned}\text{Area of deck concrete:} \quad A_d &= 6.112E5 \text{ mm}^2 \\ \text{Perimeter of section:} \quad p &= 7365.55 \text{ mm} \\ \text{Volume to surface ratio:} \quad V/S &= A_d/p = 82.98 \text{ mm} \\ \text{Factor for the effect of the volume:} \quad k_s &= 1.45 - 0.0051 \cdot (V/S) = 1.4333 \\ \text{Modulus of elasticity of deck concrete:} \quad E_{cd} &= 29.5566 \text{ mm}^2 \\ \text{Eccentricity of the deck:} \quad e_d &= 288.894 \text{ mm}^3\end{aligned}$$

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$$\Delta f_{cdf} = \frac{\epsilon_{ddf} \cdot A_d \cdot E_{cd}}{[1 + 0.7\psi_b(t_f, t_d)]} \left[\frac{1}{A_c} \frac{e_{pc} \cdot e_d}{I_c} \right]$$

$$= \frac{2.7E-4 * 6.11E5 * 29.557 * 1000}{[1 + 0.7 * 0.5309]} \left[\frac{1}{8.44E5} \frac{752.269 * 288.894}{1.8E11} \right]$$

$$= -0.0602 \text{ MPa}$$

$$\text{Loss of prestress} = \frac{E_p}{E_c} \cdot \Delta f_{cdf} \cdot K_{df} \cdot [1 + 0.7\psi_b(t_f, t_d)]$$

$$= \frac{197.0}{18.6932} * -0.0602 * 0.85760 * (1 + 0.7 * 0.53092)$$

$$= -0.7466 \text{ MPa}$$

$$= \Delta f_{pss}$$

$$\begin{aligned} \text{Total shrinkage gain of force} &= \Delta f_{pss} \cdot A_{ps} \\ &= -0.7466 * 3944.78 \\ &= -2.9455 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Corresponding gain of moment} &= -2.9455 * 0.20803 \\ (\text{about } y = 0) &= -0.6127 \text{ kN.m} \end{aligned}$$

$$\begin{aligned} \text{Moment about the centroid of the composite beam:} \\ M_{sh} &= -0.6127 - (-2.9455 * 0.9603) \\ &= 2.21584 \text{ kN.m} \end{aligned}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= -2.94554 / 844161 + 2.21584 / 9.901E8 \\ &= -0.003489 + 0.002238 \\ &= -0.00125136 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= -2.94554 / 844161 + 2.21584 / -1.884E8 \\ &= -0.003489 + -0.011763 \\ &= -0.0152524 \text{ MPa} \end{aligned}$$

Superimposed dead load 1 Loading

$$M_{\text{Applied}} = 148.14137 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 148.14137 / 9.9012E8 \\ &= 0.14962 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 148.14137 / -1.884E8 \\ &= -0.7864 \text{ MPa} \end{aligned}$$

Transient Load BM 1 : [Max +ve] Loading

$$\begin{aligned} M_{\text{Applied}} &= 2250.62 \text{ kN.m} && \text{for Service-I} \\ &= 1800.5 \text{ kN.m} && \text{for Service-III} \end{aligned}$$

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Corresponding stresses:

top stress = 2250.62/9.9012E8	Service-I
= 2.27309 MPa	
bottom stress = 1800.5/-1.884E8	Service-III
= -9.5582 MPa	

PERMISSIBLE STRESSES IN PRECAST BEAM

Compression

Article 5.9.4.2.1 for permanent & transient loads

Permissible compression stress = $0.6 * f'_c$
= $0.6 * 55.1581$
= 33.09 MPa

Tension

Article 5.9.4.2.2

Component is subject to normal exposure conditions.

Permissible tension stress = $-0.498 * \sqrt{f'_c}$
= $-0.498 * \sqrt{55.1581}$
= -3.70451 MPa

PERMISSIBLE STRESSES FOR CAST IN PLACE CONCRETE

Compression

Article 5.9.4.2

char. strength of c.i.p. concrete = 34.4738 MPa
stress limitation factor = 0.6
permissible compression stress = $0.6 * f_{cu}$
= $0.6 * 34.4738$
= 20.6843 MPa

Tension

Article 5.7.3.4

Flexural tensile stresses may need to be limited by cracking considerations
in accordance with article 5.7.3.4.

However, no tensile stress is present at this section.

SERVICE LIMIT STATE - STRESS SUMMARY TABLE

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minimum for girder bottom extreme fibre

Concrete Stresses (MPa)						
	force kN	moment kN.m	Cast In Place		Precast	
			top	bottom	top	bottom
Prestress	5507.66	-1703.5			-5.2413	32.0656
Self Weight		567.998			6.83511	-5.6041
Prestress + Self Wt.					1.59381	26.4615
Elastic Def	-474.77	158.837			0.59611	-2.8825
TRANSFER	5032.88	-976.66			2.18992	23.579
Erection		106.564			1.28235	-1.0514
C.I.P. Stage 1A		1017.56			12.245	-10.04
C.I.P. Stage 1B		89.6016	0.18902	0.07154	0.0905	-0.4756
Time-Dependent Losses						
Time of Transfer to Time of Deck Placement						
Shrinkage	-140.02	42.9735			0.12923	-0.8119
Creep	-312.2	95.8186			0.28815	-1.8103
Relaxation	-23.168	7.11061			0.02138	-0.1343
Time of Deck Placement to Final Time						
Shrinkage						
Girder	-177.07	133.207	0.11517	-0.0595	-0.0752	-0.9169
Deck	27.3485	-20.573	-0.0178	0.00919	0.01162	0.14161
Creep	-294.01	221.178	0.19124	-0.0987	-0.1249	-1.5224
Relaxation	-23.168	17.4286	0.01507	-0.0078	-0.0098	-0.1199
Wearing Surface		148.141	0.31251	0.11828	0.14962	-0.7864
(Diff. Shr. 1	-27.349	20.5734	9.98E-4	0.27517	-0.0116	-0.1416)
(Diff. Shr. 2		-11.207	-0.0236	-0.0089	-0.0113	0.05949)
(Differential shrinkage is not adverse or not specified)						
TOTAL PERMANENT			0.80523	0.03301	16.1978	6.05158
(Y _{TG} = 0.5)						
Temp Grad P1	-752.44	-291.34	2.3162	-0.5968	-0.7549	0.65526
Temp Grad P2		192.707	0.40652	0.15386	0.19463	-1.023
Temp Grad R1	150.487	58.2675	-0.4632	0.11936	0.15098	-0.1310
Temp Grad R2		-38.54	-0.0813	-0.0308	-0.0389	0.20459

(Temperature restraint is not adverse or not specified)

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TRANSIENT LOADS				
Transient Load BM 1- I	2250.62	4.74783	2.27309	
- III	1800.5	1.43763	-9.5582	
Transient Load BM 2- I	-385.71	-0.8136	-0.3895	
- III	-308.57	-0.2463	1.63808	
TOTAL PERMANENT LOAD + TRANSIENT LOAD				
Transient Load BM 1	5.00852	1.0277	17.9106	-3.8744

SLS FLEXURE

calculated using curvature of uncracked sections

The deflections are calculated from integration of the curvatures along the beam, using the parameters detailed below:
(Note that the reported values of deflections for live loadings are exaggerated when these are derived from enveloped effects)

Elastic Modulus at Transfer, $E_T = 32.3777 \text{ kN/mm}^2$
Intermediate Term Elastic Modulus, $E_I = 22.0714 \text{ kN/mm}^2$
 $E_I = E_C / (\psi(t, t_i) + 1)$
where $\psi(t, t_i) = 0.69388$ (Article 5.14.2.3.6)]
Effective Elastic Modulus for time dependant effects, $E_E = 34.2214 \text{ kN/mm}^2$
 $E_E = E_S \cdot (\psi_{tc\%} + ((1 - \psi_{tc\%}) / (1 + \chi \cdot \psi)))$
 ψ = creep factor = 0.87367
 $\psi_{tc\%}$ = percentage of creep occurring before c.i.p. deck added
= $0.69388 / 0.87367 = 79.4216\%$
 χ = ageing factor, taken as 0.8
Short Term Elastic Modulus, $E_S = 37.3865 \text{ kN/mm}^2$

Precast section height = 1143.0 mm

	Precast		Curvature ($\times 10^{-6}$) (rad/m)	Deflection ^[1] (mm)	
	Stress (MPa)	E Strain ($\times 10^{-6}$)		Here	Max.
At Transfer	T 2.11241 B 23.6426	E_T 65.2428 730.213	-581.78	29.9015	30.3396
At Erection	T 3.81257 B 19.8518	E_I 172.738 899.435	-635.78	35.7234	36.1998
Long-term Dead	T 16.0401 B 6.19298				

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Dead Stress Increment	T	13.9277	E_E	406.989	802.181	-48.721	-49.25
	B	-17.45		-509.9			
Total Dead Load deflection				166.4	-12.998	-13.05	
Transient Load BM 1-I	T	2.28985	E_S	61.2481	335.239	-20.45	-20.541
	B	-12.036		-321.93			
Extreme in-service		-5.8429		501.639	-33.448	Cracked	

The stress limit in service (-3.7134MPa) is exceeded.
[Article 5.9.4.2.2]

[1] Deflection 'Cracked' indicates tensile stress at one or more sections along the beam exceeds the stress limit.

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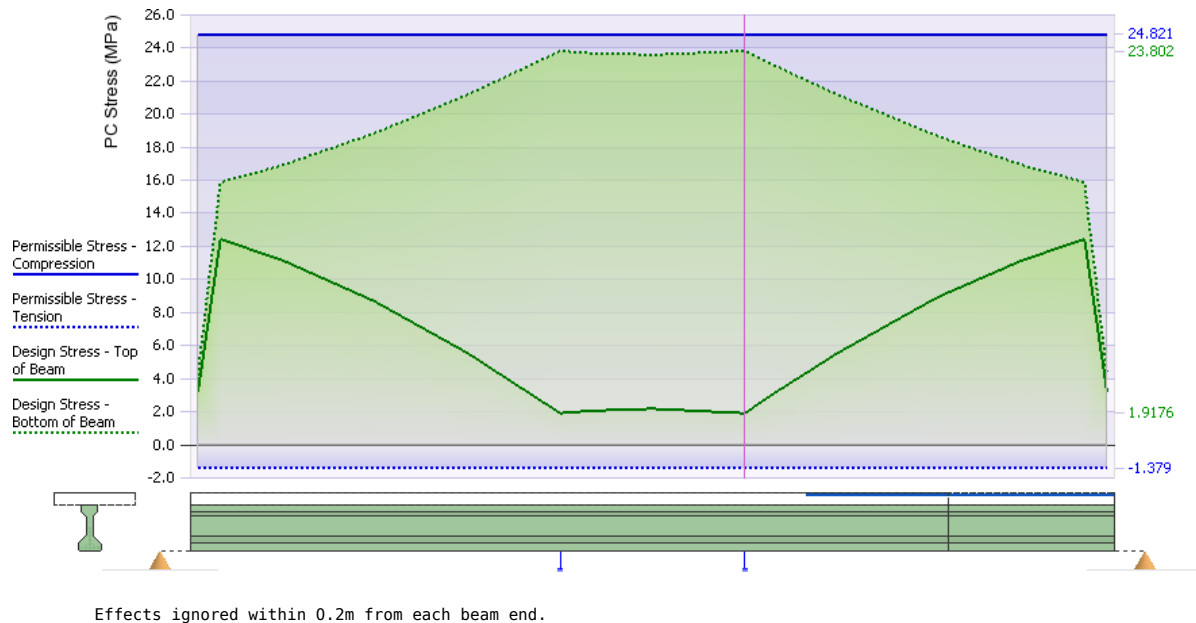
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Girder Design Calculations: Prestress Transfer



Performance ratio = $23.8 / 24.8 = 0.959$

Section details:

Ref 1 "Section 1"
at $0.599 \times \text{span} = 0.599 \times 23.1136 = 13.8636$ m from left end of beam

Design Code:

AASHTO LRFD Bridge Design Specifications
Sixth Edition with 2013 Interim Revisions

Analysis:

Stresses at Transfer

ACTUAL STRESSES IN PRECAST BEAM

40 tendons are fully bonded at this section
0 tendons are fully debonded at this section
0 tendons are harped at this section

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INITIAL PRESTRESS

height mm	No of tendons	f_{pu} MPa	area mm ²	% of f_{pu}	initial force kN
50.8	8	1861.58	98.71	75.0	1102.542
50.8	2	1861.58	98.71	75.0	275.17634
101.6	8	1861.58	98.71	75.0	1102.542
101.6	2	1861.58	98.71	75.0	275.17634
152.4	2	1861.58	98.71	75.0	275.6355
152.4	2	1861.58	98.71	75.0	275.17634
203.2	2	1861.58	98.71	75.0	275.17634
254.0	2	1861.58	98.71	75.0	275.17634
304.8	2	1861.58	98.71	75.0	275.17634
355.6	2	1861.58	98.71	75.0	275.17634
406.4	2	1861.58	98.71	75.0	275.17634
457.2	2	1861.58	98.71	75.0	275.17634
508.0	2	1861.58	98.71	75.0	275.17634
558.8	2	1861.58	98.71	75.0	275.17634
TOTAL	40				5507.6592

Transverse Eccentricity

Tendon layout is symmetrical about the vertical centroidal axis.

INITIAL RELAXATION - Article 5.9.5.4.4b

Data has the time from stressing to transfer set to zero, indicating that initial relaxation is not required to be calculated here.

height mm	No of tendons	relax.		After relaxation			
		f_{pj}	f_{py} MPa	loss	area mm ²	force kN	moment kN.m
50.8	8	1396.19	1675.43	0.0	98.71	1102.542	56.009134
50.8	2	1393.86	1675.43	0.0	98.71	275.17634	13.978958
101.6	8	1396.19	1675.43	0.0	98.71	1102.542	112.01827
101.6	2	1393.86	1675.43	0.0	98.71	275.17634	27.957916
152.4	2	1396.19	1675.43	0.0	98.71	275.6355	42.006851
152.4	2	1393.86	1675.43	0.0	98.71	275.17634	41.936874
203.2	2	1393.86	1675.43	0.0	98.71	275.17634	55.915832
254.0	2	1393.86	1675.43	0.0	98.71	275.17634	69.89479
304.8	2	1393.86	1675.43	0.0	98.71	275.17634	83.873748
355.6	2	1393.86	1675.43	0.0	98.71	275.17634	97.852705
406.4	2	1393.86	1675.43	0.0	98.71	275.17634	111.83166
457.2	2	1393.86	1675.43	0.0	98.71	275.17634	125.81062
508.0	2	1393.86	1675.43	0.0	98.71	275.17634	139.78958
558.8	2	1393.86	1675.43	0.0	98.71	275.17634	153.76854
TOTAL	40					5507.6592	1132.6455

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Moment about the centroid of the precast beam:

$$M_r = 1132.6455 - (5507.6592 * 0.514946) \\ = -1703.501 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 5507.66 / 360.967 + (-1703.5 / 8.31E7) \\ &= 15.258068 - 20.49937 \\ &= -5.2413 \text{ MPa} \\ \text{bottom stress} &= 5507.66 / 360.967 - (-1703.5 / -1.014E8) \\ &= 15.258068 + 16.807569 \\ &= 32.0656 \text{ MPa} \end{aligned}$$

Self weight moment:

$$\begin{aligned} \text{c.s.a.} &= 3.61E5 \text{ mm}^2 \\ \text{density} &= 23.5631 \text{ kN/m}^3 \\ \text{self weight} &= 3.61E5 * 23.5631 \\ &= 8.50551 \text{ kN/m} \\ \text{beam length} &= 23.1136 \text{ m} \\ \text{distance} &= 13.8636 \text{ m} \\ M_{sw} &= 0.5 * 8.50551 * 13.8636 * (23.1136 - 13.8636) \\ &= 545.368 \text{ kN.m} \end{aligned}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 545.368 / 8.31E7 \\ &= 6.56278 \text{ MPa} \\ \text{bottom stress} &= 545.368 / -1.014E8 \\ &= -5.3809 \text{ MPa} \end{aligned}$$

ELASTIC SHORTENING LOSSES - Article 5.9.5.2.3a

concrete stresses at mid-span:

$$\begin{aligned} \text{stress at top of precast beam} &= 1.59381 \text{ MPa} \\ \text{stress at bottom of precast beam} &= 26.4615 \text{ MPa} \\ \text{depth of precast beam} &= 1143.0 \text{ mm} \end{aligned}$$

height mm	No of tendons	conc stress MPa	E_p/E_{ci}	tendon force kN	tendon moment kN.m
50.8	10	25.35626	6.084443	152.28851	7.7362564
101.6	10	24.25103	6.084443	145.65055	14.798096
152.4	4	23.1458	6.084443	55.605035	8.4742074
203.2	2	22.04057	6.084443	26.474925	5.3797048
254.0	2	20.93534	6.084443	25.147333	6.3874226
304.8	2	19.83011	6.084443	23.819741	7.2602569
355.6	2	18.72488	6.084443	22.492148	7.9982079
406.4	2	17.61965	6.084443	21.164556	8.6012755
457.2	2	16.51442	6.084443	19.836963	9.0694597
508.0	2	15.40919	6.084443	18.509371	9.4027605
558.8	2	14.30395	6.084443	17.181779	9.6011779
TOTAL	40			528.17091	94.708826

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Moment about the centroid of the precast beam:

$$M_{ed} = 94.708826 - (528.17091 * 0.514946) \\ = -177.2706 \text{ kN.m}$$

$$\text{hence top stress} = 1.5938 - 528.171 / 360.967 - (-177.271 / 8.31E7) \\ = 1.5938 - 1.463211 - (-2.133216) \\ = 2.26381 \text{ MPa}$$

$$\text{bottom stress} = 26.461 - 528.171 / 360.967 - (-177.271 / -1.014E8) \\ = 26.461 - 1.463211 - 1.7490381 \\ = 23.2492 \text{ MPa}$$

After a further 2 iterations of the above process, the top and bottom stresses are as follows:

$$\text{top stress} = 2.18992 \text{ MPa} \\ \text{bottom stress} = 23.579 \text{ MPa}$$

PERMISSIBLE STRESSES IN PRECAST BEAM

Compression

Article 5.9.4.1.1

$$\text{Permissible compression stress} = 0.6 * f'_{ci} \\ = 0.6 * 41.3685 \\ = 24.8211 \text{ MPa}$$

Tension

Article 5.9.4.1.2

$$\text{Permissible tension stress} = -0.248 * \sqrt{f'_{ci}} \\ = -0.248 * \sqrt{41.3685} \\ = -1.601 \text{ MPa}$$

but not greater than 1.38 MPa, therefore,
stress limit = -0.2 MPa

SERVICE LIMIT STATE - STRESS SUMMARY TABLE

	Concrete Stresses (MPa)					
	force kN	moment kN.m	Cast In Place		Precast	
			top	bottom	top	bottom
Prestress	5507.66	-1703.5			-5.2413	32.0656
Self Weight		545.368			6.56278	-5.3809
Prestress + Self Wt.					1.32148	26.6848
Elastic Def	-474.77	158.837			0.59611	-2.8825
TRANSFER	5032.88	-999.3			1.91759	23.8023

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SLS FLEXURE calculated using curvature of uncracked sections

The deflections are calculated from integration of the curvatures along the beam, using the parameters detailed below:

Elastic Modulus at Transfer,

$$E_T = 32.3777 \text{ kN/mm}^2$$

Precast section height = 1143.0 mm

	Precast		Curvature		Deflection	
	Stress (MPa)	E E_T	Strain ($\times 10^{-6}$)	($\times 10^{-6}$) (rad/m)	(mm) Here	Max.
At Transfer	$\begin{matrix} T \\ B \end{matrix}$	$\begin{matrix} 2.18992 \\ 23.579 \end{matrix}$	$\begin{matrix} E_T \\ \end{matrix}$	$\begin{matrix} 67.6368 \\ 728.25 \end{matrix}$	$\begin{matrix} -577.96 \\ \end{matrix}$	$\begin{matrix} 30.4682 \\ 30.4682 \end{matrix}$

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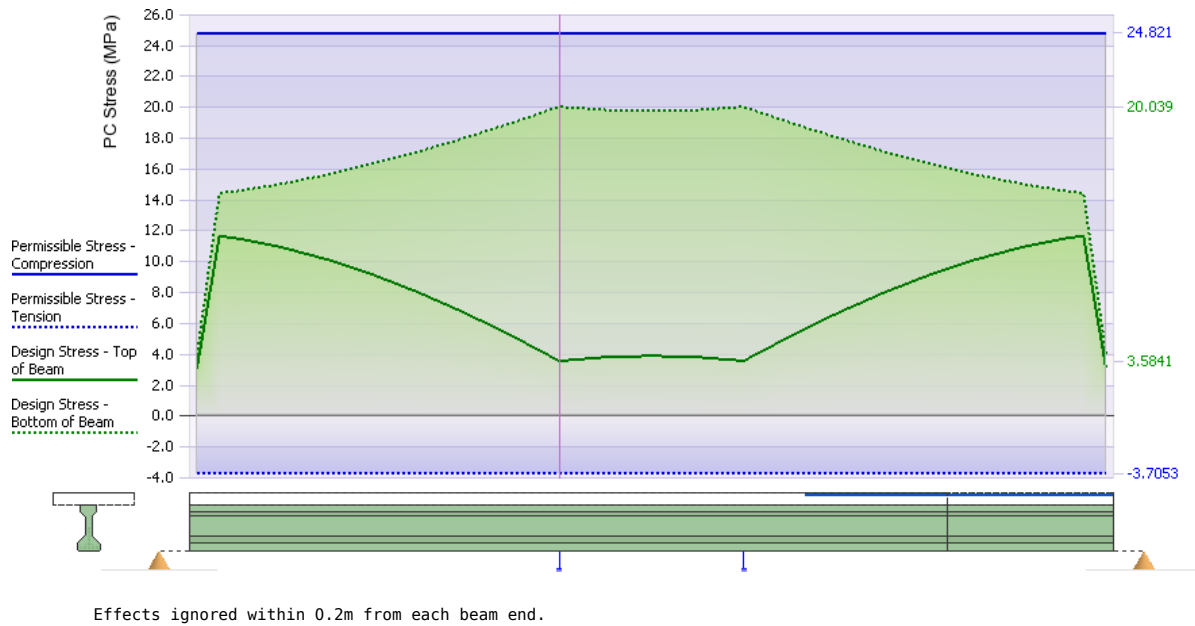
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Girder Design Calculations: Erection Stage



Performance ratio = $20.0 / 24.8 = 0.807$

Section details:

Ref 1 "Section 1"
at $0.400 \times \text{span} = 0.400 \times 23.1136 = 9.25$ m from left end of beam

Design Code:

AASHTO LRFD Bridge Design Specifications
Sixth Edition with 2013 Interim Revisions

Analysis:

Erection stage stresses
Limit State - Service I

ACTUAL STRESSES IN PRECAST BEAM

40 tendons are fully bonded at this section
0 tendons are fully debonded at this section
0 tendons are harped at this section

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INITIAL PRESTRESS

height mm	No of tendons	f_{pu} MPa	area mm ²	% of f_{pu}	initial force kN
50.8	8	1861.58	98.71	75.0	1102.542
50.8	2	1861.58	98.71	75.0	275.17634
101.6	8	1861.58	98.71	75.0	1102.542
101.6	2	1861.58	98.71	75.0	275.17634
152.4	2	1861.58	98.71	75.0	275.6355
152.4	2	1861.58	98.71	75.0	275.17634
203.2	2	1861.58	98.71	75.0	275.17634
254.0	2	1861.58	98.71	75.0	275.17634
304.8	2	1861.58	98.71	75.0	275.17634
355.6	2	1861.58	98.71	75.0	275.17634
406.4	2	1861.58	98.71	75.0	275.17634
457.2	2	1861.58	98.71	75.0	275.17634
508.0	2	1861.58	98.71	75.0	275.17634
558.8	2	1861.58	98.71	75.0	275.17634
TOTAL	40				5507.6592

Transverse Eccentricity

Tendon layout is symmetrical about the vertical centroidal axis.

INITIAL RELAXATION - Article 5.9.5.4.4b

Data has the time from stressing to transfer set to zero, indicating that initial relaxation is not required to be calculated here.

height mm	No of tendons	relax.			After relaxation		
		f_{pj}	f_{py} MPa	loss	area mm ²	force kN	moment kN.m
50.8	8	1396.19	1675.43	0.0	98.71	1102.542	56.009134
50.8	2	1393.86	1675.43	0.0	98.71	275.17634	13.978958
101.6	8	1396.19	1675.43	0.0	98.71	1102.542	112.01827
101.6	2	1393.86	1675.43	0.0	98.71	275.17634	27.957916
152.4	2	1396.19	1675.43	0.0	98.71	275.6355	42.006851
152.4	2	1393.86	1675.43	0.0	98.71	275.17634	41.936874
203.2	2	1393.86	1675.43	0.0	98.71	275.17634	55.915832
254.0	2	1393.86	1675.43	0.0	98.71	275.17634	69.89479
304.8	2	1393.86	1675.43	0.0	98.71	275.17634	83.873748
355.6	2	1393.86	1675.43	0.0	98.71	275.17634	97.852705
406.4	2	1393.86	1675.43	0.0	98.71	275.17634	111.83166
457.2	2	1393.86	1675.43	0.0	98.71	275.17634	125.81062
508.0	2	1393.86	1675.43	0.0	98.71	275.17634	139.78958
558.8	2	1393.86	1675.43	0.0	98.71	275.17634	153.76854
TOTAL	40					5507.6592	1132.6455

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Moment about the centroid of the precast beam:

$$M_r = 1132.6455 - (5507.6592 * 0.514946) \\ = -1703.501 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 5507.66/360.967 + (-1703.5/8.31E7) \\ &= 15.258068 - 20.49937 \\ &= -5.2413 \text{ MPa} \\ \text{bottom stress} &= 5507.66/360.967 + (-1703.5/-1.014E8) \\ &= 15.258068 + 16.807569 \\ &= 32.0656 \text{ MPa} \end{aligned}$$

Self weight moment:

$$\begin{aligned} \text{c.s.a.} &= 3.61E5 \text{ mm}^2 \\ \text{density} &= 23.5631 \text{ kN/m}^3 \\ \text{self weight} &= 3.61E5 * 23.5631 \\ &= 8.50551 \text{ kN/m} \\ \text{beam length} &= 23.1136 \text{ m} \\ \text{distance} &= 9.25 \text{ m} \\ M_{sw} &= 0.5 * 8.50551 * 9.25 * (23.1136 - 9.25) \\ &= 545.368 \text{ kN.m} \end{aligned}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 545.368/8.31E7 \\ &= 6.56278 \text{ MPa} \\ \text{bottom stress} &= 545.368/-1.014E8 \\ &= -5.3809 \text{ MPa} \end{aligned}$$

ELASTIC SHORTENING LOSSES - Article 5.9.5.2.3a

concrete stresses at mid-span:

$$\begin{aligned} \text{stress at top of precast beam} &= 1.59381 \text{ MPa} \\ \text{stress at bottom of precast beam} &= 26.4615 \text{ MPa} \\ \text{depth of precast beam} &= 1143.0 \text{ mm} \end{aligned}$$

height mm	No of tendons	conc stress MPa	E_p/E_{ci}	tendon force kN	tendon moment kN.m
50.8	10	25.35626	6.084443	152.28851	7.7362564
101.6	10	24.25103	6.084443	145.65055	14.798096
152.4	4	23.1458	6.084443	55.605035	8.4742074
203.2	2	22.04057	6.084443	26.474925	5.3797048
254.0	2	20.93534	6.084443	25.147333	6.3874226
304.8	2	19.83011	6.084443	23.819741	7.2602569
355.6	2	18.72488	6.084443	22.492148	7.9982079
406.4	2	17.61965	6.084443	21.164556	8.6012755
457.2	2	16.51442	6.084443	19.836963	9.0694597
508.0	2	15.40919	6.084443	18.509371	9.4027605
558.8	2	14.30395	6.084443	17.181779	9.6011779
TOTAL	40			528.17091	94.708826

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Moment about the centroid of the precast beam:

$$M_{ed} = 94.708826 - (528.17091 * 0.514946) \\ = -177.2706 \text{ kN.m}$$

$$\text{hence top stress} = 1.5938 - 528.171 / 360.967 - (-177.271 / 8.31E7) \\ = 1.5938 - 1.463211 - (-2.133216) \\ = 2.26381 \text{ MPa}$$

$$\text{bottom stress} = 26.461 - 528.171 / 360.967 - (-177.271 / -1.014E8) \\ = 26.461 - 1.463211 - 1.7490381 \\ = 23.2492 \text{ MPa}$$

After a further 2 iterations of the above process, the top and bottom stresses are as follows:

$$\text{top stress} = 2.18992 \text{ MPa} \\ \text{bottom stress} = 23.579 \text{ MPa}$$

REFINED ESTIMATES OF TIME-DEPENDENT LOSSES - Article 5.9.5.4

Elastic modulus of prestressing steel:	$E_p = 197.0 \text{ kN/mm}^2$
Total effective tendon area:	$A_{ps} = 3944.8 \text{ mm}^2$
Elastic modulus of concrete at transfer:	$E_{ci} = 32.378 \text{ kN/mm}^2$
Percentage relative humidity:	$H = 70.0 \%$
Humidity factor for creep:	$k_{hc} = 1.56 - 0.008H = 1.0$
Humidity factor for shrinkage:	$k_{hs} = 2.00 - 0.014H = 1.02$
Age at the end of curing:	$t_c = 3.0 \text{ day}$
Age at transfer:	$t_i = 4.0 \text{ day}$
Age at in-situ casting:	$t_d = 60.0 \text{ day}$
Final age:	$t_f = 120.0 \text{ day}$
Comp. strength of conc. at 1st loading:	$f'_{ci} = 41.37 \text{ MPa}$

$$\text{Factor for the effect of concrete strength: } k_f = \frac{35.0}{7 + f'_{ci}} = \frac{35.0}{7 + 41.4} = 0.7236$$

$$\text{Time factor for creep at final time: } k_{tdc, f, i} = \frac{t_f - t_i}{61 - 0.58 * f'_{ci} + t_f - t_i} \\ = \frac{120.0 - 4.0}{61 - 0.58 * 41.4 + 120.0 - 4.0} \\ = 0.7581$$

$$\text{Time fac. for shrinkage at final time: } k_{tds, f, i} = \frac{t_f - t_c}{61 - 0.58 * f'_{ci} + t_f - t_c} \\ = \frac{120.0 - 3.0}{61 - 0.58 * 41.4 + 120.0 - 3.0} \\ = 0.7597$$

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Losses: Time of Transfer to Time of Deck Placement - Article 5.9.5.4.2

Gross area of section: $A_g = 3.61E5 \text{ mm}^2$
Perimeter of section: $p = 3503.7 \text{ mm}$
Volume to surface ratio: $V/S = A_g/p = 103.02 \text{ mm}$
Factor for the effect of the volume: $k_s = 1.45 - 0.0051 \cdot (V/S) = 0.9245$
Creep coefficient at final time:

$$\begin{aligned}\psi_b(t_f, t_i) &= 1.9 \cdot k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, f, i} \cdot t_i^{-0.118} \\ &= 1.9 \cdot 0.9245 \cdot 1.0 \cdot 0.7236 \cdot 0.7581 \cdot 4.0^{-0.118} \\ &= 0.8182\end{aligned}$$

Inertia of the gross concrete section: $I_g = 5.22E10 \text{ mm}^4$

Eccentricity of prestressing force: $e_{pg} = -306.91 \text{ mm}$

Transformed section coefficient:

$$\begin{aligned}K_{id} &= \frac{1}{1 + \frac{E_p}{E_{ci}} \cdot \frac{A_{ps}}{A_g} \left[1 + \frac{A_g \cdot e_{pg}^2}{I_g} \right] \cdot [1 + 0.7 \cdot \psi_b(t_f, t_i)]} \\ &= \frac{1}{1 + \frac{197.0}{32.378} \cdot \frac{3944.8}{3.61E5} \left[1 + \frac{3.61E5 \cdot (-306.9)^2}{5.2E10} \right] \cdot (1 + 0.7 \cdot 0.8182)} \\ &= 0.85272\end{aligned}$$

Time factor for creep at deck placement:

$$\begin{aligned}k_{tdc, d, i} &= \frac{t_d - t_i}{61 - 0.58 \cdot f'_{ci} + t_d - t_i} \\ &= \frac{60.0 - 4.0}{61 - 0.58 \cdot 41.4 + 60.0 - 4.0} \\ &= 0.602\end{aligned}$$

Time factor for shrinkage at deck placement:

$$\begin{aligned}k_{tds, d, i} &= \frac{t_d - t_c}{61 - 0.58 \cdot f'_{ci} + t_d - t_c} \\ &= \frac{60.0 - 3.0}{61 - 0.58 \cdot 41.4 + 60.0 - 3.0} \\ &= 0.606\end{aligned}$$

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Shrinkage of Girder Concrete - Article 5.9.5.4.2a

Concrete shrinkage strain of girder:
$$\begin{aligned}\epsilon_{bid} &= k_s \cdot k_{hs} \cdot k_f \cdot k_{tds,d,i} \cdot 0.00048 \\ &= 1.0 \cdot 1.02 \cdot 0.71 \cdot 0.60 \cdot 0.00048 \\ &= 2.121\text{E-}4\end{aligned}$$

$$\begin{aligned}\text{Loss of prestress} &= \epsilon_{bid} \cdot E_p \cdot K_{id} \\ &= 2.12\text{E-}4 \cdot 197.0 \cdot 0.84963 \\ &= 35.495 \text{ MPa} \\ &= \Delta f_{pSR}\end{aligned}$$

$$\begin{aligned}\text{Total shrinkage loss of force} &= \Delta f_{pSR} \cdot A_{ps} \\ &= 35.4945 \cdot 3944.78 \\ &= 140.018 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding gain of moment} &= 140.018 \cdot 0.20803 \\ (\text{about } y = 0) &= 29.1282 \text{ kN.m}\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{sh} &= 29.1282 - (140.018 \cdot 0.51494) \\ &= -42.974 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 140.018/360967 + (-42.9735/8.31\text{E}7) \\ &= 0.3878972 + (-0.517129) \\ &= -0.129232 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 140.018/360967 + (-42.9735/-1.014\text{E}8) \\ &= 0.3878972 + 0.4239978 \\ &= 0.811895 \text{ MPa}\end{aligned}$$

Creep of Girder Concrete - Article 5.9.5.4.2b

Creep coefficient at deck placement:

$$\begin{aligned}\psi_b(t_d, t_i) &= 1.9 k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc,d,i} \cdot t_i^{-0.118} \\ &= 1.9 \cdot 1.0 \cdot 1.0 \cdot 0.7142 \cdot 0.6021 \cdot 4.0^{-0.118} \\ &= 0.6938\end{aligned}$$

Concrete stress at the center of gravity of prestressing tendons:

concrete stresses at transfer:

$$\begin{aligned}\text{at top of precast beam} &= 1.75172 \text{ MPa} \\ \text{at bottom of precast beam} &= 26.332 \text{ MPa} \\ \text{at center of gravity of prestress: } f_{cgp} &= 21.8583 \text{ MPa}\end{aligned}$$

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$$\begin{aligned}\text{Loss of prestress} &= \frac{E_p}{E_{ci}} \cdot f_{cgp} \cdot \Psi_b(t_d, t_i) \cdot K_{id} \\ &= \frac{197.0}{32.3777} \cdot 21.858 \cdot 0.6938 \cdot 0.8576 \\ &= 79.1425 \text{ MPa} \\ &= \Delta f_{pCR}\end{aligned}$$

$$\begin{aligned}\text{Total creep loss of force} &= \Delta f_{pCR} \cdot A_{ps} \\ &= 79.1425 \cdot 3944.78 \\ &= 312.2 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding loss of moment} &= 312.2 \cdot 0.20803 \\ &= 64.9475 \text{ kN.m} \\ &\quad (\text{about } y = 0)\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{Cr} &= 64.9475 - (312.2 \cdot 0.51494) \\ &= -95.819 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 312.2 / 3.61\text{E}5 + -95.819 / 8.31002\text{E}7 \\ &= 0.86489 + -1.153 \\ &= -0.2881 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 312.2 / 3.61\text{E}5 + -95.819 / -1.0135\text{E}8 \\ &= 0.86489 + 0.94539 \\ &= 1.81029 \text{ MPa}\end{aligned}$$

Relaxation of Prestressing Strands - Article 5.9.5.4.2c

$$\begin{array}{ll}\text{Stress in tendons after transfer:} & f_{pt} = 1275.83 \text{ MPa} \\ \text{Yield strength of prestressing steel:} & f_{py} = 1675.43 \text{ MPa} \\ \text{Time between tensioning and deck placement:} & t = t_s - t_i = 60.0 - 4.0 = 56.0 \text{ day} \\ \text{Factor for relaxation steel type:} & K'_L = 45.0 \text{ (low relaxation)}\end{array}$$

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$$\begin{aligned} \text{Loss of prestress} &= \frac{f_{pt}}{K'_L} \cdot \frac{\log(24t)}{\log(24t_i)} \cdot \left[\frac{f_{pt}}{f_{py}} - 0.55 \right] \cdot \left[1 - \frac{3(\Delta f_{pSR} + \Delta f_{pCR})}{f_{pt}} \right] \cdot K_{id} \\ &= \frac{1275.8}{45.0} \cdot \frac{\log(24 \cdot 56.0)}{\log(24 \cdot 4.0)} \cdot \left[\frac{1275.8}{1675.4} - 0.55 \right] \cdot \left[1 - \frac{3 \cdot (35.495 + 79.142)}{1275.8} \right] \cdot 0.85 \\ &= 5.87309 \text{ MPa} \\ &= \Delta f_{pR1} \end{aligned}$$

$$\begin{aligned} \text{Total relaxation loss of force} &= \Delta f_{pR1} \cdot A_{ps} \\ &= 5.8731 \cdot 3944.8 \\ &= 23.168069 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Corresponding loss of moment} &= 23.168 \cdot 0.2080 \\ &= 4.8196938 \text{ kN.m} \\ &\quad (\text{about } y = 0) \end{aligned}$$

$$\begin{aligned} \text{Moment about the centroid of the composite beam:} \\ M_{rx} &= 4.81969 - (23.1681 \cdot 0.5149) \\ &= -7.1106 \text{ kN.m} \end{aligned}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 23.1681/360967 + -7.11061/8.31E7 \\ &= 0.0641833 + -0.085567 \\ &= -0.0213834 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 23.1681/360967 + -7.11061/-1.014E8 \\ &= 0.0641833 + 0.0701567 \\ &= 0.13434 \text{ MPa} \end{aligned}$$

Erection of beam Loading

Bending moment from erection loadcase at current span location:

$$M_{\text{Applied}} = 647.3922 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 647.3922/8.31E7 \\ &= 7.7905 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 647.3922/-1.014E8 \\ &= -6.3875 \text{ MPa} \end{aligned}$$

Remove the dead load applied for transfer calculations

$$M_{sw} = -545.37 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= -545.37/8.31E7 \\ &= -6.5628 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= -545.37/-1.014E8 \\ &= 5.38086 \text{ MPa} \end{aligned}$$

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PERMISSIBLE STRESSES IN PRECAST BEAM

Compression

Article 5.9.4.2.1 for permanent loads

$$\begin{aligned}\text{Permissible compression stress} &= 0.45 * f'_c \\ &= 0.45 * 55.1581 \\ &= 24.8211 \text{ MPa}\end{aligned}$$

Tension

Article 5.9.4.2.2

$$\begin{aligned}\text{Permissible tension stress} &= -0.5 * \sqrt{f'_c} \\ &= -0.5 * \sqrt{55.1581} \\ &= -3.70451 \text{ MPa}\end{aligned}$$

SERVICE LIMIT STATE - STRESS SUMMARY TABLE

	force kN	moment kN.m	Concrete Stresses (MPa)			
			Cast In Place		Precast	
			top	bottom	top	bottom
Prestress	5507.66	-1703.5			-5.2413	32.0656
Self Weight		545.368			6.56278	-5.3809
Prestress + Self Wt.					1.32148	26.6848
Elastic Def	-474.77	158.837			0.59611	-2.8825
TRANSFER	5032.88	-999.3			1.91759	23.8023
Erection		102.024			1.22773	-1.0066
TOTAL PERMANENT					3.14532	22.7957

SLS FLEXURE

calculated using curvature of uncracked sections

The deflections are calculated from integration of the curvatures along the beam, using the parameters detailed below:

Elastic Modulus at Transfer,

$$E_T = 32.3777 \text{ kN/mm}^2$$

Intermediate Term Elastic Modulus,

$$E_I = 22.0714 \text{ kN/mm}^2$$

$$E_I = E_C / (\psi(t, t_i) + 1)$$

$$\text{where } \psi(t, t_i) = 0.69388 \text{ (Article 5.14.2.3.6)]}$$

Precast section height = 1143.0 mm

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		Precast		Curvature		Deflection	
		Stress (MPa)	E ($\times 10^{-6}$)	Strain ($\times 10^{-6}$)	($\times 10^{-6}$) (rad/m)	(mm) Here	Max.
At Transfer	T	1.92514	E_T	59.4591	-591.01	28.7861	30.3361
	B	23.7969		734.979			
At Erection	T	3.59084	E_I	162.692	-651.82	34.4532	36.1437
	B	20.0348		907.726			

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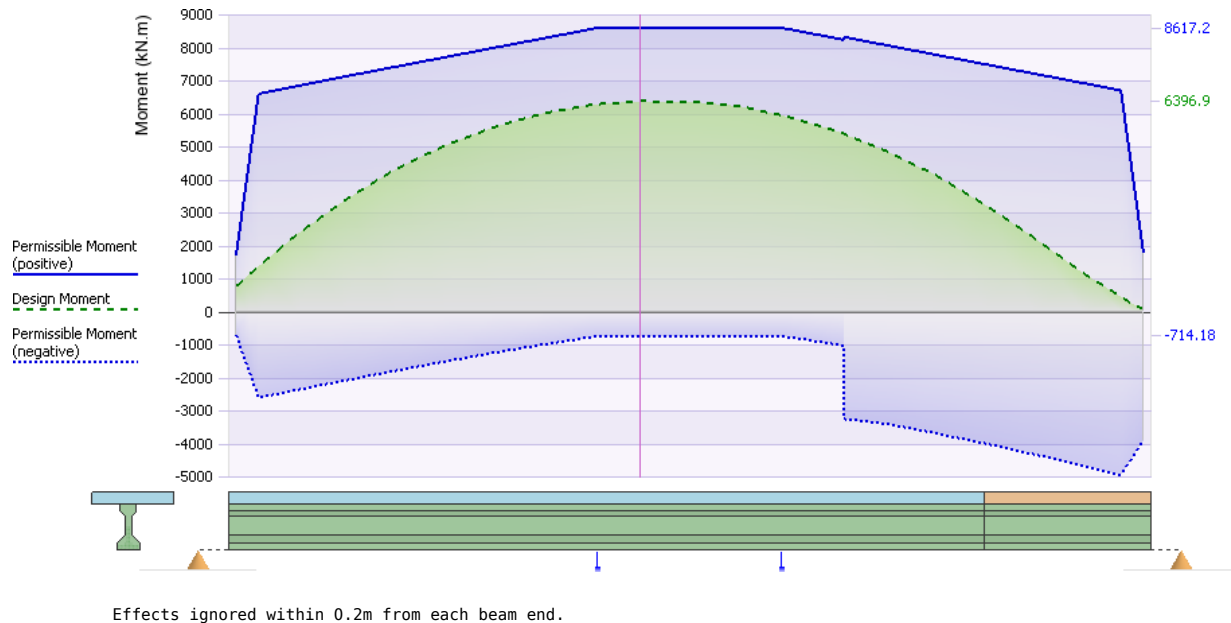
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Girder Design Calculations: Live Load Bending



Performance ratio = $6397 / 8617 = 0.742$

Section details:

Ref 1 "Section 1"
at $0.446 \times \text{span} = 0.446 \times 23.1136 = 10.3261$ m from left end of beam

Design Code:

AASHTO LRFD Bridge Design Specifications
Sixth Edition with 2013 Interim Revisions

Analysis:

Live Load Bending Moments
Transient Load BM 1 : [Max +ve]
Limit State - Strength I

Approximate Methods of Analysis are used - Article 4.6.2

Live Load Distribution Factor for +ve Moment = 0.94124 lanes/beam
Live Load Distribution Factor for -ve Moment = 0.94124 lanes/beam
Live Load Distribution Factor for Shear = 0.94124 lanes/beam
Live Load Distribution Factor for Fatigue = 0.78437 lanes/beam

Strength Limit State Stress/Strain summary for section with NEGATIVE moment

height of neutral axis = 228.627 mm
depth in compression = 228.627 mm

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Resistance Factor (ϕ) from Article 5.5.4.2.1

Type of force effect is:

Non-tension-controlled and non-compression-controlled

Compression-controlled strain limit in the extreme tension steel (5.7.2.1)

$$\epsilon_{cl} = -0.002$$

Tension-controlled strain limit in the extreme tension steel (5.7.2.1)

$$\epsilon_{tl} = -0.005$$

Net tensile strain in extreme steel at nominal resistance

$$\epsilon_t = -0.00433$$

prestressed section:

$$0.75 \leq \phi = 0.75 + 0.25 \left[\frac{\epsilon_{st} - \epsilon_{cl}}{\epsilon_{tl} - \epsilon_{cl}} \right] \leq 1.0 \quad (\text{Eq.: 5.5.4.2.1-1})$$

$$0.75 + 0.25 \left[\frac{-0.0043 - -0.002}{-0.005 - -0.002} \right]$$

$$= 0.94433$$

$$\phi = 0.94433$$

Location	strain	stress MPa	height mm
Precast beam - top	-0.011998	0.0	1143.0
- bottom	0.003	46.8843	0.0
C.I.P. stage 1 - top	-0.015935	0.0	1443.0
- bottom	-0.011998	0.0	1143.0
Tendon - top	-0.011013	-1674.9	558.8
- bottom	-0.004054	-798.58	50.8

Ultimate Strength capacity of section = -756.287×0.94433
= -714.185 kN.m

Strength Limit State Stress/Strain summary for section with POSITIVE moment

height of neutral axis = 1293.47 mm

depth in compression = 149.53 mm

Resistance Factor (ϕ) from Article 5.5.4.2.1

Type of force effect is:

Tension-controlled prestressed concrete:

$$\phi = 1.00$$

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Location	strain	stress MPa	height mm
Precast beam - <i>top</i>	-0.003019	0.0	1143.0
- <i>bottom</i>	-0.025951	0.0	0.0
C.I.P. stage 1 - <i>top</i>	0.003	29.3027	1443.0
- <i>bottom</i>	-0.003019	0.0	1143.0
Tendon - <i>top</i>	-0.02142	-1860.0	558.8
- <i>bottom</i>	-0.031319	-1860.0	50.8

Ultimate Strength capacity of section = 8617.17*1
= 8617.17 kN.m

SUMMARY OF APPLIED LOADINGS

	BENDING MOMENT kN.m	AXIAL kN
Erection loading before composite	= 832.97427	0.0
Erection loading to stage 1A	= 1266.3321	0.0
Erection loading to stage 1B	= 100.08702	0.0
Wearing Surface loading	= 229.84975	0.0
Differential Shrinkage / Creep is not adverse		
Transient loading	= 3967.636	0.0
TOTAL	6396.8791	0.0

Note:

The following effects are not considered (article 3.4.1) -
differential settlement
temperature gradient

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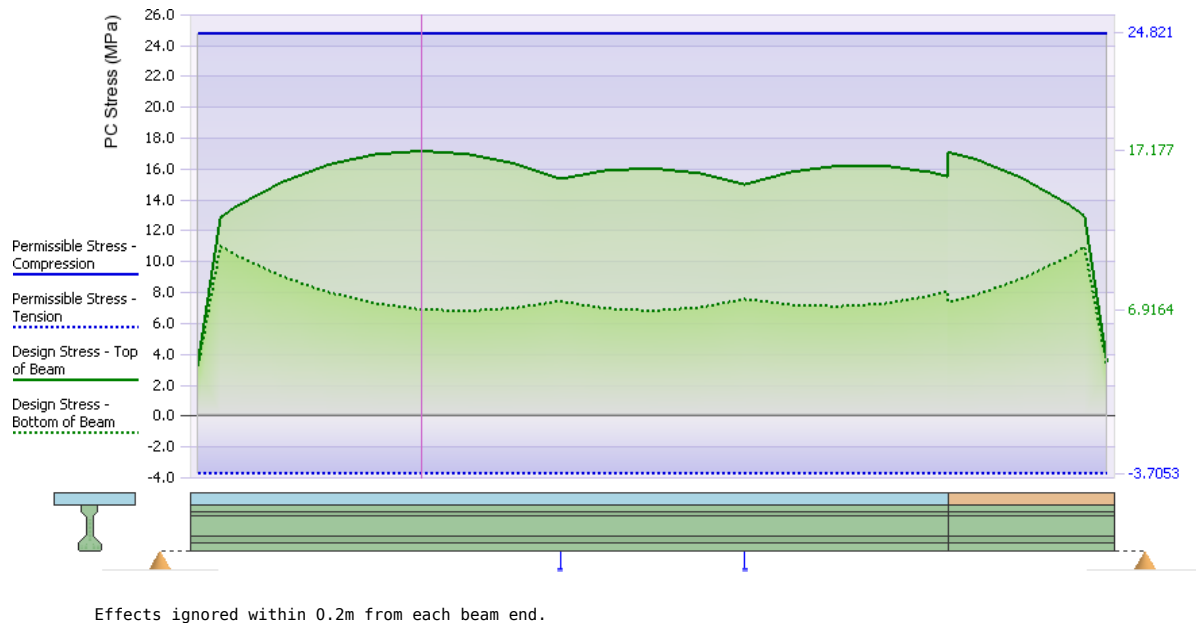
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Girder Design Calculations: Construction Stage



Performance ratio = $17.2 / 24.8 = 0.692$

Section details:

Ref 1 "Section 1"
at $0.25 \times \text{span} = 0.25 \times 23.1136 = 5.77841$ m from left end of beam

Design Code:

AASHTO LRFD Bridge Design Specifications
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Analysis:

Construction stage stresses
Limit State - Service I

ACTUAL STRESSES IN PRECAST BEAM

40 tendons are fully bonded at this section
0 tendons are fully debonded at this section
22 tendons are harped at this section

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INITIAL PRESTRESS

height mm	No of tendons	f_{pu} MPa	area mm ²	% of f_{pu}	initial force kN
50.8	8	1861.58	98.71	75.0	1102.542
251.1	2	1861.58	98.71	75.0	275.17634
101.6	8	1861.58	98.71	75.0	1102.542
301.9	2	1861.58	98.71	75.0	275.17634
152.4	2	1861.58	98.71	75.0	275.6355
352.7	2	1861.58	98.71	75.0	275.17634
403.5	2	1861.58	98.71	75.0	275.17634
454.3	2	1861.58	98.71	75.0	275.17634
505.1	2	1861.58	98.71	75.0	275.17634
555.9	2	1861.58	98.71	75.0	275.17634
606.7	2	1861.58	98.71	75.0	275.17634
657.5	2	1861.58	98.71	75.0	275.17634
708.3	2	1861.58	98.71	75.0	275.17634
759.1	2	1861.58	98.71	75.0	275.17634
TOTAL	40				5507.6592

Transverse Eccentricity

Tendon layout is symmetrical about the vertical centroidal axis.

INITIAL RELAXATION - Article 5.9.5.4.4b

Data has the time from stressing to transfer set to zero, indicating that initial relaxation is not required to be calculated here.

relax.					After relaxation		
height mm	No of tendons	f_{pj} MPa	f_{py} MPa	loss	area mm ²	force kN	moment kN.m
50.8	8	1396.19	1675.43	0.0	98.71	1102.542	56.009134
251.1	2	1393.86	1675.43	0.0	98.71	275.17634	69.096658
101.6	8	1396.19	1675.43	0.0	98.71	1102.542	112.01827
301.9	2	1393.86	1675.43	0.0	98.71	275.17634	83.075615
152.4	2	1396.19	1675.43	0.0	98.71	275.6355	42.006851
352.7	2	1393.86	1675.43	0.0	98.71	275.17634	97.054573
403.5	2	1393.86	1675.43	0.0	98.71	275.17634	111.03353
454.3	2	1393.86	1675.43	0.0	98.71	275.17634	125.01249
505.1	2	1393.86	1675.43	0.0	98.71	275.17634	138.99145
555.9	2	1393.86	1675.43	0.0	98.71	275.17634	152.97041
606.7	2	1393.86	1675.43	0.0	98.71	275.17634	166.94936
657.5	2	1393.86	1675.43	0.0	98.71	275.17634	180.92832
708.3	2	1393.86	1675.43	0.0	98.71	275.17634	194.90728
759.1	2	1393.86	1675.43	0.0	98.71	275.17634	208.88624
TOTAL	40					5507.6592	1738.9402

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Moment about the centroid of the precast beam:

$$M_r = 1738.9402 - (5507.6592 * 0.514946) \\ = -1097.206 \text{ kN.m}$$

Corresponding stresses:

$$\text{top stress} = 5507.66 / 360.967 + (-1097.21 / 8.31\text{E}7) \\ = 15.258068 + (-13.20342) \\ = 2.05465 \text{ MPa}$$

$$\text{bottom stress} = 5507.66 / 360.967 + (-1097.21 / -1.014\text{E}8) \\ = 15.258068 + 10.82557 \\ = 26.0836 \text{ MPa}$$

Self weight moment:

$$\text{c.s.a.} = 3.61\text{E}5 \text{ mm}^2$$

$$\text{density} = 23.5631 \text{ kN/m}^3$$

$$\text{self weight} = 3.61\text{E}5 * 23.5631 \\ = 8.50551 \text{ kN/m}$$

$$\text{beam length} = 23.1136 \text{ m}$$

$$\text{distance} = 5.77841 \text{ m}$$

$$M_{sw} = 0.5 * 8.50551 * 5.77841 * (23.1136 - 5.77841) \\ = 425.999 \text{ kN.m}$$

Corresponding stresses:

$$\text{top stress} = 425.999 / 8.31\text{E}7 \\ = 5.12633 \text{ MPa}$$

$$\text{bottom stress} = 425.999 / -1.014\text{E}8 \\ = -4.2031 \text{ MPa}$$

ELASTIC SHORTENING LOSSES - Article 5.9.5.2.3a

concrete stresses at mid-span:

$$\text{stress at top of precast beam} = 8.88976 \text{ MPa}$$

$$\text{stress at bottom of precast beam} = 20.4795 \text{ MPa}$$

$$\text{depth of precast beam} = 1143.0 \text{ mm}$$

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height mm	No of tendons	conc stress MPa	E_p/E_{ci}	tendon force kN	tendon moment kN.m
50.8	8	19.96439	6.084443	95.924161	4.8729474
251.1	2	17.9334	6.084443	21.541438	5.4090455
101.6	8	19.44929	6.084443	93.449231	9.4944419
301.9	2	17.4183	6.084443	20.922705	6.3165555
152.4	2	18.93419	6.084443	22.743576	3.4661209
352.7	2	16.9032	6.084443	20.303973	7.1612023
403.5	2	16.3881	6.084443	19.685241	7.9429859
454.3	2	15.87301	6.084443	19.066508	8.6619063
505.1	2	15.35791	6.084443	18.447776	9.3179635
555.9	2	14.84281	6.084443	17.829044	9.9111575
606.7	2	14.32771	6.084443	17.210311	10.441488
657.5	2	13.81261	6.084443	16.591579	10.908956
708.3	2	13.29751	6.084443	15.972847	11.31356
759.1	2	12.78241	6.084443	15.354114	11.655301
TOTAL	40			415.0425	116.87363

Moment about the centroid of the precast beam:

$$M_{ed} = 116.87363 - (415.0425 \times 0.514946) \\ = -96.85078 \text{ kN.m}$$

$$\text{hence top stress} = 8.8898 - 415.043/360.967 - -96.8508/8.31E7 \\ = 8.8898 - 1.1498073 - -1.16547 \\ = 8.90542 \text{ MPa}$$

$$\text{bottom stress} = 20.479 - 415.043/360.967 - -96.8508/-1.014E8 \\ = 20.479 - 1.1498073 - 0.9555770 \\ = 18.3741 \text{ MPa}$$

After a further 2 iterations of the above process, the top and bottom stresses are as follows:

$$\text{top stress} = 8.8897 \text{ MPa} \\ \text{bottom stress} = 18.5542 \text{ MPa}$$

REFINED ESTIMATES OF TIME-DEPENDENT LOSSES - Article 5.9.5.4

Elastic modulus of prestressing steel:	$E_p = 197.0 \text{ kN/mm}^2$
Total effective tendon area:	$A_{ps} = 3944.8 \text{ mm}^2$
Elastic modulus of concrete at transfer:	$E_{ci} = 32.378 \text{ kN/mm}^2$
Percentage relative humidity:	$H = 70.0 \%$
Humidity factor for creep:	$k_{hc} = 1.56 - 0.008H = 1.0$
Humidity factor for shrinkage:	$k_{hs} = 2.00 - 0.014H = 1.02$
Age at the end of curing:	$t_c = 3.0 \text{ day}$
Age at transfer:	$t_i = 4.0 \text{ day}$
Age at in-situ casting:	$t_d = 60.0 \text{ day}$
Final age:	$t_f = 120.0 \text{ day}$
Comp. strength of conc. at 1st loading:	$f'_{ci} = 41.37 \text{ MPa}$

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$$\text{Factor for the effect of concrete strength: } k_f = \frac{35.0}{7+f'_{ci}} = \frac{35.0}{7+41.4} = 0.7236$$

$$\begin{aligned} \text{Time factor for creep at final time: } k_{tdc,f,i} &= \frac{t_f - t_i}{61 - 0.58 \cdot f'_{ci} + t_f - t_i} \\ &= \frac{120.0 - 4.0}{61 - 0.58 \cdot 41.4 + 120.0 - 4.0} \\ &= 0.7581 \end{aligned}$$

$$\begin{aligned} \text{Time fac. for shrinkage at final time: } k_{tds,f,i} &= \frac{t_f - t_c}{61 - 0.58 \cdot f'_{ci} + t_f - t_c} \\ &= \frac{120.0 - 3.0}{61 - 0.58 \cdot 41.4 + 120.0 - 3.0} \\ &= 0.7597 \end{aligned}$$

Losses: Time of Transfer to Time of Deck Placement - Article 5.9.5.4.2

$$\begin{aligned} \text{Gross area of section: } A_g &= 3.61\text{E}5 \text{ mm}^2 \\ \text{Perimeter of section: } p &= 3503.7 \text{ mm} \\ \text{Volume to surface ratio: } V/S &= A_g/p = 103.02 \text{ mm} \\ \text{Factor for the effect of the volume: } k_s &= 1.45 - 0.0051 \cdot (V/S) = 0.9245 \\ \text{Creep coefficient at final time: } \psi_b(t_f, t_i) &= 1.9 \cdot k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc,f,i} \cdot t_i^{-0.118} \\ &= 1.9 \cdot 0.9245 \cdot 1.0 \cdot 0.7236 \cdot 0.7581 \cdot 4.0^{-0.118} \\ &= 0.8182 \\ \text{Inertia of the gross concrete section: } I_g &= 5.22\text{E}10 \text{ mm}^4 \\ \text{Eccentricity of prestressing force: } e_{pg} &= -196.91 \text{ mm} \end{aligned}$$

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Transformed section coefficient:

$$K_{id} = \frac{1}{1 + \frac{E_p}{E_{ci}} \cdot \frac{A_{ps}}{A_g} \left[1 + \frac{A_g \cdot e_{pg}^2}{I_g} \right] \cdot [1 + 0.7 \cdot \psi_b(t_f, t_i)]}$$

$$= \frac{1}{1 + \frac{197.0}{32.378} \cdot \frac{3944.8}{3.61E5} \left[1 + \frac{3.61E5 \cdot 196.9^2}{5.2E10} \right] \cdot (1 + 0.7 \cdot 0.8182)}$$

$$= 0.88290$$

Time factor for creep at deck placement:

$$k_{tdc,d,i} = \frac{t_d - t_i}{61 - 0.58 \cdot f'_{ci} + t_d - t_i}$$

$$= \frac{60.0 - 4.0}{61 - 0.58 \cdot 41.4 + 60.0 - 4.0}$$

$$= 0.602$$

Time factor for shrinkage at deck placement:

$$k_{tds,d,i} = \frac{t_d - t_c}{61 - 0.58 \cdot f'_{ci} + t_d - t_c}$$

$$= \frac{60.0 - 3.0}{61 - 0.58 \cdot 41.4 + 60.0 - 3.0}$$

$$= 0.606$$

Shrinkage of Girder Concrete - Article 5.9.5.4.2a

Concrete shrinkage strain of girder: $\epsilon_{bid} = k_s \cdot k_{hs} \cdot k_f \cdot k_{tds,d,i} \cdot 0.00048$

$$= 1.0 \cdot 1.02 \cdot 0.71 \cdot 0.60 \cdot 0.00048$$

$$= 2.121E-4$$

Loss of prestress = $\epsilon_{bid} \cdot E_p \cdot K_{id}$

$$= 2.12E-4 \cdot 197.0 \cdot 0.88036$$

$$= 36.778 \text{ MPa}$$

$$= \Delta f_{psR}$$

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$$\begin{aligned}\text{Total shrinkage loss of force} &= \Delta f_{pSR} \cdot A_{ps} \\ &= 36.7781 \cdot 3944.78 \\ &= 145.081 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding gain of moment} &= 145.081 \cdot 0.31804 \\ (\text{about } y = 0) &= 46.1417 \text{ kN.m}\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{sh} &= 46.1417 - (145.081 \cdot 0.51494) \\ &= -28.567 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 145.081/360967 + (-28.5674/8.31E7) \\ &= 0.4019245 + (-0.343770) \\ &= 0.0581537 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 145.081/360967 + (-28.5674/-1.014E8) \\ &= 0.4019245 + 0.2818600 \\ &= 0.683785 \text{ MPa}\end{aligned}$$

Creep of Girder Concrete - Article 5.9.5.4.2b

Creep coefficient at deck placement:

$$\begin{aligned}\psi_b(t_d, t_i) &= 1.9k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, d, i} \cdot t_i^{-0.118} \\ &= 1.9 \cdot 1.0 \cdot 1.0 \cdot 0.7142 \cdot 0.6021 \cdot 4.0^{-0.118} \\ &= 0.6938\end{aligned}$$

Concrete stress at the center of gravity of prestressing tendons:

concrete stresses at transfer:

$$\begin{aligned}\text{at top of precast beam} &= 9.04277 \text{ MPa} \\ \text{at bottom of precast beam} &= 20.354 \text{ MPa} \\ \text{at center of gravity of prestress: } f_{cgp} &= 17.2067 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{Loss of prestress} &= \frac{E_p}{E_{ci}} \cdot f_{cgp} \cdot \psi_b(t_d, t_i) \cdot K_{id} \\ &= \frac{197.0}{32.3777} \cdot 17.207 \cdot 0.6938 \cdot 0.8821 \\ &= 64.0856 \text{ MPa} \\ &= \Delta f_{PCR}\end{aligned}$$

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$$\begin{aligned}\text{Total creep loss of force} &= \Delta f_{pCR} \cdot A_{ps} \\ &= 64.0856 \cdot 3944.78 \\ &= 252.804 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding loss of moment} &= 252.804 \cdot 0.31804 \\ &= 80.4017 \text{ kN.m} \\ &\quad (\text{about } y = 0)\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{Cr} &= 80.4017 - (252.804 \cdot 0.51494) \\ &= -49.779 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 252.804 / 3.61\text{E}5 - 49.779 / 8.31002\text{E}7 \\ &= 0.70035 - 0.5990 \\ &= 0.10133 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 252.804 / 3.61\text{E}5 - 49.779 / -1.0135\text{E}8 \\ &= 0.70035 + 0.49114 \\ &= 1.19149 \text{ MPa}\end{aligned}$$

Relaxation of Prestressing Strands - Article 5.9.5.4.2c

$$\begin{aligned}\text{Stress in tendons after transfer:} & f_{pt} = 1299.38 \text{ MPa} \\ \text{Yield strength of prestressing steel:} & f_{py} = 1675.43 \text{ MPa} \\ \text{Time between tensioning and deck placement:} & t = t_s - t_i = 60.0 - 4.0 = 56.0 \text{ day} \\ \text{Factor for relaxation steel type:} & K'_L = 45.0 \text{ (low relaxation)}\end{aligned}$$

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$$\begin{aligned}\text{Loss of prestress} &= \frac{f_{pt}}{K'_L} \cdot \frac{\log(24t)}{\log(24t_i)} \cdot \left[\frac{f_{pt}}{f_{py}} - 0.55 \right] \cdot \left[1 - \frac{3(\Delta f_{pSR} + \Delta f_{pCR})}{f_{pt}} \right] \cdot K_{id} \\ &= \frac{1299.4}{45.0} \cdot \frac{\log(24 \cdot 56.0)}{\log(24 \cdot 4.0)} \cdot \left[\frac{1299.4}{1675.4} - 0.55 \right] \cdot \left[1 - \frac{3 \cdot (36.778 + 64.086)}{1299.4} \right] \cdot 0.88 \\ &= 6.94164 \text{ MPa} \\ &= \Delta f_{pR1}\end{aligned}$$

$$\begin{aligned}\text{Total relaxation loss of force} &= \Delta f_{pR1} \cdot A_{ps} \\ &= 6.9416 \cdot 3944.8 \\ &= 27.383265 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding loss of moment} &= 27.383 \cdot 0.3180 \\ &= 8.7089704 \text{ kN.m} \\ &\quad (\text{about } y = 0)\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{rx} &= 8.70897 - (27.3833 \cdot 0.5149) \\ &= -5.3919 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 27.3833/360967 + -5.39193/8.31E7 \\ &= 0.0758609 + -0.064885 \\ &= 0.0109762 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 27.3833/360967 + -5.39193/-1.014E8 \\ &= 0.0758609 + 0.0531994 \\ &= 0.12906 \text{ MPa}\end{aligned}$$

Erection of beam Loading

Bending moment from erection loadcase at current span location:

$$M_{\text{Applied}} = 505.89017 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 505.89017/8.31E7 \\ &= 6.08772 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 505.89017/-1.014E8 \\ &= -4.9914 \text{ MPa}\end{aligned}$$

Remove the dead load applied for transfer calculations

$$M_{sw} = -426.0 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= -426.0/8.31E7 \\ &= -5.1263 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= -426.0/-1.014E8 \\ &= 4.20311 \text{ MPa}\end{aligned}$$

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Construction stage 1A Loading

$$M_{\text{Applied}} = 783.32263 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 783.32263/8.31\text{E}7 \\ &= 9.42625 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 783.32263/-1.014\text{E}8 \\ &= -7.7286 \text{ MPa} \end{aligned}$$

Construction stage 1B Loading

$$M_{\text{Applied}} = 44.810547 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 44.810547/8.31\text{E}7 \\ &= 0.53923 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 44.810547/-1.014\text{E}8 \\ &= -0.4421 \text{ MPa} \end{aligned}$$

Losses: Time of Deck Placement to Final Time - Article 5.9.5.4.3

$$\text{Gross composite section area: } A_c = 9.72\text{E}5 \text{ mm}^2$$

$$\text{Perimeter of section: } p = 7365.6 \text{ mm}$$

$$\text{Volume to surface ratio: } V/S = A_c/p = 131.99 \text{ mm}$$

$$\text{Factor for the effect of the volume: } k_s = 1.45 - 0.0051 \cdot (V/S) = 0.7768$$

Creep coefficient at final time:

$$\begin{aligned} \psi_b(t_f, t_i) &= 1.9 \cdot k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, f, i} \cdot t_i^{-0.118} \\ &= 1.9 \cdot 0.776 \cdot 1.0 \cdot 0.723 \cdot 0.758 \cdot 4.0^{-0.118} \\ &= 0.6875 \end{aligned}$$

$$\text{Inertia of the net concrete section: } I_c = 1.94\text{E}8 \text{ mm}^4$$

$$\text{Eccentricity of prestressing force: } e_{pc} = 0.6860 \text{ mm}$$

Transformed section coefficient:

$$\begin{aligned} K_{df} &= \frac{1}{1 + \frac{E_p}{E_{ci}} \cdot \frac{A_{ps}}{A_c} \left[1 + \frac{A_c \cdot e_{pc}^2}{I_c} \right] \cdot [1 + 0.7 \cdot \psi_b(t_f, t_i)]} \\ &= \frac{1}{1 + \frac{197.0}{32.378} \cdot \frac{3944.8}{9.72\text{E}5} \left[1 + \frac{9.72\text{E}5 \cdot 686.07^2}{1.9\text{E}11} \right] \cdot (1 + 0.7 \cdot 0.6875)} \\ &= 0.89066 \end{aligned}$$

Shrinkage of Girder Concrete - Article 5.9.5.4.3a

$$\begin{aligned} \text{Concrete shrinkage strain of girder: } \epsilon_{bdf} &= k_s \cdot k_{hs} \cdot k_f \cdot k_{tds, f, i} \cdot 0.00048 \\ &= 1.0 \cdot 1.02 \cdot 0.71 \cdot 0.76 \cdot 0.00048 \\ &= 2.657\text{E}-4 \end{aligned}$$

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$$\begin{aligned}\text{Loss of prestress} &= \epsilon_{bdf} \cdot E_p \cdot K_{df} \\ &= 2.66\text{E-}4 \cdot 1.97\text{E}8 \cdot 0.88217 \\ &= 46.1743 \text{ MPa} \\ &= \Delta f_{pSD}\end{aligned}$$

$$\begin{aligned}\text{Total shrinkage loss of force} &= \Delta f_{pSD} \cdot A_{ps} \\ &= 46.1743 \cdot 3944.78 \\ &= 182.147 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding gain of moment} &= 182.147 \cdot 0.31804 \\ (\text{about } y = 0) &= 57.9302 \text{ kN.m}\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{sh} &= 57.9302 - (182.147 \cdot 0.9603) \\ &= -116.99 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 182.147 / 844161 + (-116.986 / 9.901\text{E}8) \\ &= 0.2157735 + (-0.118153) \\ &= 0.0976197 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 182.147 / 844161 + (-116.986 / -1.884\text{E}8) \\ &= 0.2157735 + 0.6210367 \\ &= 0.83681 \text{ MPa}\end{aligned}$$

Creep of Girder Concrete - Article 5.9.5.4.2b

Creep coefficient at deck placement:

$$\begin{aligned}\psi_b(t_d, t_i) &= 1.9k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, d, i} \cdot t_i^{-0.118} \\ &= 1.9 \cdot 1.0 \cdot 1.0 \cdot 0.7142 \cdot 0.6021 \cdot 4.0^{-0.118} \\ &= 0.6938\end{aligned}$$

Creep coefficient at final time:

$$\begin{aligned}\psi_b(t_f, t_d) &= 1.9k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, f, i} \cdot t_d^{-0.118} \\ &= 1.9 \cdot 1.0 \cdot 1.0 \cdot 0.7142 \cdot 0.6185 \cdot 60.0^{-0.118} \\ &= 0.5178\end{aligned}$$

Concrete stress at the center of gravity of prestressing tendons:

concrete stresses at transfer:

$$\begin{aligned}\text{at top of precast beam} &= 9.04277 \text{ MPa} \\ \text{at bottom of precast beam} &= 20.354 \text{ MPa} \\ \text{at center of gravity of prestress: } f_{cgp} &= 17.2067 \text{ MPa}\end{aligned}$$

Change in concrete stress at centroid of prestressing strands:

concrete stress change after permanent loads:

$$\begin{aligned}\text{at top of precast beam} &= 12.1466 \text{ MPa} \\ \text{at bottom of precast beam} &= 11.3949 \text{ MPa} \\ \Delta f_{cd} &= 11.604 \text{ MPa}\end{aligned}$$

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$$\begin{aligned}
 \text{Loss of prestress} &= \frac{E_p}{E_{ci}} * f_{cgp} * \left[\psi_b(t_f, t_i) - \psi_b(t_d, t_i) \right] * K_{df} \\
 &+ \frac{E_p}{E_c} * \Delta f_{cd} * \psi_b(t_f, t_d) * K_{df} \\
 &= \frac{197.0}{32.3777} * 17.2067 * (0.87367 - 0.69388) * 0.88036 \\
 &+ \frac{197.0}{18.6932} * 11.604 * 0.51782 * 0.88036 \\
 &= 72.3196 \text{ MPa} \\
 &= \Delta f_{pCD}
 \end{aligned}$$

$$\begin{aligned}
 \text{Total creep loss of force} &= \Delta f_{pCD} * A_{ps} \\
 &= 72.3196 * 3944.78 \\
 &= 285.285 \text{ kN}
 \end{aligned}$$

$$\begin{aligned}
 \text{Corresponding loss of moment} &= 285.285 * 0.31804 \\
 &= 90.7321 \text{ kN.m} \\
 &\quad (\text{about } y = 0)
 \end{aligned}$$

$$\begin{aligned}
 \text{Moment about the centroid of the composite beam:} \\
 M_{cr} &= 90.7321 - (285.285 * 0.9603) \\
 &= -183.23 \text{ kN.m}
 \end{aligned}$$

Corresponding stresses:

$$\begin{aligned}
 \text{top stress} &= 285.285 / 8.442\text{E}5 + -183.23 / 9.90117\text{E}8 \\
 &= 0.33795 + -0.1850 \\
 &= 0.15289 \text{ MPa}
 \end{aligned}$$

$$\begin{aligned}
 \text{bottom stress} &= 285.285 / 8.442\text{E}5 + -183.23 / -1.8837\text{E}8 \\
 &= 0.33795 + 0.97268 \\
 &= 1.31064 \text{ MPa}
 \end{aligned}$$

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Relaxation of Prestressing Strands - Article 5.9.5.4.3c

$$\begin{aligned}\text{Loss of prestress} &= \Delta f_{pR1} \\ &= 6.94164 \text{ MPa} \\ &= \Delta f_{pR2}\end{aligned}$$

$$\begin{aligned}\text{Total relaxation loss of force} &= \Delta f_{pR2} \cdot A_{ps} \\ &= 6.9416 \cdot 3944.8 \\ &= 27.383265 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding loss of moment} &= 27.383 \cdot 0.3180 \\ &= 8.7089704 \text{ kN.m} \\ &\quad (\text{about } y = 0)\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{rx} &= 8.70897 - (27.3833 \cdot 0.9603) \\ &= -17.587 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 27.3833/844161 + (-17.5872/9.901E8) \\ &= 0.0324385 + (-0.017763) \\ &= 0.0146757 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 27.3833/844161 + (-17.5872/-1.884E8) \\ &= 0.0324385 + 0.093364 \\ &= 0.125802 \text{ MPa}\end{aligned}$$

Shrinkage of Deck Concrete - Article 5.9.5.4.3d

$$\begin{aligned}\text{Concrete shrinkage strain of girder:} \quad \epsilon_{ddf} &= k_s \cdot k_{hs} \cdot k_f \cdot k_{tds, f, i} \cdot 0.00048 \\ &= 1.025 \cdot 1.02 \cdot 0.71 \cdot 0.76 \cdot 0.00048 \\ &= 2.724E-4\end{aligned}$$

Creep coefficient at final time:

$$\begin{aligned}\psi_b(t_f, t_d) &= 1.9 k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, f, i} \cdot t_d^{-0.118} \\ &= 1.9 \cdot 1.0253 \cdot 1.0 \cdot 0.7142 \cdot 0.6185 \cdot 60.0^{-0.118} \\ &= 0.5309\end{aligned}$$

Change in concrete stress at centroid of prestressing strands:

$$\begin{aligned}\text{Area of deck concrete:} \quad A_d &= 6.112E5 \text{ mm}^2 \\ \text{Perimeter of section:} \quad p &= 7365.55 \text{ mm} \\ \text{Volume to surface ratio:} \quad V/S &= A_d/p = 82.98 \text{ mm} \\ \text{Factor for the effect of the volume:} \quad k_s &= 1.45 - 0.0051 \cdot (V/S) = 1.4333 \\ \text{Modulus of elasticity of deck concrete:} \quad E_{cd} &= 29.5566 \text{ mm}^2 \\ \text{Eccentricity of the deck:} \quad e_d &= 288.894 \text{ mm}^3\end{aligned}$$

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$$\Delta f_{cdf} = \frac{\epsilon_{ddf} \cdot A_d \cdot E_{cd}}{[1 + 0.7\psi_b(t_f, t_d)]} \left[\frac{1}{A_c} \frac{e_{pc} \cdot e_d}{I_c} \right]$$

$$= \frac{2.7E-4 \cdot 6.11E5 \cdot 29.557 \cdot 1000}{[1 + 0.7 \cdot 0.5309]} \left[\frac{1}{8.44E5} \frac{642.261 \cdot 288.894}{1.8E11} \right]$$

$$= 0.57008 \text{ MPa}$$

$$\text{Loss of prestress} = \frac{E_p}{E_c} \cdot \Delta f_{cdf} \cdot K_{df} \cdot [1 + 0.7\psi_b(t_f, t_d)]$$

$$= \frac{197.0}{18.6932} \cdot 0.57008 \cdot 0.88217 \cdot (1 + 0.7 \cdot 0.53092)$$

$$= 7.26975 \text{ MPa}$$

$$= \Delta f_{pss}$$

$$\begin{aligned} \text{Total shrinkage gain of force} &= \Delta f_{pss} \cdot A_{ps} \\ &= 7.26975 \cdot 3944.78 \\ &= 28.6776 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Corresponding gain of moment} &= 28.6776 \cdot 0.31804 \\ (\text{about } y = 0) &= 9.12061 \text{ kN.m} \end{aligned}$$

$$\begin{aligned} \text{Moment about the centroid of the composite beam:} \\ M_{sh} &= 9.12061 - (28.6776 \cdot 0.9603) \\ &= -18.418 \text{ kN.m} \end{aligned}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 28.6776/844161 + (-18.4185/9.901E8) \\ &= 0.0339717 + (-0.018602) \\ &= 0.0153694 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 28.6776/844161 + (-18.4185/-1.884E8) \\ &= 0.0339717 + 0.097777 \\ &= 0.131749 \text{ MPa} \end{aligned}$$

PERMISSIBLE STRESSES IN PRECAST BEAM

Compression

Article 5.9.4.2.1 for permanent loads

$$\begin{aligned} \text{Permissible compression stress} &= 0.45 \cdot f'_c \\ &= 0.45 \cdot 55.1581 \\ &= 24.8211 \text{ MPa} \end{aligned}$$

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Tension

Article 5.9.4.2.2

$$\begin{aligned}\text{Permissible tension stress} &= -0.5 * \sqrt{f'_c} \\ &= -0.5 * \sqrt{55.1581} \\ &= -3.70451 \text{ MPa}\end{aligned}$$

PERMISSIBLE STRESSES FOR CAST IN PLACE CONCRETE

Compression

Article 5.9.4.2

$$\begin{aligned}\text{char. strength of c.i.p. concrete} &= 34.4738 \text{ MPa} \\ \text{stress limitation factor} &= 0.6 \\ \text{permissible compression stress} &= 0.6 * f_{cu} \\ &= 0.6 * 34.4738 \\ &= 20.6843 \text{ MPa}\end{aligned}$$

Tension

Article 5.7.3.4

Flexural tensile stresses may need to be limited by cracking considerations in accordance with article 5.7.3.4.

SERVICE LIMIT STATE - STRESS SUMMARY TABLE

	Concrete Stresses (MPa)					
	force kN	moment kN.m	Cast In Place top bottom		Precast top bottom	
Prestress	5507.66	-1097.2			2.05465	26.0836
Self Weight		425.999			5.12633	-4.2031
Prestress + Self Wt.					7.18098	21.8805
Elastic Def	-381.88	87.9095			-6.1E-5	-1.9253
TRANSFER	5125.78	-583.3			7.18092	19.9552

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Erection	79.8913			0.96138	-0.7882
C.I.P. Stage 1A	783.323			9.42625	-7.7286
C.I.P. Stage 1B	44.8105	0.09453	0.03578	0.04526	-0.2378

Time-Dependent Losses

Time of Transfer to Time of Deck Placement

Shrinkage	-145.08	28.5674		-0.0582	-0.6837
Creep	-252.8	49.7786		-0.1013	-1.1915
Relaxation	-27.383	5.39193		-0.011	-0.1290

Time of Deck Placement to Final Time

Shrinkage					
Girder	-182.15	116.986	0.07621	-0.0772	-0.0976
Deck	-1.4094	0.90517	5.9E-4	-6.0E-4	-7.6E-4
Creep	-285.29	183.227	0.11935	-0.1208	-0.1529
Relaxation	-27.383	17.5872	0.01146	-0.0116	-0.0147

TOTAL PERMANENT		0.20760	-0.2102	17.1774	6.9164
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SLS FLEXURE

calculated using curvature of uncracked sections

The deflections are calculated from integration of the curvatures along the beam, using the parameters detailed below:

Elastic Modulus at Transfer,	$E_T = 32.3777 \text{ kN/mm}^2$
Intermediate Term Elastic Modulus,	$E_I = 22.0714 \text{ kN/mm}^2$
$E_I = E_C / (\psi(t, t_i) + 1)$	
where $\psi(t, t_i) = 0.69388$ (Article 5.14.2.3.6)]	
Short Term Elastic Modulus,	$E_S = 37.3865 \text{ kN/mm}^2$

Precast section height = 1143.0 mm

		Precast		Curvature		Deflection
		Stress (MPa)	E ($\times 10^{-6}$)	Strain ($\times 10^{-6}$)	($\times 10^{-6}$) (rad/m)	(mm) Here Max.
At Transfer	^T	8.6673	E_T	267.694	-275.14	17.427
	^B	18.8497		582.183		30.3361
At Erection	^T	9.14173	E_I	414.188	-286.39	22.0707
	^B	16.3666		741.527		36.1437
From in situ 1A	^T	8.06855	E_S	215.814	343.624	-20.148
						-31.482

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B -6.6155 -176.95

From in situ 1B ^T 0.03621 *E_S* 0.96841 5.30056 -0.6323 -1.2659

B -0.1903 -5.0901

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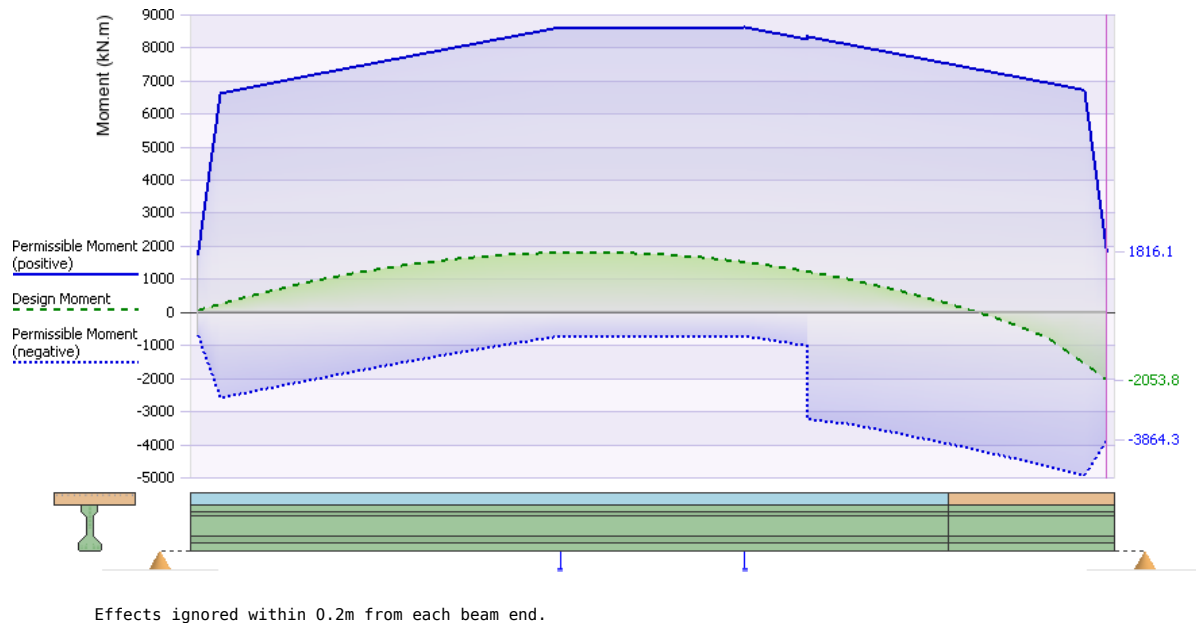
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Girder Design Calculations: Live Load Bending



Performance ratio = $-2054 / -3864 = 0.531$

Section details:

Ref 2 "Section 2"
at $0.991 \times \text{span} = 0.991 \times 23.1136 = 22.9136$ m from left end of beam

Design Code:

AASHTO LRFD Bridge Design Specifications
Sixth Edition with 2013 Interim Revisions

Analysis:

Live Load Bending Moments
Transient Load BM 2 : [Max -ve]
Limit State - Strength I

Approximate Methods of Analysis are used - Article 4.6.2

Live Load Distribution Factor for +ve Moment = 0.94124 lanes/beam
Live Load Distribution Factor for -ve Moment = 0.94124 lanes/beam
Live Load Distribution Factor for Shear = 0.94124 lanes/beam
Live Load Distribution Factor for Fatigue = 0.78437 lanes/beam

Strength Limit State Stress/Strain summary for section with NEGATIVE moment

height of neutral axis = 144.439 mm
depth in compression = 144.439 mm

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Resistance Factor (ϕ) from Article 5.5.4.2.1

Type of force effect is:

Tension-controlled reinforced concrete:

$$\phi = 0.90$$

Location	strain	stress MPa	height mm
Precast beam - top	-0.02074	0.0	1143.0
- bottom	0.003	46.8843	0.0
C.I.P. stage 1 - top	-0.026971	0.0	1443.0
- bottom	-0.02074	0.0	1143.0
Reinforcement - top	-0.025671	-420.0	1380.4
- bottom	-0.025671	-420.0	1380.4

$$\begin{aligned}\text{Ultimate Strength capacity of section} &= -3877.05 \times 0.9 \\ &= -3489.35 \text{ kN.m}\end{aligned}$$

Strength Limit State Stress/Strain summary for section with POSITIVE moment

height of neutral axis = 1401.03 mm

depth in compression = 41.9696 mm

Resistance Factor (ϕ) from Article 5.5.4.2.1

Type of force effect is:

Compression-controlled sections:

with spirals or ties, $\phi = 0.75$

Location	strain	stress MPa	height mm
Precast beam - top	-0.018444	0.0	1143.0
- bottom	-0.100146	0.0	0.0
C.I.P. stage 1 - top	0.003	29.3027	1443.0
- bottom	-0.018444	0.0	1143.0
Reinforcement - top	-0.001475	-294.93	1380.4
- bottom	-0.001475	-294.93	1380.4

$$\begin{aligned}\text{Ultimate Strength capacity of section} &= 69.7806 \times 0.75 \\ &= 52.3354 \text{ kN.m}\end{aligned}$$

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SUMMARY OF APPLIED LOADINGS

	BENDING MOMENT kN.m	AXIAL kN
Erection loading before composite =	27.732897	0.0
Erection loading to stage 1A =	30.68843	0.0
Erection loading to stage 1B =	15.010684	0.0
Wearing Surface loading =	-161.854	0.0
Differential Shrinkage / Creep =	-10.79364	0.0
Transient loading =	-1965.399	0.0
TOTAL	-2064.615	0.0

Note:

The following effects are not considered (article 3.4.1) -
differential settlement
temperature gradient

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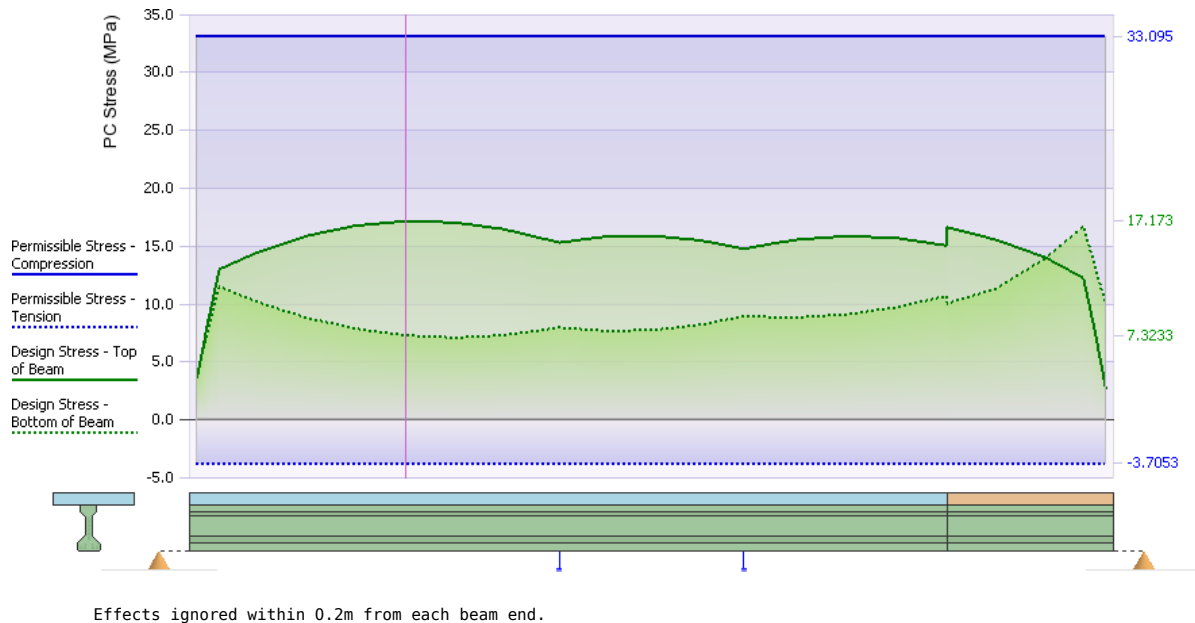
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Girder Design Calculations: Live Load Bending



Performance ratio = $17.2 / 33.1 = 0.519$

Section details:

Ref 1 "Section 1"
at $0.233 \times \text{span} = 0.233 \times 23.1136 = 5.40341$ m from left end of beam

Design Code:

AASHTO LRFD Bridge Design Specifications
Sixth Edition with 2013 Interim Revisions

Analysis:

Live Load Bending Moments
Transient Load BM 2 : [Max -ve]
Limit State - Service I
& Service III
for Normal environment conditions [A5.9.4.2.2b]

Approximate Methods of Analysis are used - Article 4.6.2

Live Load Distribution Factor for +ve Moment = 0.94124 lanes/beam
Live Load Distribution Factor for -ve Moment = 0.94124 lanes/beam
Live Load Distribution Factor for Shear = 0.94124 lanes/beam
Live Load Distribution Factor for Fatigue = 0.78437 lanes/beam

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ACTUAL STRESSES IN PRECAST BEAM

40 tendons are fully bonded at this section
0 tendons are fully debonded at this section
22 tendons are harped at this section

INITIAL PRESTRESS

height mm	No of tendons	f_{pu} MPa	area mm ²	% of f_{pu}	initial force kN
50.8	8	1861.58	98.71	75.0	1102.542
272.736	2	1861.58	98.71	75.0	275.17634
101.6	8	1861.58	98.71	75.0	1102.542
323.536	2	1861.58	98.71	75.0	275.17634
152.4	2	1861.58	98.71	75.0	275.6355
374.336	2	1861.58	98.71	75.0	275.17634
425.136	2	1861.58	98.71	75.0	275.17634
475.936	2	1861.58	98.71	75.0	275.17634
526.736	2	1861.58	98.71	75.0	275.17634
577.536	2	1861.58	98.71	75.0	275.17634
628.336	2	1861.58	98.71	75.0	275.17634
679.136	2	1861.58	98.71	75.0	275.17634
729.936	2	1861.58	98.71	75.0	275.17634
780.736	2	1861.58	98.71	75.0	275.17634
TOTAL	40				5507.6592

Transverse Eccentricity

Tendon layout is symmetrical about the vertical centroidal axis.

INITIAL RELAXATION - Article 5.9.5.4.4b

Data has the time from stressing to transfer set to zero, indicating that initial relaxation is not required to be calculated here.

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height mm	No of tendons	f_{pj}	f_{py} MPa	relax.	After relaxation		
				loss	area mm ²	force kN	moment kN.m
50.8	8	1396.19	1675.43	0.0	98.71	1102.542	56.009134
272.736	2	1393.86	1675.43	0.0	98.71	275.17634	75.050456
101.6	8	1396.19	1675.43	0.0	98.71	1102.542	112.01827
323.536	2	1393.86	1675.43	0.0	98.71	275.17634	89.029414
152.4	2	1396.19	1675.43	0.0	98.71	275.6355	42.006851
374.336	2	1393.86	1675.43	0.0	98.71	275.17634	103.00837
425.136	2	1393.86	1675.43	0.0	98.71	275.17634	116.98733
475.936	2	1393.86	1675.43	0.0	98.71	275.17634	130.96629
526.736	2	1393.86	1675.43	0.0	98.71	275.17634	144.94525
577.536	2	1393.86	1675.43	0.0	98.71	275.17634	158.9242
628.336	2	1393.86	1675.43	0.0	98.71	275.17634	172.90316
679.136	2	1393.86	1675.43	0.0	98.71	275.17634	186.88212
729.936	2	1393.86	1675.43	0.0	98.71	275.17634	200.86108
780.736	2	1393.86	1675.43	0.0	98.71	275.17634	214.84004
TOTAL	40					5507.6592	1804.432

Moment about the centroid of the precast beam:

$$M_r = 1804.432 - (5507.6592 \times 0.514946) \\ = -1031.714 \text{ kN.m}$$

Corresponding stresses:

$$\text{top stress} = 5507.66 / 360.967 + (-1031.71 / 8.31E7) \\ = 15.258068 + (-12.41531) \\ = 2.84276 \text{ MPa}$$

$$\text{bottom stress} = 5507.66 / 360.967 + (-1031.71 / -1.014E8) \\ = 15.258068 + 10.179396 \\ = 25.4375 \text{ MPa}$$

Self weight moment:

$$\begin{aligned} \text{c.s.a.} &= 3.61E5 \text{ mm}^2 \\ \text{density} &= 23.5631 \text{ kN/m}^3 \\ \text{self weight} &= 3.61E5 \times 23.5631 \\ &= 8.50551 \text{ kN/m} \\ \text{beam length} &= 23.1136 \text{ m} \\ \text{distance} &= 5.40341 \text{ m} \\ M_{sw} &= 0.5 \times 8.50551 \times 5.40341 \times (23.1136 - 5.40341) \\ &= 406.97 \text{ kN.m} \end{aligned}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 406.97 / 8.31E7 \\ &= 4.89735 \text{ MPa} \\ \text{bottom stress} &= 406.97 / -1.014E8 \\ &= -4.0154 \text{ MPa} \end{aligned}$$

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ELASTIC SHORTENING LOSSES - Article 5.9.5.2.3a

concrete stresses at mid-span:

stress at top of precast beam = 9.67786 MPa

stress at bottom of precast beam = 19.8333 MPa

depth of precast beam = 1143.0 mm

height mm	No of tendons	conc stress MPa	E_p/E_{ci}	tendon force kN	tendon moment kN.m
50.8	8	19.38196	6.084443	93.125732	4.7307872
272.736	2	17.41008	6.084443	20.912829	5.7036785
101.6	8	18.93061	6.084443	90.957086	9.2412399
323.536	2	16.95873	6.084443	20.370668	6.5906416
152.4	2	18.47925	6.084443	22.19711	3.3828396
374.336	2	16.50737	6.084443	19.828506	7.422521
425.136	2	16.05602	6.084443	19.286345	8.1993168
475.936	2	15.60467	6.084443	18.744183	8.9210291
526.736	2	15.15331	6.084443	18.202022	9.5876577
577.536	2	14.70196	6.084443	17.65986	10.199203
628.336	2	14.25061	6.084443	17.117699	10.755664
679.136	2	13.79925	6.084443	16.575537	11.257042
729.936	2	13.3479	6.084443	16.033376	11.703336
780.736	2	12.89655	6.084443	15.491214	12.094547
TOTAL	40			406.50217	119.7895

Moment about the centroid of the precast beam:

$$M_{ed} = 119.7895 - (406.50217 \times 0.514946) \\ = -89.5371 \text{ kN.m}$$

$$\text{hence top stress} = 9.6779 - 406.502/360.967 - -89.5371/8.31E7 \\ = 9.6779 - 1.1261477 - -1.07746 \\ = 9.62918 \text{ MPa}$$

$$\text{bottom stress} = 19.833 - 406.502/360.967 - -89.5371/-1.014E8 \\ = 19.833 - 1.1261477 - 0.8834166 \\ = 17.8237 \text{ MPa}$$

After a further 2 iterations of the above process, the top and bottom stresses are as follows:

$$\text{top stress} = 9.61749 \text{ MPa} \\ \text{bottom stress} = 17.993 \text{ MPa}$$

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REFINED ESTIMATES OF TIME-DEPENDENT LOSSES - Article 5.9.5.4

$$\begin{aligned}
 \text{Elastic modulus of prestressing steel: } E_p &= 197.0 \text{ kN/mm}^2 \\
 \text{Total effective tendon area: } A_{ps} &= 3944.8 \text{ mm}^2 \\
 \text{Elastic modulus of concrete at transfer: } E_{ci} &= 32.378 \text{ kN/mm}^2 \\
 \text{Percentage relative humidity: } H &= 70.0 \% \\
 \text{Humidity factor for creep: } k_{hc} &= 1.56 - 0.008H = 1.0 \\
 \text{Humidity factor for shrinkage: } k_{hs} &= 2.00 - 0.014H = 1.02 \\
 \text{Age at the end of curing: } t_c &= 3.0 \text{ day} \\
 \text{Age at transfer: } t_i &= 4.0 \text{ day} \\
 \text{Age at in-situ casting: } t_d &= 60.0 \text{ day} \\
 \text{Final age: } t_f &= 120.0 \text{ day} \\
 \text{Comp. strength of conc. at 1st loading: } f'_{ci} &= 41.37 \text{ MPa} \\
 \text{Factor for the effect of concrete strength: } k_f &= \frac{35.0}{7 + f'_{ci}} = \frac{35.0}{7 + 41.4} = 0.7236
 \end{aligned}$$

$$\begin{aligned}
 \text{Time factor for creep at final time: } k_{tdc, f, i} &= \frac{t_f - t_i}{61 - 0.58 * f'_{ci} + t_f - t_i} \\
 &= \frac{120.0 - 4.0}{61 - 0.58 * 41.4 + 120.0 - 4.0} \\
 &= 0.7581
 \end{aligned}$$

$$\begin{aligned}
 \text{Time fac. for shrinkage at final time: } k_{tds, f, i} &= \frac{t_f - t_c}{61 - 0.58 * f'_{ci} + t_f - t_c} \\
 &= \frac{120.0 - 3.0}{61 - 0.58 * 41.4 + 120.0 - 3.0} \\
 &= 0.7597
 \end{aligned}$$

Losses: Time of Transfer to Time of Deck Placement - Article 5.9.5.4.2

$$\begin{aligned}
 \text{Gross area of section: } A_g &= 3.61\text{E}5 \text{ mm}^2 \\
 \text{Perimeter of section: } p &= 3503.7 \text{ mm} \\
 \text{Volume to surface ratio: } V/S = A_g/p &= 103.02 \text{ mm} \\
 \text{Factor for the effect of the volume: } k_s &= 1.45 - 0.0051 * (V/S) = 0.9245 \\
 \text{Creep coefficient at final time: } \psi_b(t_f, t_i) &= 1.9 * k_s * k_{hc} * k_f * k_{tdc, f, i} * t_i^{-0.118} \\
 &= 1.9 * 0.9245 * 1.0 * 0.7236 * 0.7581 * 4.0^{-0.118} \\
 &= 0.8182 \\
 \text{Inertia of the gross concrete section: } I_g &= 5.22\text{E}10 \text{ mm}^4 \\
 \text{Eccentricity of prestressing force: } e_{pg} &= -185.17 \text{ mm}
 \end{aligned}$$

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Transformed section coefficient:

$$K_{id} = \frac{1}{1 + \frac{E_p}{E_{ci}} \cdot \frac{A_{ps}}{A_g} \left[1 + \frac{A_g \cdot e_{pg}^2}{I_g} \right] \cdot [1 + 0.7 \cdot \psi_b(t_f, t_i)]}$$

$$= \frac{1}{1 + \frac{197.0}{32.378} \cdot \frac{3944.8}{3.61E5} \left[1 + \frac{3.61E5 \cdot 185.2^2}{5.2E10} \right] \cdot (1 + 0.7 \cdot 0.8182)}$$

$$= 0.88544$$

Time factor for creep at deck placement:

$$k_{tdc,d,i} = \frac{t_d - t_i}{61 - 0.58 \cdot f'_{ci} + t_d - t_i}$$

$$= \frac{60.0 - 4.0}{61 - 0.58 \cdot 41.4 + 60.0 - 4.0}$$

$$= 0.602$$

Time factor for shrinkage at deck placement:

$$k_{tds,d,i} = \frac{t_d - t_c}{61 - 0.58 \cdot f'_{ci} + t_d - t_c}$$

$$= \frac{60.0 - 3.0}{61 - 0.58 \cdot 41.4 + 60.0 - 3.0}$$

$$= 0.606$$

Shrinkage of Girder Concrete - Article 5.9.5.4.2a

Concrete shrinkage strain of girder: $\epsilon_{bid} = k_s \cdot k_{hs} \cdot k_f \cdot k_{tds,d,i} \cdot 0.00048$

$$= 1.0 \cdot 1.02 \cdot 0.71 \cdot 0.60 \cdot 0.00048$$

$$= 2.121E-4$$

Loss of prestress = $\epsilon_{bid} \cdot E_p \cdot K_{id}$

$$= 2.12E-4 \cdot 197.0 \cdot 0.88294$$

$$= 36.886 \text{ MPa}$$

$$= \Delta f_{psR}$$

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$$\begin{aligned}\text{Total shrinkage loss of force} &= \Delta f_{pSR} \cdot A_{ps} \\ &= 36.886 \cdot 3944.78 \\ &= 145.507 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding gain of moment} &= 145.507 \cdot 0.32977 \\ (\text{about } y = 0) &= 47.985 \text{ kN.m}\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{sh} &= 47.985 - (145.507 \cdot 0.51494) \\ &= -26.943 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 145.507/360967 + (-26.9434/8.31E7) \\ &= 0.4031039 + (-0.324228) \\ &= 0.078876 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 145.507/360967 + (-26.9434/-1.014E8) \\ &= 0.4031039 + 0.2658366 \\ &= 0.668941 \text{ MPa}\end{aligned}$$

Creep of Girder Concrete - Article 5.9.5.4.2b

Creep coefficient at deck placement:

$$\begin{aligned}\psi_b(t_d, t_i) &= 1.9k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, d, i} \cdot t_i^{-0.118} \\ &= 1.9 \cdot 1.0 \cdot 1.0 \cdot 0.7142 \cdot 0.6021 \cdot 4.0^{-0.118} \\ &= 0.6938\end{aligned}$$

Concrete stress at the center of gravity of prestressing tendons:

concrete stresses at transfer:

$$\begin{aligned}\text{at top of precast beam} &= 9.82068 \text{ MPa} \\ \text{at bottom of precast beam} &= 19.7162 \text{ MPa} \\ \text{at center of gravity of prestress: } f_{cgp} &= 16.8612 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{Loss of prestress} &= \frac{E_p}{E_{ci}} \cdot f_{cgp} \cdot \psi_b(t_d, t_i) \cdot K_{id} \\ &= \frac{197.0}{32.3777} \cdot 16.861 \cdot 0.6938 \cdot 0.8846 \\ &= 62.9755 \text{ MPa} \\ &= \Delta f_{PCR}\end{aligned}$$

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$$\begin{aligned}\text{Total creep loss of force} &= \Delta f_{pCR} \cdot A_{ps} \\ &= 62.9755 \cdot 3944.78 \\ &= 248.425 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding loss of moment} &= 248.425 \cdot 0.32977 \\ &= 81.9248 \text{ kN.m} \\ &\quad (\text{about } y = 0)\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{Cr} &= 81.9248 - (248.425 \cdot 0.51494) \\ &= -46.001 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 248.425 / 3.61\text{E}5 + -46.001 / 8.31002\text{E}7 \\ &= 0.68822 + -0.5535 \\ &= 0.13466 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 248.425 / 3.61\text{E}5 + -46.001 / -1.0135\text{E}8 \\ &= 0.68822 + 0.45386 \\ &= 1.14208 \text{ MPa}\end{aligned}$$

Relaxation of Prestressing Strands - Article 5.9.5.4.2c

$$\begin{aligned}\text{Stress in tendons after transfer:} & f_{pt} = 1301.17 \text{ MPa} \\ \text{Yield strength of prestressing steel:} & f_{py} = 1675.43 \text{ MPa} \\ \text{Time between tensioning and deck placement:} & t = t_s - t_i = 60.0 - 4.0 = 56.0 \text{ day} \\ \text{Factor for relaxation steel type:} & K'_L = 45.0 \text{ (low relaxation)}\end{aligned}$$

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$$\begin{aligned} \text{Loss of prestress} &= \frac{f_{pt}}{K'_L} \cdot \frac{\log(24t)}{\log(24t_i)} \cdot \left[\frac{f_{pt}}{f_{py}} - 0.55 \right] \cdot \left[1 - \frac{3(\Delta f_{pSR} + \Delta f_{pCR})}{f_{pt}} \right] \cdot K_{id} \\ &= \frac{1301.2}{45.0} \cdot \frac{\log(24 \cdot 56.0)}{\log(24 \cdot 4.0)} \cdot \left[\frac{1301.2}{1675.4} - 0.55 \right] \cdot \left[1 - \frac{3 \cdot (36.886 + 62.976)}{1301.2} \right] \cdot 0.88 \\ &= 7.02855 \text{ MPa} \\ &= \Delta f_{pR1} \end{aligned}$$

$$\begin{aligned} \text{Total relaxation loss of force} &= \Delta f_{pR1} \cdot A_{ps} \\ &= 7.0286 \cdot 3944.8 \\ &= 27.726113 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Corresponding loss of moment} &= 27.726 \cdot 0.3297 \\ &= 9.1434367 \text{ kN.m} \\ &\quad (\text{about } y = 0) \end{aligned}$$

$$\begin{aligned} \text{Moment about the centroid of the composite beam:} \\ M_{rx} &= 9.14344 - (27.7261 \cdot 0.5149) \\ &= -5.134 \text{ kN.m} \end{aligned}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 27.7261/360967 + -5.13401/8.31E7 \\ &= 0.0768107 + -0.061781 \\ &= 0.0150297 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 27.7261/360967 + -5.13401/-1.014E8 \\ &= 0.0768107 + 0.0506546 \\ &= 0.127465 \text{ MPa} \end{aligned}$$

Erection of beam Loading

Bending moment from erection loadcase at current span location:

$$M_{\text{Applied}} = 481.82514 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 481.82514/8.31E7 \\ &= 5.79813 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 481.82514/-1.014E8 \\ &= -4.7539 \text{ MPa} \end{aligned}$$

Remove the dead load applied for transfer calculations

$$M_{sw} = -406.97 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= -406.97/8.31E7 \\ &= -4.8973 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= -406.97/-1.014E8 \\ &= 4.01537 \text{ MPa} \end{aligned}$$

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Construction stage 1A Loading

$$M_{\text{Applied}} = 746.7127 \text{ kN.m}$$

Corresponding stresses:

$$\text{top stress} = 746.7127/8.31\text{E}7$$

$$= 8.98569 \text{ MPa}$$

$$\text{bottom stress} = 746.7127/-1.014\text{E}8$$

$$= -7.3674 \text{ MPa}$$

Construction stage 1B Loading

$$M_{\text{Applied}} = 41.902235 \text{ kN.m}$$

Corresponding stresses:

$$\text{top stress} = 41.902235/8.31\text{E}7$$

$$= 0.50423 \text{ MPa}$$

$$\text{bottom stress} = 41.902235/-1.014\text{E}8$$

$$= -0.4134 \text{ MPa}$$

Losses: Time of Deck Placement to Final Time - Article 5.9.5.4.3

$$\text{Gross composite section area: } A_c = 9.72\text{E}5 \text{ mm}^2$$

$$\text{Perimeter of section: } p = 7365.6 \text{ mm}$$

$$\text{Volume to surface ratio: } V/S = A_c/p = 131.99 \text{ mm}$$

$$\text{Factor for the effect of the volume: } k_s = 1.45 - 0.0051 \cdot (V/S) = 0.7768$$

Creep coefficient at final time:

$$\begin{aligned} \psi_b(t_f, t_i) &= 1.9 \cdot k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, f, i} \cdot t_i^{-0.118} \\ &= 1.9 \cdot 0.776 \cdot 1.0 \cdot 0.723 \cdot 0.758 \cdot 4.0^{-0.118} \\ &= 0.6875 \end{aligned}$$

$$\text{Inertia of the net concrete section: } I_c = 1.94\text{E}8 \text{ mm}^4$$

$$\text{Eccentricity of prestressing force: } e_{pc} = 0.6743 \text{ mm}$$

Transformed section coefficient:

$$\begin{aligned} K_{df} &= \frac{1}{1 + \frac{E_p}{E_{ci}} \cdot \frac{A_{ps}}{A_c} \left[1 + \frac{A_c \cdot e_{pc}^2}{I_c} \right] \cdot [1 + 0.7 \cdot \psi_b(t_f, t_i)]} \\ &= \frac{1}{1 + \frac{197.0}{32.378} \cdot \frac{3944.8}{9.72\text{E}5} \left[1 + \frac{9.72\text{E}5 \cdot 674.33^2}{1.9\text{E}11} \right] \cdot (1 + 0.7 \cdot 0.6875)} \\ &= 0.89298 \end{aligned}$$

Shrinkage of Girder Concrete - Article 5.9.5.4.3a

$$\begin{aligned} \text{Concrete shrinkage strain of girder: } \epsilon_{bdf} &= k_s \cdot k_{hs} \cdot k_f \cdot k_{tds, f, i} \cdot 0.00048 \\ &= 1.0 \cdot 1.02 \cdot 0.71 \cdot 0.76 \cdot 0.00048 \\ &= 2.657\text{E}-4 \end{aligned}$$

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$$\begin{aligned}\text{Loss of prestress} &= \epsilon_{bdf} \cdot E_p \cdot K_{df} \\ &= 2.66\text{E-}4 \cdot 1.97\text{E}8 \cdot 0.88465 \\ &= 46.3042 \text{ MPa} \\ &= \Delta f_{pSD}\end{aligned}$$

$$\begin{aligned}\text{Total shrinkage loss of force} &= \Delta f_{pSD} \cdot A_{ps} \\ &= 46.3042 \cdot 3944.78 \\ &= 182.66 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding gain of moment} &= 182.66 \cdot 0.32977 \\ (\text{about } y = 0) &= 60.2371 \text{ kN.m}\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{sh} &= 60.2371 - (182.66 \cdot 0.9603) \\ &= -115.17 \text{ kN.m}\end{aligned}$$

Corresponding stresses:

$$\begin{aligned}\text{top stress} &= 182.66 / 844161 + (-115.17) / 9.901\text{E}8 \\ &= 0.2163807 + (-0.116321) \\ &= 0.10006 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{bottom stress} &= 182.66 / 844161 + (-115.17) / -1.884\text{E}8 \\ &= 0.2163807 + 0.6114031 \\ &= 0.827784 \text{ MPa}\end{aligned}$$

Creep of Girder Concrete - Article 5.9.5.4.2b

Creep coefficient at deck placement:

$$\begin{aligned}\psi_b(t_d, t_i) &= 1.9k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, d, i} \cdot t_i^{-0.118} \\ &= 1.9 \cdot 1.0 \cdot 1.0 \cdot 0.7142 \cdot 0.6021 \cdot 4.0^{-0.118} \\ &= 0.6938\end{aligned}$$

Creep coefficient at final time:

$$\begin{aligned}\psi_b(t_f, t_d) &= 1.9k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, f, i} \cdot t_d^{-0.118} \\ &= 1.9 \cdot 1.0 \cdot 1.0 \cdot 0.7142 \cdot 0.6185 \cdot 60.0^{-0.118} \\ &= 0.5178\end{aligned}$$

Concrete stress at the center of gravity of prestressing tendons:

concrete stresses at transfer:

$$\begin{aligned}\text{at top of precast beam} &= 9.82068 \text{ MPa} \\ \text{at bottom of precast beam} &= 19.7162 \text{ MPa} \\ \text{at center of gravity of prestress: } f_{cgp} &= 16.8612 \text{ MPa}\end{aligned}$$

Change in concrete stress at centroid of prestressing strands:

concrete stress change after permanent loads:

$$\begin{aligned}\text{at top of precast beam} &= 12.254 \text{ MPa} \\ \text{at bottom of precast beam} &= 11.3917 \text{ MPa} \\ \Delta f_{cd} &= 11.6405 \text{ MPa}\end{aligned}$$

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$$\begin{aligned}
 \text{Loss of prestress} &= \frac{E_p}{E_{ci}} * f_{cgp} * \left[\psi_b(t_f, t_i) - \psi_b(t_d, t_i) \right] * K_{df} \\
 &+ \frac{E_p}{E_c} * \Delta f_{cd} * \psi_b(t_f, t_d) * K_{df} \\
 &= \frac{197.0}{32.3777} * 16.8612 * (0.87367 - 0.69388) * 0.88294 \\
 &+ \frac{197.0}{18.6932} * 11.6405 * 0.51782 * 0.88294 \\
 &= 72.3739 \text{ MPa} \\
 &= \Delta f_{pCD}
 \end{aligned}$$

$$\begin{aligned}
 \text{Total creep loss of force} &= \Delta f_{pCD} * A_{ps} \\
 &= 72.3739 * 3944.78 \\
 &= 285.499 \text{ kN}
 \end{aligned}$$

$$\begin{aligned}
 \text{Corresponding loss of moment} &= 285.499 * 0.32977 \\
 &= 94.1512 \text{ kN.m} \\
 &\quad (\text{about } y = 0)
 \end{aligned}$$

$$\begin{aligned}
 \text{Moment about the centroid of the composite beam:} \\
 M_{cr} &= 94.1512 - (285.499 * 0.9603) \\
 &= -180.01 \text{ kN.m}
 \end{aligned}$$

Corresponding stresses:

$$\begin{aligned}
 \text{top stress} &= 285.499 / 8.442\text{E}5 + -180.01 / 9.90117\text{E}8 \\
 &= 0.33820 + -0.1818 \\
 &= 0.15639 \text{ MPa}
 \end{aligned}$$

$$\begin{aligned}
 \text{bottom stress} &= 285.499 / 8.442\text{E}5 + -180.01 / -1.8837\text{E}8 \\
 &= 0.33820 + 0.95562 \\
 &= 1.29383 \text{ MPa}
 \end{aligned}$$

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Relaxation of Prestressing Strands - Article 5.9.5.4.3c

$$\begin{aligned}\text{Loss of prestress} &= \Delta f_{pR1} \\ &= 7.02855 \text{ MPa} \\ &= \Delta f_{pR2}\end{aligned}$$

$$\begin{aligned}\text{Total relaxation loss of force} &= \Delta f_{pR2} \cdot A_{ps} \\ &= 7.0286 \cdot 3944.8 \\ &= 27.726113 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Corresponding loss of moment} &= 27.726 \cdot 0.3297 \\ &= 9.1434367 \text{ kN.m} \\ &\quad (\text{about } y = 0)\end{aligned}$$

$$\begin{aligned}\text{Moment about the centroid of the composite beam:} \\ M_{rx} &= 9.14344 - (27.7261 \cdot 0.9603) \\ &= -17.482 \text{ kN.m}\end{aligned}$$

$$\begin{aligned}\text{Corresponding stresses:} \\ \text{top stress} &= 27.7261/844161 + (-17.482/9.901E8) \\ &= 0.0328446 + (-0.017656) \\ &= 0.0151881 \text{ MPa} \\ \text{bottom stress} &= 27.7261/844161 + (-17.482/-1.884E8) \\ &= 0.0328446 + 0.0928054 \\ &= 0.12565 \text{ MPa}\end{aligned}$$

Shrinkage of Deck Concrete - Article 5.9.5.4.3d

$$\begin{aligned}\text{Concrete shrinkage strain of girder:} \quad \epsilon_{ddf} &= k_s \cdot k_{hs} \cdot k_f \cdot k_{tds, f, i} \cdot 0.00048 \\ &= 1.025 \cdot 1.02 \cdot 0.71 \cdot 0.76 \cdot 0.00048 \\ &= 2.724E-4\end{aligned}$$

Creep coefficient at final time:

$$\begin{aligned}\psi_b(t_f, t_d) &= 1.9 k_s \cdot k_{hc} \cdot k_f \cdot k_{tdc, f, i} \cdot t_d^{-0.118} \\ &= 1.9 \cdot 1.0253 \cdot 1.0 \cdot 0.7142 \cdot 0.6185 \cdot 60.0^{-0.118} \\ &= 0.5309\end{aligned}$$

Change in concrete stress at centroid of prestressing strands:

$$\begin{aligned}\text{Area of deck concrete:} \quad A_d &= 6.112E5 \text{ mm}^2 \\ \text{Perimeter of section:} \quad p &= 7365.55 \text{ mm} \\ \text{Volume to surface ratio:} \quad V/S &= A_d/p = 82.98 \text{ mm} \\ \text{Factor for the effect of the volume:} \quad k_s &= 1.45 - 0.0051 \cdot (V/S) = 1.4333 \\ \text{Modulus of elasticity of deck concrete:} \quad E_{cd} &= 29.5566 \text{ mm}^2 \\ \text{Eccentricity of the deck:} \quad e_d &= 288.894 \text{ mm}^3\end{aligned}$$

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$$\Delta f_{cdf} = \frac{\epsilon_{ddf} \cdot A_d \cdot E_{cd}}{[1 + 0.7\psi_b(t_f, t_d)]} \left[\frac{1}{A_c} - \frac{e_{pc} \cdot e_d}{I_c} \right]$$

$$= \frac{2.7E-4 * 6.11E5 * 29.557 * 1000}{[1 + 0.7 * 0.5309]} \left[\frac{1}{8.44E5} - \frac{630.523 * 288.894}{1.8E11} \right]$$

$$= 0.63733 \text{ MPa}$$

$$\text{Loss of prestress} = \frac{E_p}{E_c} \cdot \Delta f_{cdf} \cdot K_{df} \cdot [1 + 0.7\psi_b(t_f, t_d)]$$

$$= \frac{197.0}{18.6932} * 0.63733 * 0.88465 * (1 + 0.7 * 0.53092)$$

$$= 8.15021 \text{ MPa}$$

$$= \Delta f_{pss}$$

$$\begin{aligned} \text{Total shrinkage gain of force} &= \Delta f_{pss} \cdot A_{ps} \\ &= 8.15021 * 3944.78 \\ &= 32.1508 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Corresponding gain of moment} &= 32.1508 * 0.32977 \\ (\text{about } y = 0) &= 10.6026 \text{ kN.m} \end{aligned}$$

$$\begin{aligned} \text{Moment about the centroid of the composite beam:} \\ M_{sh} &= 10.6026 - (32.1508 * 0.9603) \\ &= -20.272 \text{ kN.m} \end{aligned}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 32.1508 / 844161 + (-20.2718 / 9.901E8) \\ &= 0.0380861 + (-0.020474) \\ &= 0.017612 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 32.1508 / 844161 + (-20.2718 / -1.884E8) \\ &= 0.0380861 + 0.1076157 \\ &= 0.145702 \text{ MPa} \end{aligned}$$

Superimposed dead load 1 Loading

$$M_{\text{Applied}} = 129.34157 \text{ kN.m}$$

Corresponding stresses:

$$\begin{aligned} \text{top stress} &= 129.34157 / 9.9012E8 \\ &= 0.13063 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{bottom stress} &= 129.34157 / -1.884E8 \\ &= -0.6866 \text{ MPa} \end{aligned}$$

Transient Load BM 2 : [Max -ve] Loading

$$\begin{aligned} M_{\text{Applied}} &= -192.9 \text{ kN.m} && \text{for Service-I} \\ &= -154.32 \text{ kN.m} && \text{for Service-III} \end{aligned}$$

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Corresponding stresses:

top stress = -192.9/9.9012E8 Service-I
 = -0.1948 MPa
bottom stress = -154.32/-1.884E8 Service-III
 = 0.81922 MPa

PERMISSIBLE STRESSES IN PRECAST BEAM

Compression

Article 5.9.4.2.1 for permanent & transient loads
Permissible compression stress = $0.6 * f'_c$
 = $0.6 * 55.1581$
 = 33.09 MPa

Tension

Article 5.9.4.2.2
Component is subject to normal exposure conditions.
Permissible tension stress = $-0.498 * \sqrt{f'_c}$
 = $-0.498 * \sqrt{55.1581}$
 = -3.70451 MPa

PERMISSIBLE STRESSES FOR CAST IN PLACE CONCRETE

Compression

Article 5.9.4.2
char. strength of c.i.p. concrete = 34.4738 MPa
stress limitation factor = 0.6
permissible compression stress = $0.6 * f_{cu}$
 = $0.6 * 34.4738$
 = 20.6843 MPa

Tension

Article 5.7.3.4
Flexural tensile stresses may need to be limited by cracking considerations
in accordance with article 5.7.3.4.

SERVICE LIMIT STATE - STRESS SUMMARY TABLE **maximum for girder top extreme fibre**

	Concrete Stresses (MPa)					
	force kN	moment kN.m	Cast In Place top bottom		Precast top bottom	
Prestress	5507.66	-1031.7			2.84276	25.4375
Self Weight		406.97			4.89735	-4.0154
Prestress + Self Wt.					7.7401	21.4221
Elastic Def	-374.83	81.2753			-0.0604	-1.8403
TRANSFER	5132.83	-543.47			7.67973	19.5818

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Erection	74.855			0.90078	-0.7385
C.I.P. Stage 1A	746.713			8.98569	-7.3674
C.I.P. Stage 1B	41.9022	0.0884	0.03346	0.04232	-0.2224

Time-Dependent Losses

Time of Transfer to Time of Deck Placement

Shrinkage	-145.51	26.9434		-0.0789	-0.6689
Creep	-248.42	46.0005		-0.1346	-1.1421
Relaxation	-27.726	5.13401		-0.015	-0.1274

Time of Deck Placement to Final Time

Shrinkage

Girder	-182.66	115.171	0.0719	-0.0791	-0.1000	-0.8277
Deck	-4.5741	2.88407	0.0018	-0.002	-0.0025	-0.0207
Creep	-285.5	180.014	0.11237	-0.1236	-0.1563	-1.2938
Relaxation	-27.726	17.482	0.01091	-0.012	-0.0152	-0.1256

Wearing Surface	129.342	0.27285	0.10327	0.13063	-0.6866	
(Diff. Shr. 1	4.57409	-2.8841	9.98E-4	0.27517	0.00251	0.02073)
(Diff. Shr. 2	-5.601	-0.0118	-0.0045	-0.0057	0.02973)	
(Differential shrinkage is not adverse or not specified)						

TOTAL PERMANENT	0.55823	-0.08	17.2364	6.36024
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(Y_{TG} = 0.5)

Temp Grad P1	-752.44	-291.34	2.3162	-0.5968	-0.7549	0.65526
Temp Grad P2		96.3319	0.20321	0.07692	0.09729	-0.5113
Temp Grad R1	150.487	58.2675	-0.4632	0.11936	0.15098	-0.1310
Temp Grad R2		-19.268	-0.0406	-0.0154	-0.0195	0.10228

(Temperature restraint is not adverse or not specified)

TRANSIENT LOADS

Transient Load BM 1- I	1863.99	3.93222		1.8826
- III	1491.2		1.19066	-7.9162
Transient Load BM 2- I	-192.9	-0.4069		-0.1948
- III	-154.32		-0.1232	0.81922

TOTAL PERMANENT LOAD + TRANSIENT LOAD

Transient Load BM 2	2.67072	-0.0992	17.1731	7.32333
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SLS FLEXURE calculated using curvature of uncracked sections

The deflections are calculated from integration of the curvatures along the beam, using the parameters detailed below:

(Note that the reported values of deflections for live loadings are exaggerated when these are derived from enveloped effects)

Elastic Modulus at Transfer, $E_T = 32.3777 \text{ kN/mm}^2$
Intermediate Term Elastic Modulus, $E_I = 22.0714 \text{ kN/mm}^2$
 $E_I = E_C / (\psi(t, t_i) + 1)$
where $\psi(t, t_i) = 0.69388$ (Article 5.14.2.3.6)]
Effective Elastic Modulus for time dependant effects, $E_E = 34.2214 \text{ kN/mm}^2$
 $E_E = E_S \cdot (\psi_{tc\%} + ((1 - \psi_{tc\%}) / (1 + \chi \cdot \psi)))$
 ψ = creep factor = 0.87367
 $\psi_{tc\%}$ = percentage of creep occurring before c.i.p. deck added
= $0.69388 / 0.87367 = 79.4216\%$
 χ = ageing factor, taken as 0.8
Short Term Elastic Modulus, $E_S = 37.3865 \text{ kN/mm}^2$

Precast section height = 1143.0 mm

	Precast			Curvature	Deflection	
	Stress (MPa)	E	Strain ($\times 10^{-6}$)	($\times 10^{-6}$) (rad/m)	(mm) Here	Max.
At Transfer	T 9.20544	E_T	284.315	-249.49	15.9064	30.3396
	B 18.4384		569.48			
At Erection	T 9.53222	E_I	431.88	-260.0	20.4644	36.1998
	B 16.0914		729.059			
Long-term Dead	T 16.8135					
	B 6.99716					
Dead Stress Increment	T 7.6081	E_E	222.32	487.008	-29.119	-49.25
	B -11.441		-334.33			
Total Dead Load deflection				227.01	-8.6541	-13.05
Transient Load BM 2-I	T -0.1558	E_S	-4.1687	-22.817	2.2014	4.39981
	B 0.81918		21.9112			
Extreme in-service				204.192	-6.4527	-8.8909

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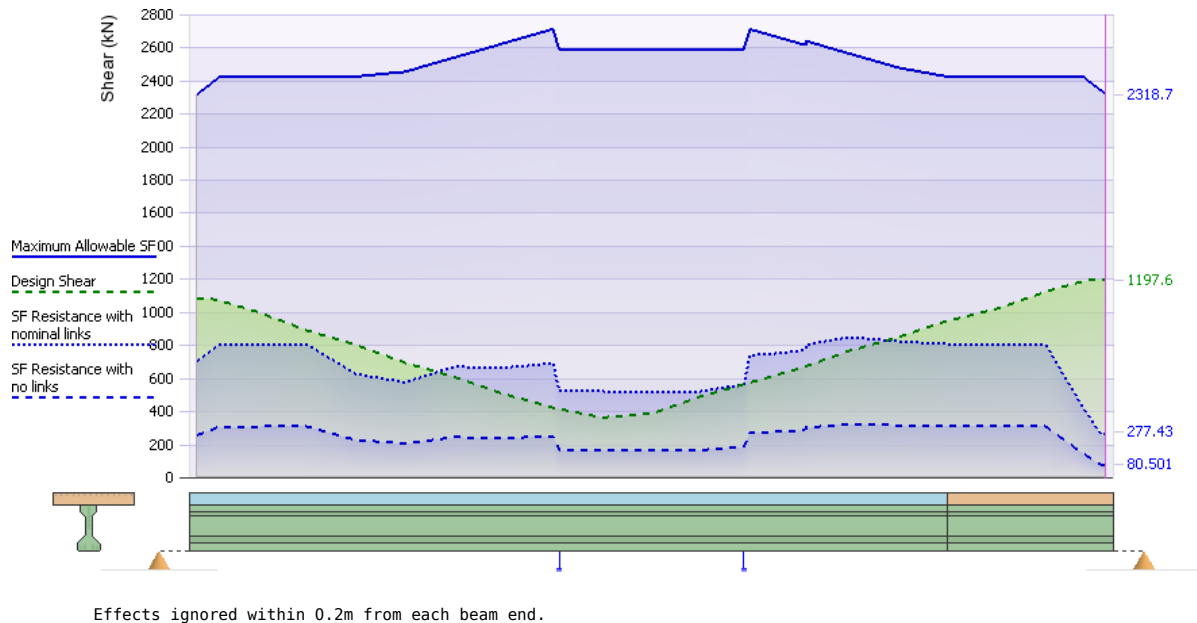
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Girder Design Calculations: Shear



Performance ratio = $1198 / 2319 = 0.516$

Section details:

Ref 2 "Section 2"
at $0.991 \times \text{span} = 0.991 \times 23.1136 = 22.9136$ m from left end of beam

Design Code:

AASHTO LRFD Bridge Design Specifications
Sixth Edition with 2013 Interim Revisions

Analysis:

Shear Forces and associated Bending Moments
Transient Load SF + assoc. BM 1
Limit State - Strength I

Approximate Methods of Analysis are used - Article 4.6.2

Live Load Distribution Factor for +ve Moment = 0.94124 lanes/beam
Live Load Distribution Factor for -ve Moment = 0.94124 lanes/beam
Live Load Distribution Factor for Shear = 0.94124 lanes/beam
Live Load Distribution Factor for Fatigue = 0.78437 lanes/beam

SUMMARY OF APPLIED LOAD EFFECTS

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	SHEAR FORCE kN	BENDING MOMENT kN.m	AXIAL LOAD kN
Erection loading before composite =	129.42331	27.732897	0.0
Erection loading to stage 1A =	144.09112	30.68843	0.0
Erection loading to stage 1B =	69.170412	15.010684	0.0
Wearing surface loading =	56.69805	-161.854	0.0
Differential Shrinkage / Creep =	0.4580671	-10.79364	0.0
Transient loading:			
Max SF + associated BM =	797.73786	-735.5756	0.0
Max BM + associated SF =	487.02182	-1965.399	0.0
TOTAL - Max SF + associated BM:	1197.5788	-834.7912	0.0
- Max BM + associated SF:	886.86278	-2064.615	0.0

Note:

The following effects are not considered (article 3.4.1) -
differential settlement
temperature gradient

The current section is closer to the support than the critical section for shear (article 5.8.3.2). The shear forces in the table are therefore the values at the critical section for shear.

Article 5.8.3 Transverse Shear Reinforcement

The '*maximum SF with associated BM*' loadcase is critical at this section.

factored shear force $V_u = 1197.58 \text{ kN}$
factored moment $M_u = -834.79 \text{ kN.m}$

The factored moment at this section is negative, and so the following calculations relate to the inverted section

Calculate effective shear depth, d_v - Article 5.8.2.9

overall depth of section $h = 1443.0 \text{ mm}$
compression fibre to tension force centroid $d_e = -1118.8 \text{ mm}$
resistance moment of section (no axial load) $M_r = -5824.3 \text{ kN.m}$
total tension force $T = 5803.48 \text{ kN}$
distance from resultant tension to compression $= M_r / T$
 $= 1.00358 \text{ m}$
 $0.9 * d_e = 0.9 * -1118.8 = -1006.9 \text{ mm}$
 $0.72 * h = 0.72 * 1443.0 = 1038.96 \text{ mm}$
hence, effective shear depth, $d_v = 1038.96 \text{ mm}$

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Critical section for shear - Article 5.8.3.2

angle of compressive stress (see below) $\theta = 41.3479^\circ$

$$0.5 \cdot d_v \cdot \cot(\theta) = 0.5 \cdot 1038.96 \cdot 1.13636 \\ = 590.316 \text{ mm}$$

critical section for shear is larger of d_v and 0.59031

hence, critical section for shear:

from face of support = 1.03896 m

from end of the beam = 22.4692 m

Determine β and θ - Article 5.8.3.4

Shear stress on the concrete - 5.8.2.9-1

Resistance factor for shear [A5.5.4.2] $\phi = 0.9$
Vertical component of prestress at section $V_p = 29.0241 \text{ kN}$

$$v = \frac{V_u - \phi \cdot V_p}{\phi \cdot b_v \cdot d_v} = \frac{1197.58 - 0.9 \cdot 29.0241}{0.9 \cdot 0.1778 \cdot 1.03896} = 7.04617 \text{ MPa}$$

Factored axial force	$N_u = 0.0 \text{ kN}$
Area of prestress steel on tension side	$A_{ps} = 1579.36 \text{ mm}^2$
Area of concrete on flexural tension side	$A_c = 6.118\text{E}5 \text{ mm}^2$
Area of non-prestress steel on tension side	$A_s = 0.0 \text{ mm}^2$
Modulus of elasticity of tendons	$E_p = 197.0 \text{ kN/mm}^2$
Modulus of elasticity of non-prestress steel	$E_s = 0.0 \text{ kN/mm}^2$
Modulus of elasticity of concrete	$E_c = 37.3865 \text{ kN/mm}^2$
	$f_{po} = 0.7 \cdot f_{pu}$
	$= 0.7 \cdot 1861.58$
	$= 1303.11 \text{ MPa}$
Factored moment (not less than $ V_u - V_p d_v$)	$ M_u = 2064.61 \text{ MPa}$

General procedure: (Article 5.8.3.4.2)

Strain in reinforcement:

$$\epsilon_s = \frac{\frac{|M_u|}{d_v} + 0.5N_u + |V_u - V_p| - A_{ps}f_{po}}{E_sA_s + E_pA_{ps}} \quad (\text{Eq. 5.8.3.4.2-4})$$

$$\epsilon_s = \frac{\left[\frac{2064.6}{1039.0} + 0.5 \cdot 0.0 + |1197.6 - 29.024| - 1579.4 \cdot 1303.1 \right]}{0.0 \cdot 0.0 + 197.0 \cdot 0.0016} \\ = 0.0035$$

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with at least the minimum amount of shear reinforcement:

$$\beta = \frac{4.8}{(1 + 750\epsilon_s)} = \frac{4.8}{(1 + 750*0.0035)} \quad (\text{Eq. 5.8.3.4.2-1})$$

$$= 1.31652$$

with no shear reinforcement:

$$s_x = 1.03896 \text{ m}$$

$$\text{maximum aggregate size: } a_g = 25.4 \text{ mm} = 1.0 \text{ IN}$$

$$s_{xe} = s_x * \frac{1.38}{a_g + 0.63} = 1.039 * \frac{1.38}{1.0 + 0.63} = 0.87961 \text{ m}$$

$$= 34.6303 \text{ IN}$$

$$12.0\text{IN} \leq s_{xe} \leq 80.0\text{IN}$$

$$s_{xe} = 34.6303 \text{ IN}$$

$$\beta = \frac{4.8}{(1 + 750\epsilon_s)} * \frac{51}{(39 + s_{xe})} \quad (\text{Eq. 5.8.3.4.2-2})$$

$$= \frac{4.8}{(1 + 750*0.0035)} * \frac{51}{(39 + 34.63)}$$

$$= 0.91188$$

$$\theta = 29 + 3500\epsilon_s \quad (\text{Eq. 5.8.3.4.2-3})$$

$$= 29 + 3500* 0.0035$$

$$= 41.3479$$

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Nominal Shear Resistance **Article 5.8.3.3**

inclination of the transverse reinforcement, $\alpha = 90.0^\circ$

$$\text{nominal shear resistance } V_n = V_c + V_s + V_p \quad (5.8.3.3-1)$$

with at least the minimum amount of shear reinforcement:

$$\begin{aligned} V_c &= 0.08297 \cdot \beta (\sqrt{f'_c}) \cdot b_v \cdot d_v & (5.8.3.3-3) \\ &= 0.08297 \cdot 1.3165 \cdot (\sqrt{55.158}) \cdot 177.8 \cdot 1039.0 \\ &= 149.86 \text{ kN} \end{aligned}$$

with no shear reinforcement:

$$\begin{aligned} V_c &= 0.08297 \cdot \beta (\sqrt{f'_c}) \cdot b_v \cdot d_v & (5.8.3.3-3) \\ &= 0.08297 \cdot 0.9118 \cdot (\sqrt{55.158}) \cdot 177.8 \cdot 1039.0 \\ &= 103.8 \text{ kN} \end{aligned}$$

$$V_p = 29.024 \text{ kN}$$

V_s depends upon the reinforcement present.

Maximum Shear Force **Articles 5.8.2.4 and 5.8.3.3**

Maximum shear with no transverse reinforcement:

$$\begin{aligned} V_u &> 0.5 \cdot \phi \cdot (V_c + V_p) & (5.8.2.4-1) \\ &= 0.5 \cdot 0.9 \cdot (103.803 + 29.0241) \\ &= 59.7724 \text{ kN} \end{aligned}$$

$$\begin{aligned} \phi \cdot V_u &> 0.9 \cdot 59.7724 \\ &= 53.7952 \text{ kN} \end{aligned}$$

Maximum value of shear resistance with transverse reinforcement

$$\begin{aligned} V_{n, \max} &= 0.25 \cdot f'_c \cdot b_v \cdot d_v + V_p & (5.8.3.3-2) \\ &= 0.25 \cdot 55.1581 \cdot 177.8 \cdot 1038.96 + 29.0241 \\ &= 2576.32 \text{ kN} \end{aligned}$$

$$\begin{aligned} \phi \cdot V_{n, \max} &= 0.9 \cdot 2576.32 \\ &= 2318.69 \text{ kN} \end{aligned}$$

Transverse Reinforcement Requirements

inclination of the transverse reinforcement, $\alpha = 90.0^\circ$

minimum yield strength of transverse rft $f_y = 420.0 \text{ MPa}$

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Minimum Transverse Reinforcement (article 5.8.2.5):

$$\frac{A_v}{s} \geq \frac{0.083 \cdot \sqrt{f'_c} \cdot b_v}{f_y}$$

$$= 0.083 \cdot \sqrt{55.1581} \cdot 177.8 / 420.0$$

$$= 0.2610 \text{ mm}^2/\text{mm}$$

Shear resistance (article 5.8.3.3) with minimum reinforcement (article 5.8.3.3):

$$V_n = V_c + V_s + V_p$$

$$V_s = A_v / s \cdot f_y \cdot d_v \cdot (\cot(\theta) + \cot(\alpha)) \cdot \sin(\alpha) \quad (5.8.3.3-4)$$

$$V_{s,min} = 0.26105 \cdot 420.0 \cdot 1038.96 \cdot 1.13636$$

$$= 129.449 \text{ kN}$$

therefore,

$$V_{n,min} = 149.868 + 129.449 + 29.0241$$

$$= 308.341 \text{ kN}$$

$$\phi \cdot V_{n,min} = 0.9 \cdot 308.341$$

$$= 277.507 \text{ kN}$$

Additional transverse reinforcement for shear (article 5.8.3.3):

V_u is greater than $\phi V_{n,min}$, therefore additional transverse reinforcement is required.

contribution to shear strength from shear rft,

$$V_s = V_u / \phi - (V_c + V_p)$$

$$= 1197.58 / 0.9 - (149.868 + 29.0241)$$

$$= 1151.75 \text{ kN}$$

from equation 5.8.3.3-4

$$A_v / s = V_s / (f_y \cdot d_v \cdot (\cot(\theta) + \cot(\alpha)) \cdot \sin(\alpha))$$

hence,

$$A_v / s = 1151.75 / (420.0 \cdot 1038.96 \cdot 1.13636)$$

$$= 2.32271 \text{ mm}^2/\text{mm}$$

Link arrangement:

size	diameter mm	Maximum spacing mm	
		2 legs	4 legs
10	11.3	86.3539	172.708
15	16.0	173.127	346.254
20	19.5	257.155	514.309
25	25.2	429.463	858.927

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Maximum spacing (article 5.8.2.7):

$$\begin{aligned} 0.125 \cdot f'_c &= 0.125 \cdot 55.1581 \\ &= 6.8948 \text{ MPa} \end{aligned}$$

$$\begin{aligned} v_u &= \frac{V_u - \phi \cdot V_p}{\phi \cdot b_v \cdot d_v} \quad \text{Eqn. 5.8.2.9-1} \\ &= \frac{1197.58 - 0.9 \cdot 29.0241}{0.9 \cdot 177.8 \cdot 1038.96} \\ &= 7.04617 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{therefore, } v_u &\geq 0.125 \cdot f'_c \\ s_{max} &= 0.4 \cdot d_v \leq 0.3048 \\ &= 0.4 \cdot 1038.96 \\ &= 415.584 \text{ mm} \end{aligned}$$

hence maximum permissible spacing = 304.8 mm

Longitudinal Reinforcement - Article 5.8.3.5

Non-prestressed reinforcing steel:

$$\begin{aligned} \text{Area on flexural tensile side } A_s &= 0.0 \text{ mm}^2 \\ \text{tensile capacity} &= 0.0 \text{ kN} \end{aligned}$$

Prestressing steel:

$$\begin{aligned} \text{Area on flexural tensile side } A_{ps} &= 1579.36 \text{ mm}^2 \\ \text{tensile strength } f_{pu} &= 1861.58 \text{ MPa} \\ \text{allowance for development} &= 0.26246 \\ \text{tensile capacity} &= 0.26246 \cdot 1579.36 \cdot 1861.58 \\ &= 771.683 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Total tensile capacity} &= 0.0 + 771.683 \\ &= 771.683 \text{ kN} \end{aligned}$$

Equation 5.8.3.5-1 right hand side:

$$\begin{aligned} M_u / (d_v \cdot \phi) &= 2064.61 / (1.03896 \cdot 1.0) \\ &= 1987.19 \text{ kN} \\ 0.5 \cdot N_u / \phi &= 0.5 \cdot 0.0 / 0.75 \\ &= 0.0 \text{ kN} \\ V_u / \phi - 0.5 \cdot V_s - V_p &= 1197.58 / 0.9 - 0.5 \cdot 1151.75 - 29.0241 \\ &= 725.744 \\ * \cot(\theta) &= 725.744 \cdot 1.13636 \\ &= 824.705 \text{ kN} \end{aligned}$$

where V_s is taken from equation 5.8.3.3-4 but not greater than V_u / ϕ

$$\begin{aligned} V_u / \phi &= 1197.58 / 0.9 \\ &= 1330.64 \text{ kN} \\ A_v / s \cdot f_y \cdot d_v \cdot \cot(\theta) &= 0.00232 \cdot 420.0 \cdot 1.03896 \cdot 1.13636 \\ &= 1151.75 \text{ kN} \end{aligned}$$

$$1987.19 + 0.0 + 824.705 = 2811.9 \text{ kN}$$

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which is greater than 771.683, so Equation 1 is not satisfied, therefore additional longitudinal reinforcement is required.

Area of fully developed non-prestressed reinforcing steel required on flexural tension side of member is given by:

$$A_s \cdot f_y = 2811.9 - 771.683 = 2040.22 \text{ kN}$$

$$\begin{aligned} \text{hence additional area required,} \\ &= 2040.22 / 420.0 \\ &= 4857.66 \text{ mm}^2 \end{aligned}$$

Summary of link requirements along the beam:

Preferred size of links: 11.3 mm Bar #: 10

dimension from left beam end m	A_v / s mm ² /mm	Spacing in mm with preferred link size ^[1]
0.2	0.79613	251.937
0.2787	0.77705	258.123
0.48068	0.72763	275.654
0.762	0.63692	300.0
1.71136	0.53740	300.0
2.94205	0.37830	300.0
4.17273	0.53517	300.0
5.40341	0.44931	300.0
6.63409	0.26087	300.0
7.86478	0.26087	300.0
9.09546	0.26087	300.0
9.25	0.26087	300.0
10.012	0.26087	300.0
10.3261	0.26087	300.0
11.5568	0.26087	300.0
12.7875	0.26087	300.0
13.8636	0.26087	300.0
14.0182	0.26087	300.0
14.6256	0.26087	300.0
15.2489	0.26087	300.0
15.4091	0.26087	300.0
15.4091	0.26087	300.0
16.4796	0.26087	300.0
17.7102	0.29572	300.0
18.9409	0.45711	300.0
18.9409	0.45717	300.0
20.1716	0.56171	300.0
21.4023	0.70957	282.669
22.3516	1.81122	110.74
22.633	2.3067	86.9532
22.8349	2.69441	74.4411
22.9136	2.32271	86.3539

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[1] Based on 2 legs (double this value if using 4 legs)

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Transverse Live Load Distribution Factor Calculations

Approximate Methods of Analysis - Article 4.6.2 **Distribution Of Live Loads Per Lane** **Article 4.6.2.2**

Check general conditions - 4.6.2.2.1

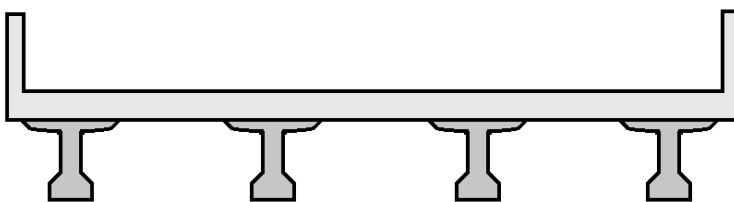
- width of deck is constant 0.K.
- no of beams is 11 0.K.
- all beams are parallel and of approximately the same stiffness 0.K.
- roadway part of overhang, d_e , is 1.13477m 0.K.
- curvature in plan is less than the limit specified in Article 4.6.1.2 0.K.
- Cross-section is consistent with one of the cross-sections shown in Table 1 0.K.

Maximum Number of Design Lanes - 3.6.1.1.1

Clear roadway width between curbs / barriers $w = 20.3206\text{m}$
 $w/3.6576 = 20.3206/3.6576$
 $= 5.55571$

number of design lanes = 5

Cross-section is type (k) from Table 4.6.2.2.1-1



Distribution factors for Moment

Beam is an exterior beam

For two or more design lanes loaded, first calculate the distribution factors for an interior beam

Spacing of beams,	$S = 1.8051 \text{ m}$
Span of beam,	$L = 24.6136 \text{ m}$
Thickness of slab,	$t_s = 300.0 \text{ mm}$

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Longitudinal stiffness parameter, K_g :

modulus of elasticity of beam material, $E_b = 37.3865 \text{ kN/mm}^2$
modulus of elasticity of deck material, $E_d = 29.5566 \text{ kN/mm}^2$

$$\begin{aligned} n &= E_b/E_d && (4.6.2.2.1-2) \\ &= 37.3865/29.5566 \\ &= 1.26491 \end{aligned}$$

area of non-composite beam, $A = 3.61\text{E}5 \text{ mm}^2$
moment of inertia of non-composite beam, $I = 5.22\text{E}10 \text{ mm}^4$
height to center of gravity of basic beam = 514.946 mm
height to center of gravity of deck = 1293.0 mm
distance between centers of gravity, $e_g = 778.054 \text{ mm}$

$$\begin{aligned} \text{hence, longitudinal stiffness parameter, } K_g &= n \cdot (I + A \cdot e_g^2) && (4.6.2.2.1-1) \\ &= 1.26491 \cdot (5.22\text{E}10 + 3.61\text{E}5 \cdot 778.054^2) \\ &= 3.42\text{E}11 \text{ mm}^4 \end{aligned}$$

With one design lane loaded:

$$\begin{aligned} DFM_1 &\text{ from lever rule for external beam} \\ &= 0.94124 \end{aligned}$$

With two or more design lanes loaded:

$$\begin{aligned} DFM_2 &= 0.075 + \left[\frac{S}{2.9} \right]^{0.6} \left[\frac{S}{L} \right]^{0.2} \left[\frac{K_g}{1. \text{E}3 \cdot L \cdot t_s^3} \right]^{0.1} \\ &= 0.075 + (1.8051/2.8956)^{0.6} \\ &\quad \cdot (1.8051/24.6136)^{0.2} \\ &\quad \cdot (3.42\text{E}11 / (1000.0 \cdot 24.6136 \cdot 300.0^3))^{0.1} \\ &= 0.49295 \end{aligned}$$

Since this is an exterior beam, the correction factor, e , must be applied, where e is given in Table 4.6.2.2.2d-1 as:

$$\begin{aligned} e &= 0.77 + d_e/2743.2 \\ &= 0.77 + 1134.77/2743.2 \\ &= 1.17912 \end{aligned}$$

hence,

$$\begin{aligned} DFM_2 &= 1.17912 \cdot 0.49295 \\ &= 0.58124 \end{aligned}$$

The distribution factor with 1 lane loaded is critical

$$DFM = 0.94124$$

Distribution factors for Shear

Beam is an exterior beam

First calculate the distribution factors for an interior beam

$$\text{Spacing of beams, } S = 1.8051 \text{ m}$$

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With one design lane loaded:

$$DFV_1 \text{ from lever rule for external beam} \\ = 0.94124$$

With two or more design lanes loaded:

$$DFV_2 = 0.2 + \frac{S}{3.6576} - \left[\frac{S}{10.67} \right]^{2.0} \\ = 0.2 + 1.8051/3.6576 - (1.8051/10.668)^2 \\ = 0.66489$$

Since this is an exterior beam, the correction factor, e, must be applied, where e is given in Table 4.6.2.2.3b-1 as:

$$e = 0.6 + d_e / 3048.0 \\ = 0.6 + 1134.77/3048.0 \\ = 0.9723$$

hence,

$$DFV_2 = 0.9723 * 0.66489 \\ = 0.64647$$

The distribution factor with 1 lane loaded is critical

$$DFV = 0.94124$$

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RIGID STRUCTURE REACTIONS FOR EXTERIOR BEAMS

Article 4.6.2.2d

Since this is an exterior beam, and diaphragms or cross frames are present, the reaction arising from rigid cross section deflection and rotation must be considered.

From formula C4.6.2.2.2d-1:

$$R = \frac{N_l}{N_b} + \frac{X_{ext} \cdot \Sigma e}{\Sigma x^2}$$

where,

R = reaction on exterior beam in terms of lanes
 N_l = number of loaded lanes under consideration
 e = eccentricity of lane center from C of G of girders
 x = horizontal distance from C of G of girders to each girder
 X_{ext} = value of x for exterior girder
 N_b = number of beams or girders

$$N_b = 11$$

$$\begin{aligned} X_{ext} &= 0.5 \cdot (S \cdot (N_b - 1)) \\ &= 0.5 \cdot (1805.1 \cdot (11 - 1)) \\ &= 9025.52 \text{ mm} \end{aligned}$$

Girder	x	x^2
1	9025.52	8.146E7
2	7220.41	5.213E7
3	5415.31	2.933E7
4	3610.21	1.303E7
5	1805.1	3.258E6
6	0.0	0.0
7	-1805.1	3.258E6
8	-3610.2	1.303E7
9	-5415.3	2.933E7
10	-7220.4	5.213E7
11	-9025.5	8.146E7
TOTAL		3.584E8 = Σx^2 mm ²

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For 1 lane loaded,

$$\begin{aligned}e &= 8636.29 & \Sigma e &= 8636.29 \\R &= 1/11 + 9025.52 \cdot 8636.29 / 3.584E8 \\&= 0.30838 \\m &= 1.2 \\m.R &= 1.2 \cdot 0.30838 \\&= 0.37005\end{aligned}$$

For 2 lanes loaded,

$$\begin{aligned}e &= 4978.69 & \Sigma e &= 13615.0 \\R &= 2/11 + 9025.52 \cdot 13615.0 / 3.584E8 \\&= 0.52465 \\m &= 1.0 \\m.R &= 1.0 \cdot 0.52465 \\&= 0.52465\end{aligned}$$

For 3 lanes loaded,

$$\begin{aligned}e &= 1321.09 & \Sigma e &= 14936.1 \\R &= 3/11 + 9025.52 \cdot 14936.1 / 3.584E8 \\&= 0.64883 \\m &= 0.85 \\m.R &= 0.85 \cdot 0.64883 \\&= 0.55150\end{aligned}$$

For 4 lanes loaded,

$$\begin{aligned}e &= -2336.5 & \Sigma e &= 12599.6 \\R &= 4/11 + 9025.52 \cdot 12599.6 / 3.584E8 \\&= 0.68090 \\m &= 0.65 \\m.R &= 0.65 \cdot 0.68090 \\&= 0.44259\end{aligned}$$

For 5 lanes loaded,

$$\begin{aligned}e &= -5994.1 & \Sigma e &= 6605.44 \\R &= 5/11 + 9025.52 \cdot 6605.44 / 3.584E8 \\&= 0.62087 \\m &= 0.65 \\m.R &= 0.65 \cdot 0.62087 \\&= 0.40357\end{aligned}$$

CALCULATION OF DISTRIBUTION FACTOR USING THE LEVER RULE

Spacing of beams, $S = 1.8051$ m
Roadway overhang, $d_e = 1.13477$ m
curb/barrier to outermost wheel (min) $= 0.6096$ m
hence,

$$\begin{aligned}\text{max possible wheel lines, } n_p &= \frac{1.8051 + 1.13477 - 0.6096}{1.8288} + 1 \\&= 2\end{aligned}$$

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Exterior beam with one lane loaded:

The furthest wheel is 0.6096 m from the curb or barrier
girder line to furthest wheel $= 1.8051 + 1.13477 - 0.6096$
 $= 2.33027$ m

moments about inner girder:

$$P \cdot 2.33027 + P \cdot 0.50147 = R_a \cdot 1.8051$$

where P is the wheel load, and R_a is the reaction at the exterior girder.

hence,

$$\begin{aligned} R_a &= 2831.75 / 1805.1 \text{ wheels} \\ &= 1.56875 \text{ wheels} \\ &= 0.78437 \text{ lanes/beam} \end{aligned}$$

From Article 3.6.1.1.2 of AASHTO LRFD the multiple lane factor for one lane loaded is 1.2.

$$\begin{aligned} \text{hence distribution factor} &= 0.78437 \cdot 1.2 \\ &= 0.94124 \end{aligned}$$

Distribution factor for Fatigue

Article 3.6.1.4.3b - For fatigue loads, the load distribution is as specified in Article 4.6.2 with the distribution factor for one one traffic lane being used.

Article 3.6.1.1.2 - the multiple presence factor is not applied to the fatigue limit state, and therefore must be removed from the single lane distribution factor value evaluated above

$$\begin{aligned} DFV_f &= 0.94124 / 1.2 \\ &= 0.78437 \end{aligned}$$

SUMMARY of distribution factors

	One Design Lane Loaded	Two or More Design Lanes Loaded
Moments	0.94124	0.58124
Shears	0.94124	0.64647
Fatigue	0.78437	

Check Range of Applicability for Moments

$$\begin{aligned} S &= 1.8051 & 1.0668 \leq S \leq 4.8768 \\ t_s &= 300.0 & 114.3 \leq t_s \leq 304.8 \\ L &= 24.6136 & 6.096 \leq L \leq 73.152 \\ d_e &= 1.13477 & -0.3048 \leq d_e \leq 1.6764 \\ N_b &= 11 & N_b \geq 4 \\ & & \text{or } N_b = 3 \text{ with lever rule check} \end{aligned}$$

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Check Range of Applicability for Negative Moments near Supports

Applicable Range:
 $L = 23.514$ $6.096 \leq L \leq 73.152$

Check Range of Applicability for Shear

Applicable ranges are as for Moments, and in addition

Applicable Range:
 $K_g = 1.425E5$ $4.162E9 \leq K_g \leq 2.91E12$

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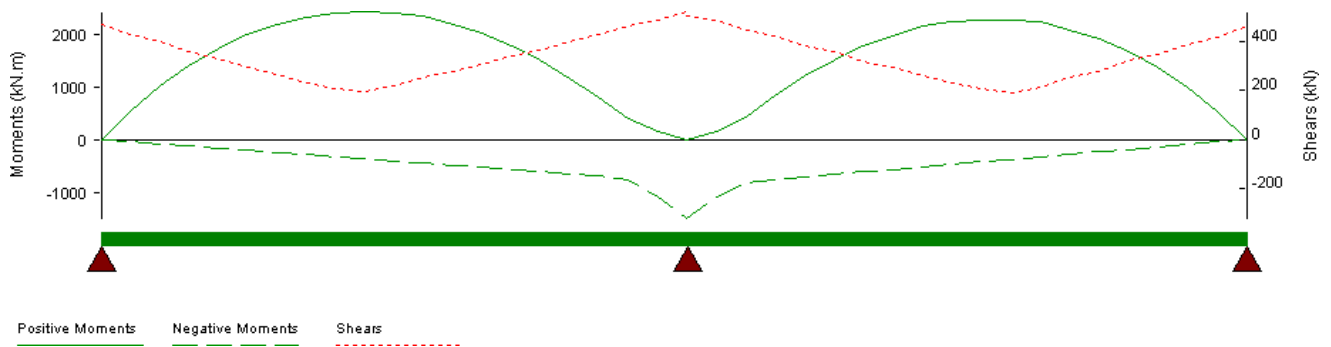
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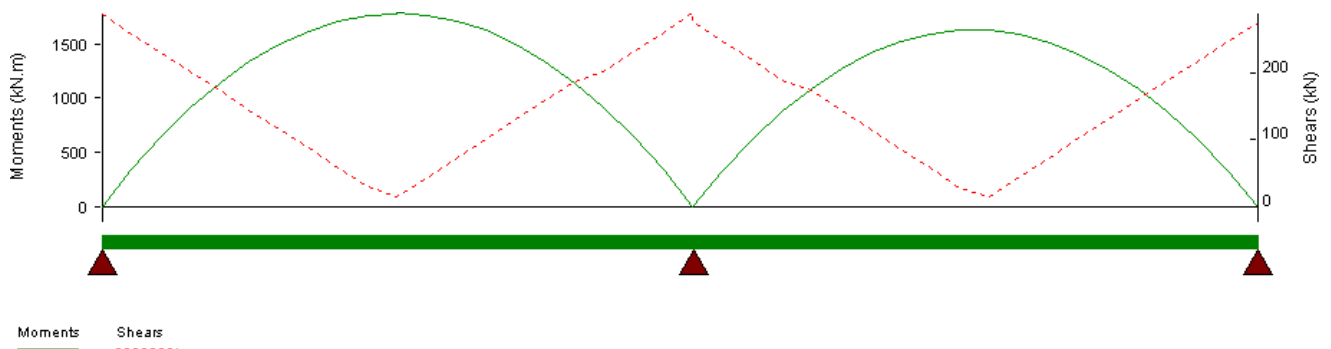
Analysis Load Envelopes

Live Load Envelope for Strength I and Service



The above envelope excludes the effects of transverse distribution.

Moments and Shears due to Dead Load



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Analytical Model Data



MATERIALS

MP1: C35 Es 29.6

Type: Concrete - Parabola-Rectangle

Compressive strength f'_c : 34.473785 MPa

Strength LS stress/strain curve parameters:
slope at start of parabola: 36.373012 kN/mm²
strain at end of parabola: 0.0016136
stress at end of parabola: 29.30266 MPa
maximum strain: 0.003

Elastic modulus - E_c : 29.55662 kN/mm²
Elastic modulus - long term: 14.77831 kN/mm²
Shear modulus: 12.315258 kN/mm²
Poisson's ratio: 0.2

Compressive Stress limit factor: 0.6000000 x f'_c
Modulus of Rupture: -3.700114 MPa
Coefficient of thermal expansion: 0.0000108 /°C
Density: 23.563114 kN/m³

MP2: C56 Es 37.4

Type: Concrete - Parabola-Rectangle

Compressive strength f'_c : 55.158059 MPa

Strength LS stress/strain curve parameters:
slope at start of parabola: 46.008624 kN/mm²
strain at end of parabola: 0.0020411
stress at end of parabola: 46.884254 MPa
maximum strain: 0.003

Elastic modulus - E_c : 37.386496 kN/mm²
Elastic modulus - long term: 18.693248 kN/mm²
Shear modulus: 15.577706 kN/mm²
Poisson's ratio: 0.2

Compressive Stress limit factor: 0.6000000 x f'_c
Modulus of Rupture: -4.680315 MPa
Coefficient of thermal expansion: 0.0000108 /°C
Density: 23.563114 kN/m³

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MP3: C42 Es 32.4

Type: Concrete - Parabola-Rectangle

Compressive strength f'_c : 41.368543 MPa

Strength LS stress/strain curve parameters:
slope at start of parabola: 39.844636 kN/mm²
strain at end of parabola: 0.0017677
stress at end of parabola: 35.163191 MPa
maximum strain: 0.003

Elastic modulus - E_c : 32.377654 kN/mm²

Elastic modulus - long term: 16.188827 kN/mm²

Shear modulus: 13.490689 kN/mm²

Poisson's ratio: 0.2

Compressive Stress limit factor: 0.6000000 $\times f'_c$

Modulus of Rupture: -4.053272 MPa

Coefficient of thermal expansion: 0.0000108 /°C

Density: 23.563114 kN/m³

MP4: Grade 1862 E 197.0

Type: Prestressing Steel

Tensile strength f_{pu} : 1861.5845 MPa

Strength LS stress/strain curve parameters:

	strain	stress MPa
Tension		
full yield:	-0.014442	-1860.0
start yield:	-0.007553	-1488.0

Elastic modulus E_p : 197.0 kN/mm²

Shear modulus: 75.769232 kN/mm²

Yield strength f_{py} : 90.0% of f_{pu}

Initial Prestress force: 75.0% of f_{pu}

Relaxation type: Low Relaxation

Time from stressing to transfer: 0.0 days

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MP5: Grade 420 E 200.0
Type: Reinforcing Steel

Yield strength f_y : 420.0 MPa

Strength LS stress/strain curve parameters:

	strain	stress MPa
Tension		
full yield:	-0.0041	-420.0
start yield:	-0.00168	-336.0
Compression		
start yield:	0.00168	336.0
full yield:	0.002	347.10744

Elastic modulus E_s : 200.0 kN/mm²

Shear modulus: 76.92308 kN/mm²

Max. stress limitation factor: $0.6000000 \times f_y$

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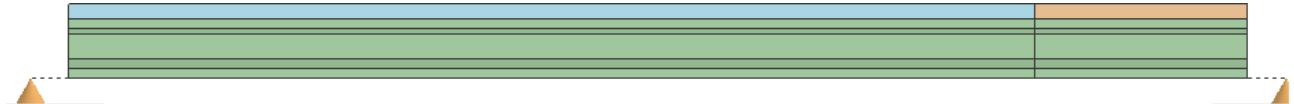
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DESIGN BEAM - SB1: PRE-TENSIONED PRESTRESSED



BEAM DEFINITION

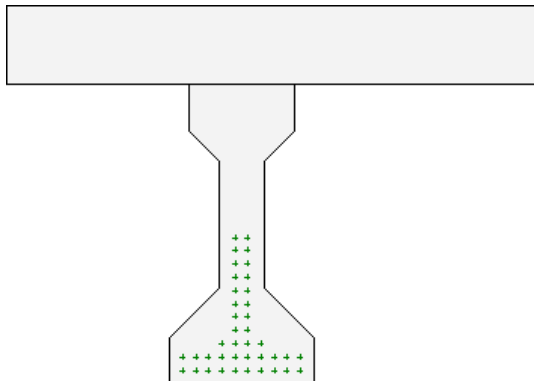
AASHTO LRFD Pre-tensioned Prestressed Beam

Total length of pre-tensioned beam: 23.1136 m
Distance from left support to beam end face: -0.75 m
Distance from right support to beam end face: -0.75 m
Total distance between supports: 24.6136 m

Beam section varies along length of beam.

Number of different sections : 2
No. of longitudinal construction stages : 2
No. of superimposed construction stages : 1

Section 1



Precast beam is standard section: GIRDER III
Property set for precast concrete -
at transfer: MP3: C42 Es 32.4
in final structure: MP2: C56 Es 37.4

Cast In Place concrete - stage 1A:
C.I.P. is from standard section:
- width: 2.03732 m
- depth: 0.3 m
Property set: MP1: C35 Es 29.6

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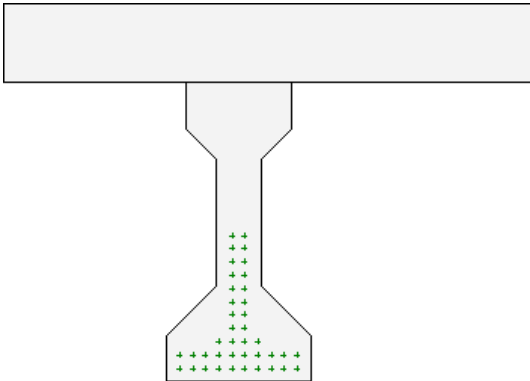
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Section 2



Precast beam is standard section: GIRDER III
Property set for precast concrete -
at transfer: MP3: C42 Es 32.4
in final structure: MP2: C56 Es 37.4

Cast In Place concrete - stage 1B:
C.I.P. is from standard section:
- width: 2.03732 m
- depth: 0.3 m
Property set: MP1: C35 Es 29.6

Tendons

x-y	coordinates	area	Property	K	d_b	type
	mm	mm ²	ref		mm	
-228.6	50.8	98.71	MP4	60	12.7	Full stress
-177.8	50.8	98.71	MP4	60	12.7	Full stress
-127.0	50.8	98.71	MP4	60	12.7	Full stress
-76.2	50.8	98.71	MP4	60	12.7	Full stress
-25.4	50.8	98.71	MP4	60	12.7	Harped
25.4	50.8	98.71	MP4	60	12.7	Harped
76.2	50.8	98.71	MP4	60	12.7	Full stress
127.0	50.8	98.71	MP4	60	12.7	Full stress
177.8	50.8	98.71	MP4	60	12.7	Full stress
228.6	50.8	98.71	MP4	60	12.7	Full stress
-228.6	101.6	98.71	MP4	60	12.7	Full stress
-177.8	101.6	98.71	MP4	60	12.7	Full stress
-127.0	101.6	98.71	MP4	60	12.7	Full stress
-76.2	101.6	98.71	MP4	60	12.7	Full stress
-25.4	101.6	98.71	MP4	60	12.7	Harped
25.4	101.6	98.71	MP4	60	12.7	Harped
76.2	101.6	98.71	MP4	60	12.7	Full stress
127.0	101.6	98.71	MP4	60	12.7	Full stress

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177.8	101.6	98.71	MP4	60	12.7 Full stress
228.6	101.6	98.71	MP4	60	12.7 Full stress
-76.2	152.4	98.71	MP4	60	12.7 Full stress
-25.4	152.4	98.71	MP4	60	12.7 Harped
25.4	152.4	98.71	MP4	60	12.7 Harped
76.2	152.4	98.71	MP4	60	12.7 Full stress
-25.4	203.2	98.71	MP4	60	12.7 Harped
25.4	203.2	98.71	MP4	60	12.7 Harped
-25.4	254.0	98.71	MP4	60	12.7 Harped
25.4	254.0	98.71	MP4	60	12.7 Harped
-25.4	304.8	98.71	MP4	60	12.7 Harped
25.4	304.8	98.71	MP4	60	12.7 Harped
-25.4	355.6	98.71	MP4	60	12.7 Harped
25.4	355.6	98.71	MP4	60	12.7 Harped
-25.4	406.4	98.71	MP4	60	12.7 Harped
25.4	406.4	98.71	MP4	60	12.7 Harped
-25.4	457.2	98.71	MP4	60	12.7 Harped
25.4	457.2	98.71	MP4	60	12.7 Harped
-25.4	508.0	98.71	MP4	60	12.7 Harped
25.4	508.0	98.71	MP4	60	12.7 Harped
-25.4	558.8	98.71	MP4	60	12.7 Harped
25.4	558.8	98.71	MP4	60	12.7 Harped

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Deflected Tendons

x-y coordinates			location		exit height	
mm			(m)		(mm)	
		deflection angle (°)	left	right	left	right
-25.4	50.8	3.30762	9.25	13.8636	585.386	585.386
25.4	50.8	3.30762	9.25	13.8636	585.386	585.386
-25.4	101.6	3.30762	9.25	13.8636	636.186	636.186
25.4	101.6	3.30762	9.25	13.8636	636.186	636.186
-25.4	152.4	3.30762	9.25	13.8636	686.986	686.986
25.4	152.4	3.30762	9.25	13.8636	686.986	686.986
-25.4	203.2	3.30762	9.25	13.8636	737.786	737.786
25.4	203.2	3.30762	9.25	13.8636	737.786	737.786
-25.4	254.0	3.30762	9.25	13.8636	788.586	788.586
25.4	254.0	3.30762	9.25	13.8636	788.586	788.586
-25.4	304.8	3.30762	9.25	13.8636	839.386	839.386
25.4	304.8	3.30762	9.25	13.8636	839.386	839.386
-25.4	355.6	3.30762	9.25	13.8636	890.186	890.186
25.4	355.6	3.30762	9.25	13.8636	890.186	890.186
-25.4	406.4	3.30762	9.25	13.8636	940.986	940.986
25.4	406.4	3.30762	9.25	13.8636	940.986	940.986
-25.4	457.2	3.30762	9.25	13.8636	991.786	991.786
25.4	457.2	3.30762	9.25	13.8636	991.786	991.786
-25.4	508.0	3.30762	9.25	13.8636	1042.59	1042.59
25.4	508.0	3.30762	9.25	13.8636	1042.59	1042.59
-25.4	558.8	3.30762	9.25	13.8636	1093.39	1093.39
25.4	558.8	3.30762	9.25	13.8636	1093.39	1093.39

Reinforcement

x-y coordinates		diameter	Property	Start	End	Length
mm		mm	ref	m	m	m
1062.01	1380.4	25.2	MP5	15.4091	23.1136	7.70455
916.486	1380.4	25.2	MP5	15.4091	23.1136	7.70455
770.963	1380.4	25.2	MP5	15.4091	23.1136	7.70455
625.44	1380.4	25.2	MP5	15.4091	23.1136	7.70455
479.917	1380.4	25.2	MP5	15.4091	23.1136	7.70455
334.394	1380.4	25.2	MP5	15.4091	23.1136	7.70455
188.871	1380.4	25.2	MP5	15.4091	23.1136	7.70455
43.3481	1380.4	25.2	MP5	15.4091	23.1136	7.70455
-102.17	1380.4	25.2	MP5	15.4091	23.1136	7.70455
-247.7	1380.4	25.2	MP5	15.4091	23.1136	7.70455
-393.22	1380.4	25.2	MP5	15.4091	23.1136	7.70455
-538.74	1380.4	25.2	MP5	15.4091	23.1136	7.70455
-684.27	1380.4	25.2	MP5	15.4091	23.1136	7.70455
-829.79	1380.4	25.2	MP5	15.4091	23.1136	7.70455

Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

Location of sections

Position along span from left support: dimension (m) proportion		Section	
0.0	0.0	1	Section 1
18.940918	0.819	1	Section 1
18.940918	0.819	2	Section 2
23.113647	1.0	2	Section 2

PRE-TENSIONED BEAM LOADING DATA

Approximate Methods of Analysis are used - Article 4.6.2

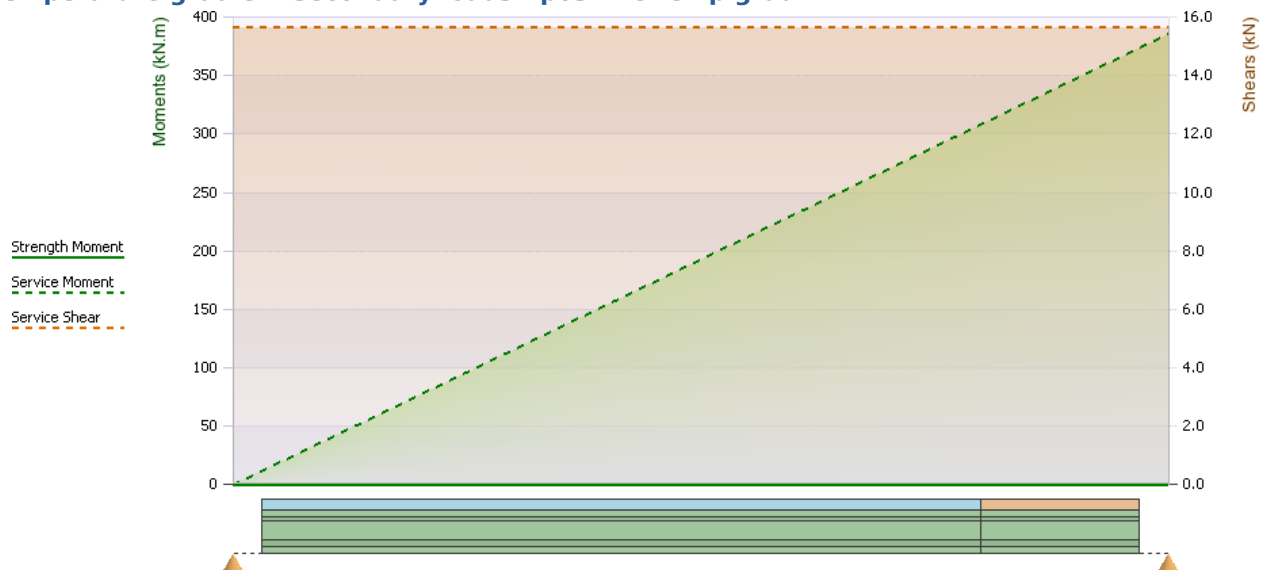
Live Load Distribution Factor for +ve Moment = 0.94124 lanes/beam

Live Load Distribution Factor for -ve Moment = 0.94124 lanes/beam

Live Load Distribution Factor for Shear = 0.94124 lanes/beam

Live Load Distribution Factor for Fatigue = 0.78437 lanes/beam

Temperature gradient secondary loads - positive temp grad



Loading is defined for the distance between supports

ASCENT
630 Peter Jefferson Parkway, Suite 175, Charlottesville, VA
22911



Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

Span Location (from left support)		Moment		Shear		Axial	
		kN.m		kN		kN	
dim (m)	pro	Strength	Service	Strength	Service	Strength	Service
0.0	0.0	0.0	0.0	0.0	15.6548	0.0	0.0
1.2306823	0.05	0.0	19.265	0.0	15.6548	0.0	0.0
2.4613647	0.1	0.0	38.5311	0.0	15.6562	0.0	0.0
3.692047	0.15	0.0	57.8006	0.0	15.6616	0.0	0.0
4.9227294	0.2	0.0	77.0799	0.0	15.6544	0.0	0.0
6.1534117	0.25	0.0	96.3319	0.0	15.6552	0.0	0.0
7.384094	0.3	0.0	115.613	0.0	15.6632	0.0	0.0
8.6147764	0.35	0.0	134.885	0.0	15.6536	0.0	0.0
9.8454587	0.4	0.0	154.142	0.0	15.652	0.0	0.0
11.076141	0.45	0.0	173.41	0.0	15.6679	0.0	0.0
12.306823	0.5	0.0	192.707	0.0	15.6711	0.0	0.0
13.537506	0.55	0.0	211.982	0.0	15.6616	0.0	0.0
14.768188	0.6	0.0	231.256	0.0	15.6624	0.0	0.0
15.99887	0.65	0.0	250.533	0.0	15.6663	0.0	0.0
17.229553	0.7	0.0	269.816	0.0	15.6639	0.0	0.0
18.460235	0.75	0.0	289.088	0.0	15.6711	0.0	0.0
19.690917	0.8	0.0	308.389	0.0	15.6778	0.0	0.0
20.9216	0.85	0.0	327.677	0.0	15.6749	0.0	0.0
22.152282	0.9	0.0	346.97	0.0	15.6775	0.0	0.0
23.382964	0.95	0.0	366.265	0.0	15.6776	0.0	0.0
24.613647	1.0	0.0	385.558	0.0	15.6776	0.0	0.0

These loads are transferred from the following analysis run:

Location: Span 1

Analysis time: 10/27/2016 15:48:35

Analysis Loadcase - Linebeam with Temperature or Shrinkage
- Factor for Strength: 0.0 Service: 0.5

Job: Utah County Development

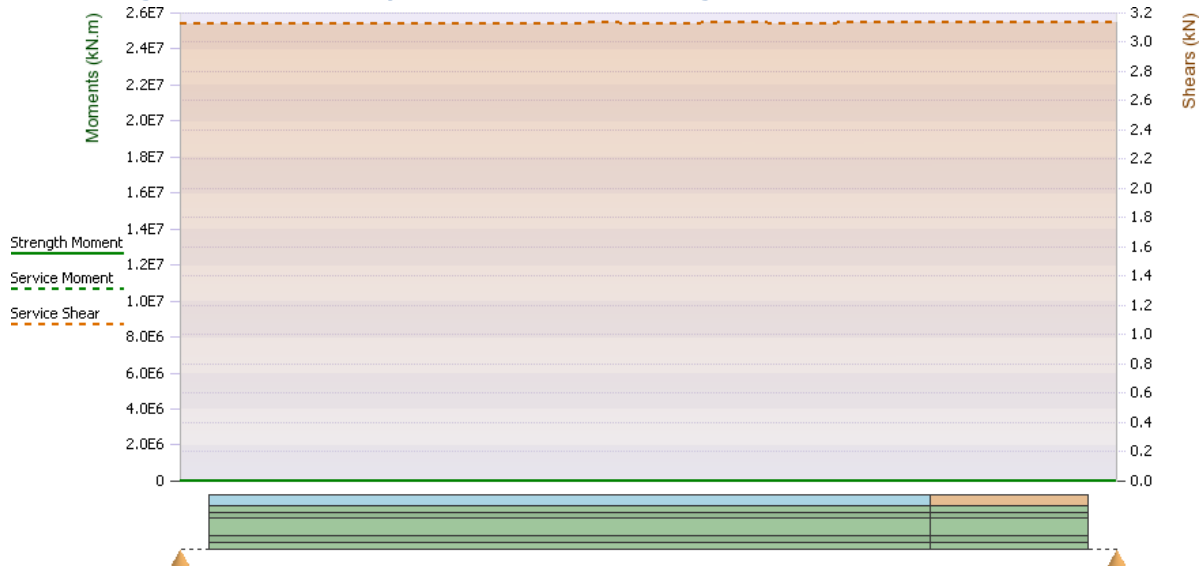
Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

Temperature gradient secondary loads - reverse temp grad



Loading is defined for the distance between supports

Span Location (from left support)		Moment		Shear		Axial	
		kN.m		kN		kN	
dim (m)	pro	Strength	Service	Strength	Service	Strength	Service
0.0	0.0	0.0	1.55E-4	0.0	3.13105	0.0	0.0
1.2306823	0.05	0.0	-3.8524	0.0	3.13105	0.0	0.0
2.4613647	0.1	0.0	-7.7065	0.0	3.13165	0.0	0.0
3.692047	0.15	0.0	-11.561	0.0	3.1318	0.0	0.0
4.9227294	0.2	0.0	-15.415	0.0	3.1312	0.0	0.0
6.1534117	0.25	0.0	-19.268	0.0	3.1318	0.0	0.0
7.384094	0.3	0.0	-23.124	0.0	3.13081	0.0	0.0
8.6147764	0.35	0.0	-26.974	0.0	3.13041	0.0	0.0
9.8454587	0.4	0.0	-30.829	0.0	3.13279	0.0	0.0
11.076141	0.45	0.0	-34.685	0.0	3.13319	0.0	0.0
12.306823	0.5	0.0	-38.54	0.0	3.13279	0.0	0.0
13.537506	0.55	0.0	-42.395	0.0	3.13299	0.0	0.0
14.768188	0.6	0.0	-46.252	0.0	3.13358	0.0	0.0
15.99887	0.65	0.0	-50.108	0.0	3.13259	0.0	0.0
17.229553	0.7	0.0	-53.962	0.0	3.13299	0.0	0.0
18.460235	0.75	0.0	-57.82	0.0	3.13438	0.0	0.0
19.690917	0.8	0.0	-61.677	0.0	3.13453	0.0	0.0
20.9216	0.85	0.0	-65.535	0.0	3.13532	0.0	0.0
22.152282	0.9	0.0	-69.394	0.0	3.13568	0.0	0.0
23.382964	0.95	0.0	-73.253	0.0	3.13548	0.0	0.0
24.613647	1.0	0.0	-77.112	0.0	3.13548	0.0	0.0

Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

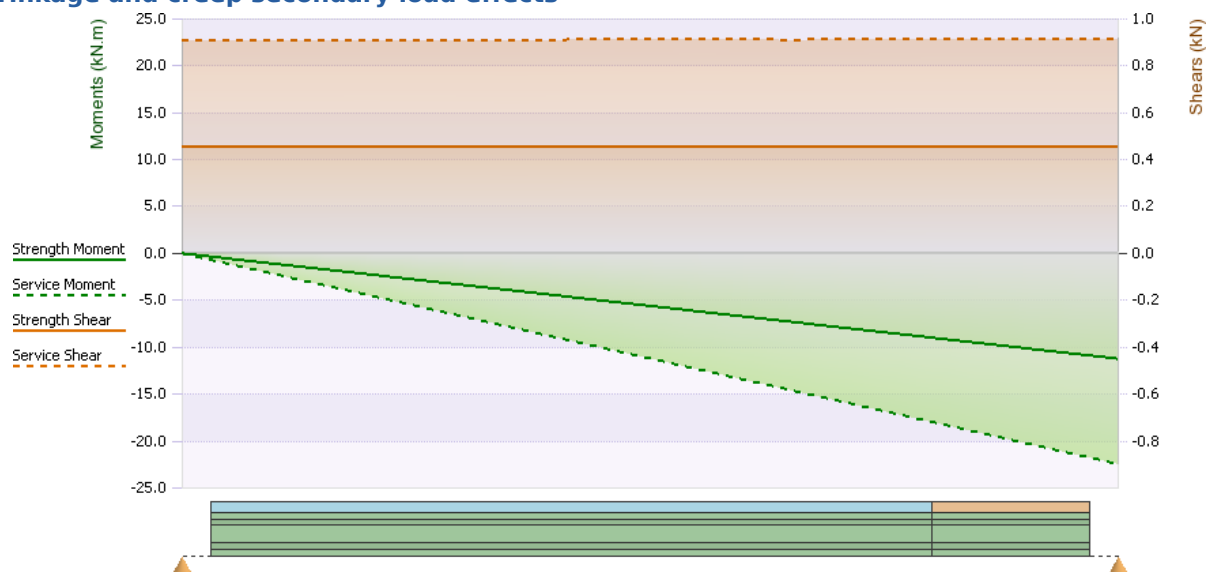
These loads are transferred from the following analysis run:

Location: Span 1

Analysis time: 10/27/2016 15:48:35

Analysis Loadcase - Linebeam with Temperature or Shrinkage
- Factor for Strength: 0.0 Service: 0.5

Shrinkage and creep secondary load effects



Loading is defined for the distance between supports

Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

Span Location (from left support)		Moment		Shear		Axial	
		kN.m		kN		kN	
dim (m)	pro	Strength	Service	Strength	Service	Strength	Service
0.0	0.0	0.0	0.0	0.45501	0.91002	0.0	0.0
1.2306823	0.05	-0.5598	-1.1197	0.45501	0.91002	0.0	0.0
2.4613647	0.1	-1.1199	-2.2399	0.45486	0.90973	0.0	0.0
3.692047	0.15	-1.6794	-3.3589	0.45515	0.91030	0.0	0.0
4.9227294	0.2	-2.2402	-4.4805	0.45546	0.91092	0.0	0.0
6.1534117	0.25	-2.8005	-5.601	0.45535	0.91070	0.0	0.0
7.384094	0.3	-3.361	-6.7221	0.45520	0.91040	0.0	0.0
8.6147764	0.35	-3.9209	-7.8418	0.45446	0.90892	0.0	0.0
9.8454587	0.4	-4.4796	-8.9593	0.45562	0.91125	0.0	0.0
11.076141	0.45	-5.0424	-10.085	0.45661	0.91323	0.0	0.0
12.306823	0.5	-5.6035	-11.207	0.45622	0.91244	0.0	0.0
13.537506	0.55	-6.1653	-12.331	0.45691	0.91382	0.0	0.0
14.768188	0.6	-6.7282	-13.456	0.45634	0.91268	0.0	0.0
15.99887	0.65	-7.2885	-14.577	0.45565	0.9113	0.0	0.0
17.229553	0.7	-7.8497	-15.699	0.45614	0.91229	0.0	0.0
18.460235	0.75	-8.4113	-16.823	0.45685	0.91371	0.0	0.0
19.690917	0.8	-8.9742	-17.948	0.45759	0.91519	0.0	0.0
20.9216	0.85	-9.5376	-19.075	0.45793	0.91586	0.0	0.0
22.152282	0.9	-10.101	-20.203	0.45807	0.91614	0.0	0.0
23.382964	0.95	-10.665	-21.33	0.45806	0.91613	0.0	0.0
24.613647	1.0	-11.229	-22.458	0.45806	0.91613	0.0	0.0

These loads are transferred from the following analysis run:

Location: Span 1

Analysis time: 10/27/2016 15:48:35

Analysis Loadcase - Linebeam with Temperature or Shrinkage
- Factor for Strength: 0.5 Service: 1.0

Settlement of supports

- none defined -

Job: Utah County Development

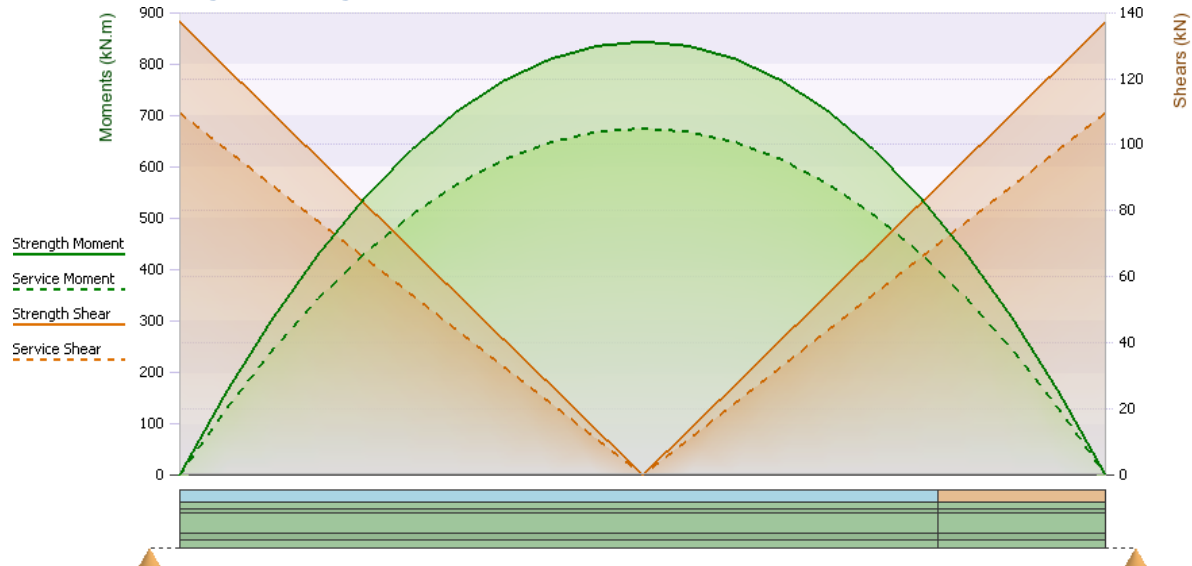
Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

Beam Erection Stage Loading



Loading is defined for the distance between beam end faces

Span Location (from left end)		Moment kN.m		Shear kN		Axial kN	
dim (m)	pro	Strength	Service	Strength	Service	Strength	Service
0.0	0.0	0.0	0.0	137.054	109.643	0.0	0.0
1.1556823	0.05	160.224	128.179	123.343	98.6745	0.0	0.0
2.3113647	0.1	303.574	242.859	109.632	87.7057	0.0	0.0
3.467047	0.15	430.058	344.046	95.9212	76.737	0.0	0.0
4.6227293	0.2	539.658	431.726	82.1907	65.7526	0.0	0.0
5.7784117	0.25	632.363	505.89	68.4603	54.7682	0.0	0.0
6.934094	0.3	708.144	566.515	54.7298	43.7838	0.0	0.0
8.0897763	0.35	767.089	613.671	41.0775	32.862	0.0	0.0
9.2454587	0.4	809.14	647.312	27.5228	22.0182	0.0	0.0
10.401141	0.45	834.628	667.703	13.8118	11.0495	0.0	0.0
11.556823	0.5	843.203	674.562	0.13995	0.11196	0.0	0.0
12.712506	0.55	834.785	667.828	13.6101	10.888	0.0	0.0
13.868188	0.6	809.628	647.703	27.3796	21.9037	0.0	0.0
15.02387	0.65	767.48	613.984	41.1296	32.9037	0.0	0.0
16.179553	0.7	708.437	566.75	54.8601	43.8881	0.0	0.0
17.335235	0.75	632.538	506.031	68.5515	54.8412	0.0	0.0
18.490917	0.8	539.746	431.796	82.2038	65.763	0.0	0.0
19.6466	0.85	430.058	344.046	95.8952	76.7162	0.0	0.0
20.802282	0.9	303.598	242.878	109.626	87.7005	0.0	0.0
21.957964	0.95	160.252	128.202	123.355	98.6838	0.0	0.0
23.113647	1.0	0.0	0.0	137.072	109.658	0.0	0.0

Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

These loads are transferred from the following analysis run:

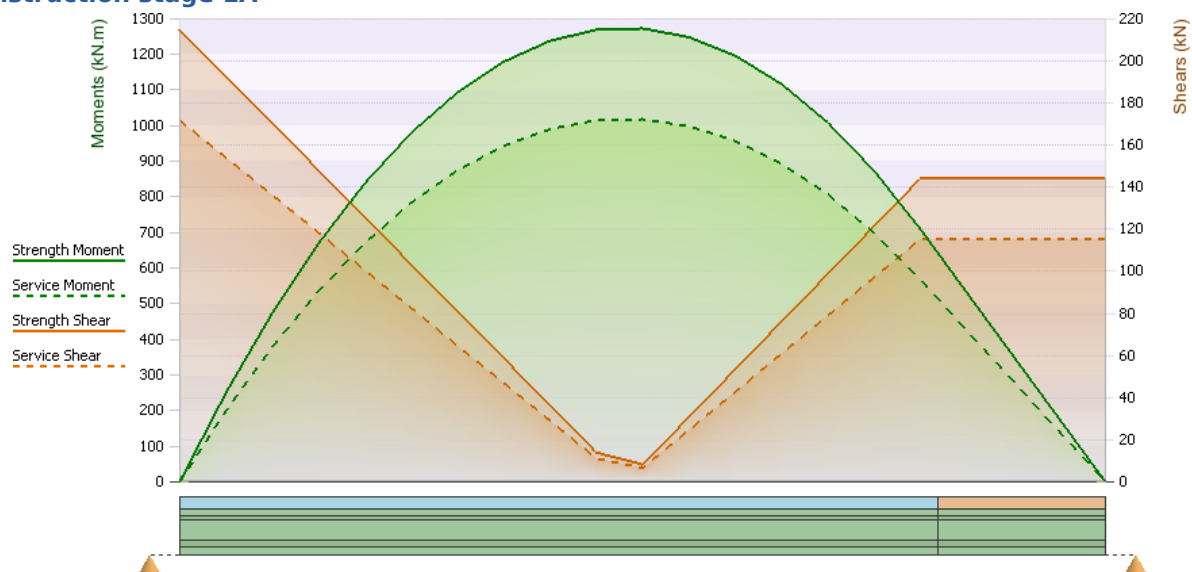
Location: Span 1

Analysis time: 10/27/2016 15:48:35

Analysis Loadcase - Linebeam with Erection of beam

- Factor for Strength: 1.25 Service: 1.0

Construction stage 1A



Loading is defined for the distance between beam end faces

ASCENT
630 Peter Jefferson Parkway, Suite 175, Charlottesville, VA
22911



Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

Span Location (from left end)		Moment		Shear		Axial	
		kN.m		kN		kN	
dim (m)	pro	Strength	Service	Strength	Service	Strength	Service
0.0	0.0	0.0	0.0	214.662	171.73	0.0	0.0
1.1556823	0.05	250.535	200.428	192.487	153.99	0.0	0.0
2.3113647	0.1	473.725	378.98	170.318	136.254	0.0	0.0
3.467047	0.15	669.649	535.719	147.992	118.394	0.0	0.0
4.6227293	0.2	838.122	670.497	125.725	100.58	0.0	0.0
5.7784117	0.25	979.153	783.323	103.321	82.6568	0.0	0.0
6.934094	0.3	1092.7	874.163	80.9561	64.7648	0.0	0.0
8.0897763	0.35	1178.62	942.895	58.8256	47.0605	0.0	0.0
9.2454587	0.4	1237.15	989.72	36.5388	29.2311	0.0	0.0
10.401141	0.45	1268.36	1014.69	14.0958	11.2767	0.0	0.0
11.556823	0.5	1271.95	1017.56	8.38623	6.70898	0.0	0.0
12.712506	0.55	1247.65	998.117	30.8683	24.6947	0.0	0.0
13.868188	0.6	1195.79	956.63	53.5457	42.8365	0.0	0.0
15.02387	0.65	1115.96	892.768	76.223	60.9784	0.0	0.0
16.179553	0.7	1008.3	806.64	98.8223	79.0578	0.0	0.0
17.335235	0.75	872.808	698.246	121.461	97.1685	0.0	0.0
18.490917	0.8	709.346	567.477	144.121	115.297	0.0	0.0
19.6466	0.85	531.904	425.523	144.023	115.219	0.0	0.0
20.802282	0.9	354.619	283.695	144.082	115.266	0.0	0.0
21.957964	0.95	177.33	141.864	144.091	115.273	0.0	0.0
23.113647	1.0	0.0	0.0	144.091	115.273	0.0	0.0

These loads are transferred from the following analysis run:

Location: Span 1

Analysis time: 10/27/2016 15:48:35

Analysis Loadcase - Linebeam with Construction stage 1A

- Factor for Strength: 1.25 Service: 1.0

Job: Utah County Development

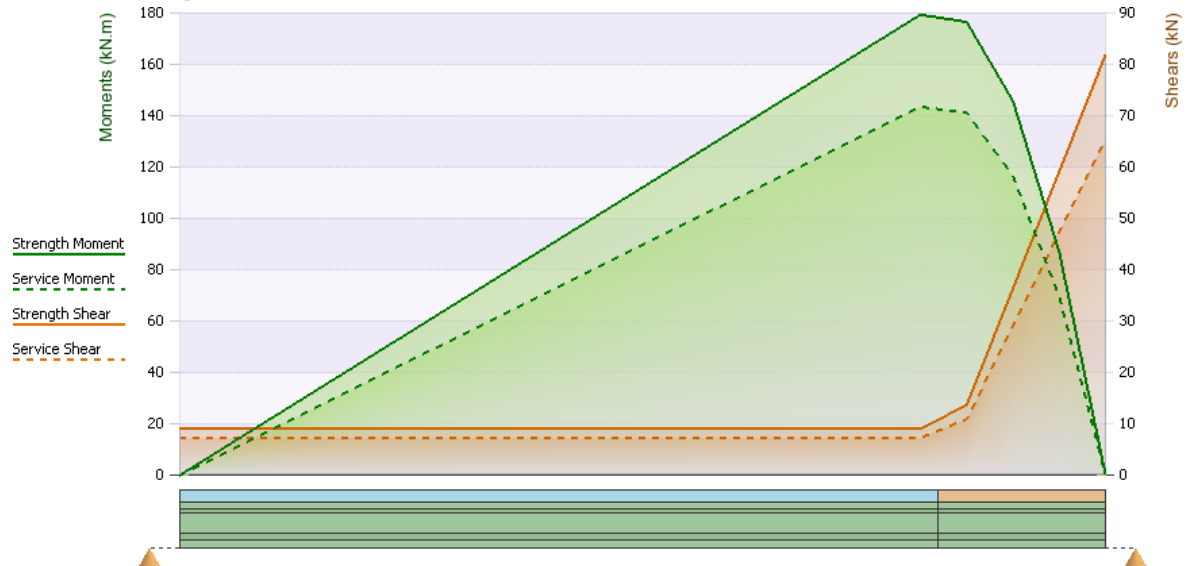
Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

Construction stage 1B



Loading is defined for the distance between beam end faces

Span Location (from left end)		Moment kN.m		Shear kN		Axial kN	
dim (m)	pro	Strength	Service	Strength	Service	Strength	Service
0.0	0.0	0.0	2.44E-4	9.104	7.2832	0.0	0.0
1.1556823	0.05	11.2048	8.96387	9.10278	7.28223	0.0	0.0
2.3113647	0.1	22.4097	17.9277	9.10156	7.28125	0.0	0.0
3.467047	0.15	33.6096	26.8877	9.10645	7.28516	0.0	0.0
4.6227293	0.2	44.8096	35.8477	9.104	7.2832	0.0	0.0
5.7784117	0.25	56.0132	44.8105	9.10156	7.28125	0.0	0.0
6.934094	0.3	67.2192	53.7754	9.09668	7.27734	0.0	0.0
8.0897763	0.35	78.4229	62.7383	9.09668	7.27734	0.0	0.0
9.2454587	0.4	89.6265	71.7012	9.0918	7.27344	0.0	0.0
10.401141	0.45	100.813	80.6504	9.10156	7.28125	0.0	0.0
11.556823	0.5	112.002	89.6016	9.10156	7.28125	0.0	0.0
12.712506	0.55	123.193	98.5547	9.09668	7.27734	0.0	0.0
13.868188	0.6	134.39	107.512	9.08203	7.26562	0.0	0.0
15.02387	0.65	145.581	116.465	9.08691	7.26953	0.0	0.0
16.179553	0.7	156.763	125.41	9.09668	7.27734	0.0	0.0
17.335235	0.75	167.957	134.365	9.0625	7.25	0.0	0.0
18.490917	0.8	179.117	143.294	9.07077	7.25661	0.0	0.0
19.6466	0.85	176.296	141.037	13.6588	10.927	0.0	0.0
20.802282	0.9	145.503	116.403	36.3882	29.1106	0.0	0.0
21.957964	0.95	86.7379	69.3903	59.1151	47.2921	0.0	0.0
23.113647	1.0	0.0	0.0	81.844	65.4752	0.0	0.0

Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

These loads are transferred from the following analysis run:

Location: Span 1

Analysis time: 10/27/2016 15:48:35

Analysis Loadcase - Linebeam with Construction stage 1B
- Factor for Strength: 1.25 Service: 1.0

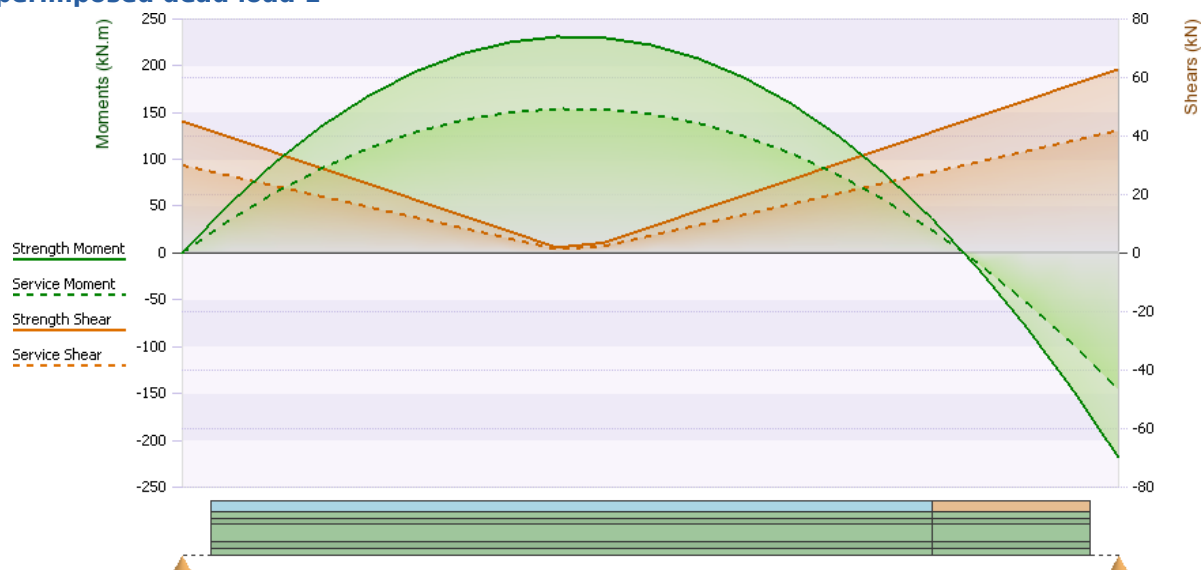
Construction stage 2

- none defined -

Construction stage 3

- none defined -

Superimposed dead load 1



Loading is defined for the distance between supports

ASCENT
630 Peter Jefferson Parkway, Suite 175, Charlottesville, VA
22911



Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

Span Location (from left support)		Moment		Shear		Axial	
		kN.m		kN		kN	
dim (m)	pro	Strength	Service	Strength	Service	Strength	Service
0.0	0.0	0.0	0.0	45.0037	30.0025	0.0	0.0
1.2306823	0.05	52.0712	34.7141	39.6125	26.4083	0.0	0.0
2.4613647	0.1	97.5081	65.0054	34.2204	22.8136	0.0	0.0
3.692047	0.15	136.306	90.8704	28.8357	19.2238	0.0	0.0
4.9227294	0.2	168.476	112.317	23.4494	15.633	0.0	0.0
6.1534117	0.25	194.012	129.342	18.0617	12.0412	0.0	0.0
7.384094	0.3	212.91	141.94	12.6814	8.45424	0.0	0.0
8.6147764	0.35	225.202	150.135	7.28342	4.85561	0.0	0.0
9.8454587	0.4	230.871	153.914	1.86496	1.2433	0.0	0.0
11.076141	0.45	229.85	153.233	3.4993	2.33287	0.0	0.0
12.306823	0.5	222.212	148.141	8.8782	5.9188	0.0	0.0
13.537506	0.55	207.968	138.645	14.2923	9.52818	0.0	0.0
14.768188	0.6	187.048	124.699	19.6712	13.1141	0.0	0.0
15.99887	0.65	159.523	106.348	25.0442	16.6961	0.0	0.0
17.229553	0.7	125.39	83.5935	30.4612	20.3075	0.0	0.0
18.460235	0.75	84.5856	56.3904	35.8548	23.9032	0.0	0.0
19.690917	0.8	37.151	24.7673	41.2425	27.495	0.0	0.0
20.9216	0.85	-16.927	-11.284	46.6382	31.0921	0.0	0.0
22.152282	0.9	-77.639	-51.759	52.0277	34.6852	0.0	0.0
23.382964	0.95	-144.98	-96.655	57.4147	38.2765	0.0	0.0
24.613647	1.0	-218.96	-145.97	62.8028	41.8686	0.0	0.0

These loads are transferred from the following analysis run:

Location: Span 1

Analysis time: 10/27/2016 15:48:35

Analysis Loadcase - Linebeam with Superimposed dead load
- Factor for Strength: 1.5 Service: 1.0

Job: Utah County Development

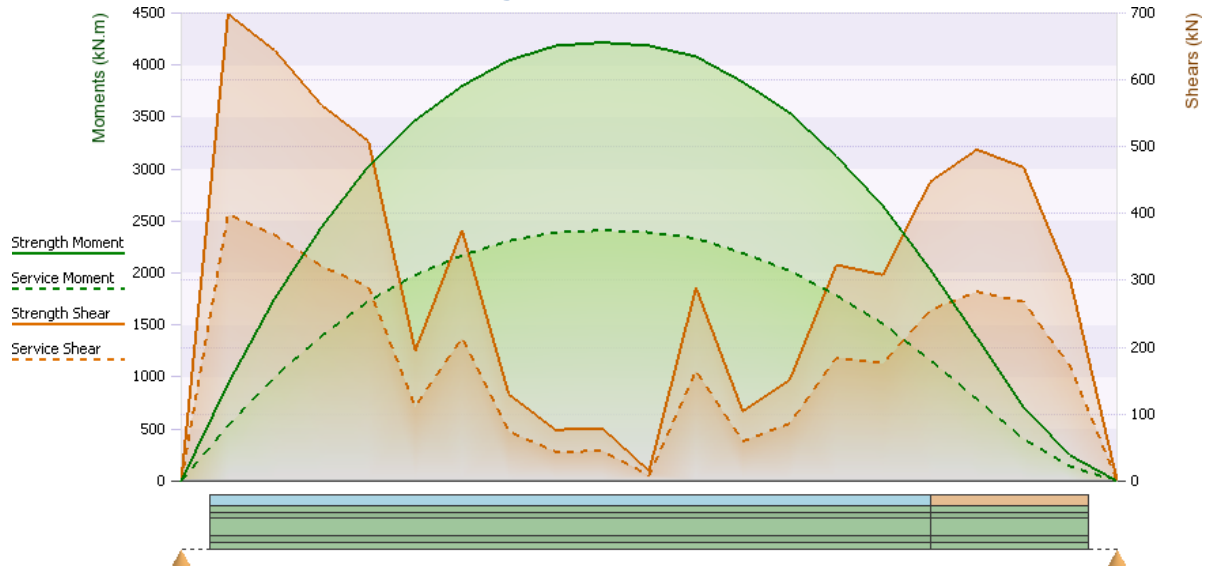
Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

Transient Load BM 1 : [Max +ve] - Strength I & Service



Loading is defined for the distance between supports

Span Location (from left support)		Moment kN.m		Shear kN		Axial kN	
dim (m)	pro	Strength	Service	Strength	Service	Strength	Service
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
1.2306823	0.05	933.653	533.516	698.206	398.975	0.0	0.0
2.4613647	0.1	1757.05	1004.03	643.578	367.759	0.0	0.0
3.692047	0.15	2441.54	1395.16	562.069	321.182	0.0	0.0
4.9227294	0.2	3026.65	1729.52	508.169	290.382	0.0	0.0
6.1534117	0.25	3465.6	1980.34	194.877	111.358	0.0	0.0
7.384094	0.3	3796.91	2169.66	374.847	214.198	0.0	0.0
8.6147764	0.35	4042.67	2310.1	129.432	73.9613	0.0	0.0
9.8454587	0.4	4183.06	2390.32	76.6881	43.8218	0.0	0.0
11.076141	0.45	4215.29	2408.74	78.8976	45.0844	0.0	0.0
12.306823	0.5	4184.44	2391.11	14.9847	8.56269	0.0	0.0
13.537506	0.55	4079.65	2331.23	289.14	165.223	0.0	0.0
14.768188	0.6	3835.13	2191.5	104.081	59.4748	0.0	0.0
15.99887	0.65	3538.84	2022.2	150.813	86.179	0.0	0.0
17.229553	0.7	3121.48	1783.7	323.189	184.679	0.0	0.0
18.460235	0.75	2641.83	1509.62	308.208	176.119	0.0	0.0
19.690917	0.8	2037.27	1164.15	447.208	255.547	0.0	0.0
20.9216	0.85	1379.84	788.478	495.498	283.142	0.0	0.0
22.152282	0.9	708.738	404.993	469.11	268.063	0.0	0.0
23.382964	0.95	245.162	140.092	299.285	171.02	0.0	0.0
24.613647	1.0	0.0	0.0	0.0	0.0	0.0	0.0

The loading shown excludes the distribution factors applied during design.

Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

These loads are transferred from the following analysis run:

Location: Span 1

Analysis time: 10/27/2016 15:48:35

Analysis Loadcase - Moving Load for Maximum +ve Moments
- Factor for Strength: 1.75 Service: 1.0

Transient Load BM 2 : [Max -ve] - Strength I & Service



Loading is defined for the distance between supports

Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

Span Location (from left support)		Moment		Shear		Axial	
		kN.m		kN		kN	
dim (m)	pro	Strength	Service	Strength	Service	Strength	Service
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
1.2306823	0.05	-71.74	-40.994	58.2869	33.3068	0.0	0.0
2.4613647	0.1	-143.47	-81.986	58.2797	33.3027	0.0	0.0
3.692047	0.15	-215.21	-122.97	58.2762	33.3007	0.0	0.0
4.9227294	0.2	-286.9	-163.94	58.2949	33.3114	0.0	0.0
6.1534117	0.25	-358.64	-204.94	58.2452	33.283	0.0	0.0
7.384094	0.3	-430.35	-245.91	58.2747	33.2998	0.0	0.0
8.6147764	0.35	-502.08	-286.9	58.2963	33.3122	0.0	0.0
9.8454587	0.4	-573.84	-327.91	58.2151	33.2657	0.0	0.0
11.076141	0.45	-645.44	-368.82	58.2693	33.2968	0.0	0.0
12.306823	0.5	-717.13	-409.79	58.2228	33.2702	0.0	0.0
13.537506	0.55	-788.75	-450.71	58.2081	33.2618	0.0	0.0
14.768188	0.6	-860.34	-491.62	58.2702	33.2972	0.0	0.0
15.99887	0.65	-932.01	-532.58	58.2872	33.307	0.0	0.0
17.229553	0.7	-1003.8	-573.58	58.1495	33.2283	0.0	0.0
18.460235	0.75	-1075.4	-614.49	58.0351	33.1629	0.0	0.0
19.690917	0.8	-1146.8	-655.34	58.0488	33.1707	0.0	0.0
20.9216	0.85	-1218.3	-696.16	57.9702	33.1258	0.0	0.0
22.152282	0.9	-1347.8	-770.19	374.808	214.176	0.0	0.0
23.382964	0.95	-1923.8	-1099.3	539.306	308.175	0.0	0.0
24.613647	1.0	-2644.2	-1511.0	630.837	360.478	0.0	0.0

The loading shown excludes the distribution factors applied during design.
These loads are transferred from the following analysis run:

Location: Span 1
Analysis time: 10/27/2016 15:48:35
Analysis Loadcase - Moving Load for Maximum -ve Moments
- Factor for Strength: 1.75 Service: 1.0

Job: Utah County Development

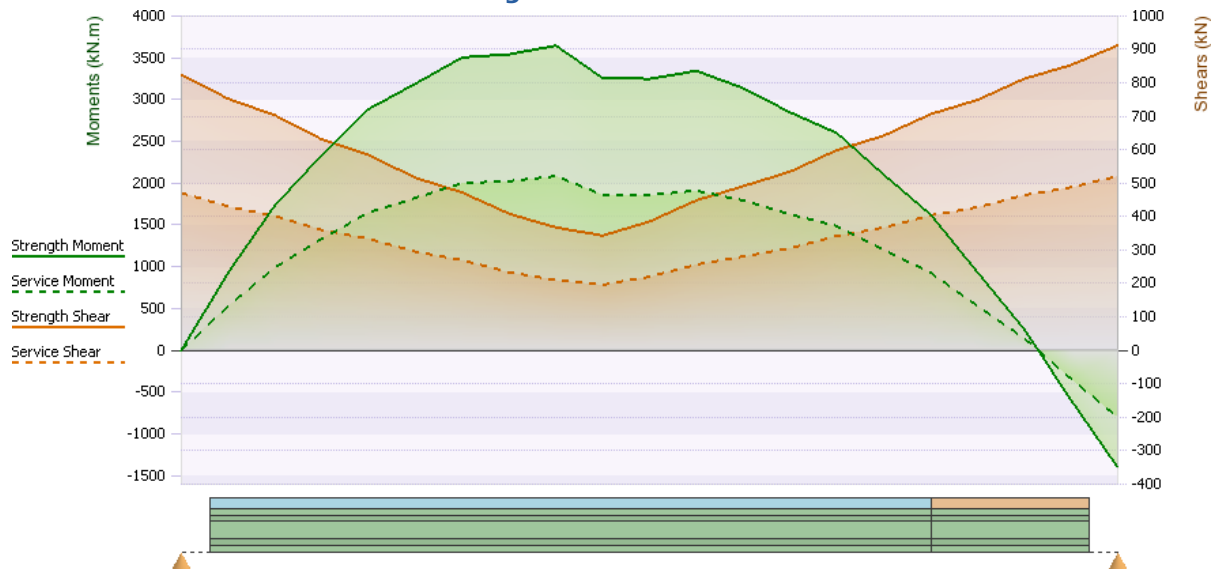
Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

Transient Load SF + assoc. BM 1 - Strength I & Service



Loading is defined for the distance between supports

Span Location (from left support)		Moment		Shear		Axial	
		kN.m		kN		kN	
dim (m)	pro	Strength	Service	Strength	Service	Strength	Service
0.0	0.0	0.0	0.0	823.866	470.781	0.0	0.0
1.2306823	0.05	927.791	530.166	752.11	429.777	0.0	0.0
2.4613647	0.1	1734.18	990.961	702.709	401.548	0.0	0.0
3.692047	0.15	2336.32	1335.04	630.469	360.268	0.0	0.0
4.9227294	0.2	2885.1	1648.63	583.846	333.627	0.0	0.0
6.1534117	0.25	3189.06	1822.32	515.731	294.703	0.0	0.0
7.384094	0.3	3502.48	2001.42	471.718	269.553	0.0	0.0
8.6147764	0.35	3540.0	2022.86	408.164	233.237	0.0	0.0
9.8454587	0.4	3643.81	2082.18	367.195	209.826	0.0	0.0
11.076141	0.45	3254.11	1859.49	343.006	196.004	0.0	0.0
12.306823	0.5	3247.22	1855.56	385.062	220.036	0.0	0.0
13.537506	0.55	3341.79	1909.59	448.516	256.295	0.0	0.0
14.768188	0.6	3133.53	1790.59	490.886	280.506	0.0	0.0
15.99887	0.65	2845.29	1625.88	534.287	305.307	0.0	0.0
17.229553	0.7	2596.97	1483.98	598.752	342.144	0.0	0.0
18.460235	0.75	2099.92	1199.95	641.84	366.765	0.0	0.0
19.690917	0.8	1623.19	927.539	706.073	403.47	0.0	0.0
20.9216	0.85	933.739	533.565	748.777	427.873	0.0	0.0
22.152282	0.9	250.131	142.932	811.939	463.965	0.0	0.0
23.382964	0.95	-597.3	-341.31	852.994	487.425	0.0	0.0
24.613647	1.0	-1404.9	-802.81	911.837	521.05	0.0	0.0

The loading shown excludes the distribution factors applied during design.

ASCENT
630 Peter Jefferson Parkway, Suite 175, Charlottesville, VA
22911



Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

These loads are transferred from the following analysis run:

Location: Span 1

Analysis time: 10/27/2016 15:48:35

Analysis Loadcase - Moving Load for Maximum Shears

- Factor for Strength: 1.75 Service: 1.0

ASCENT
630 Peter Jefferson Parkway, Suite 175, Charlottesville, VA
22911



Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

STRUCTURE GEOMETRY

Line Beam Structure with 2 spans as follows:

Span Ref	Span Length m	Elements in span	Support at Left of span	
			Displacement	Rotation
1	24.6136	20	fixed	free
2	23.514	19	fixed	free
	End support:		fixed	free

Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

STRUCTURE PROPERTIES

STRUCTURE PROPERTY DATA

SP1: PS Beam

Type: Prestressed Design Beam
Reference: SB1: Pre-tensioned Prestressed
Material: MP2: C56 Es 37.4
Slab density factor: 1.0

Ref	Dim m	A_x mm ²	A_y mm ²	A_z mm ²	I_y mm ⁴	I_z mm ⁴	C mm ⁴	γ kN/m ³
1	-0.13465	844160.5	0.0	0.0	1.809E11	1.75E11	1.623E10	27.38602
2	15.86421	875994.0	0.0	0.0	1.863E11	1.86E11	1.623E10	26.816766
3	20.78694	398320.8	0.0	0.0	7.755E10	1.84E10	1.623E10	58.975904
4	23.24831	360967.0	0.0	0.0	5.219E10	5.0849E9	1.623E10	64.04518

Notes: Axes refer to line beam local axes.

γ = (unit length weight) / (transformed section area)

Cracked Section Details:

from left: 0.0 m

from right: 3.46705 m

Assigned to the following line beam spans:

1

SP2: PS Beam

Type: Prestressed Design Beam
Reference: SB2: Pre-tensioned Prestressed
Material: MP2: C56 Es 37.4
Slab density factor: 1.0

Ref	Dim m	A_x mm ²	A_y mm ²	A_z mm ²	I_y mm ⁴	I_z mm ⁴	C mm ⁴	γ kN/m ³
1	-0.13121	360967.0	0.0	0.0	5.219E10	5.0849E9	1.623E10	64.015418
2	1.106365	398320.8	0.0	0.0	7.755E10	1.84E10	1.623E10	58.948933
3	3.581519	875994.0	0.0	0.0	1.863E11	1.86E11	1.623E10	26.804503
4	8.531826	844160.5	0.0	0.0	1.809E11	1.75E11	1.623E10	27.373294

Notes: Axes refer to line beam local axes.

ASCENT
630 Peter Jefferson Parkway, Suite 175, Charlottesville, VA
22911



Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

$$\gamma = (\text{unit length weight}) / (\text{transformed section area})$$

Cracked Section Details:

from left: 3.30209 m

from right: 0.0 m

Assigned to the following line beam spans:

2

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22911



Job: Utah County Development

Job No.: 2015720
Calc. By: MLR

Project: White Water Park

Checked:

Data File: BRIDGE_2_G11.sst 10/27/2016 9:52:12

STRUCTURE LOADS

LIVE LOAD ENVELOPE DATA

The following vehicles may be included in the envelope, in addition to the lane load of 0.009 MPa which is always included:

- Design Truck
- Design Tandem
- Double Design Truck
- Double Design Tandem

The Dynamic Load Allowance for these vehicles is 33%

Vehicles move in both directions at increments of 0.5 m